



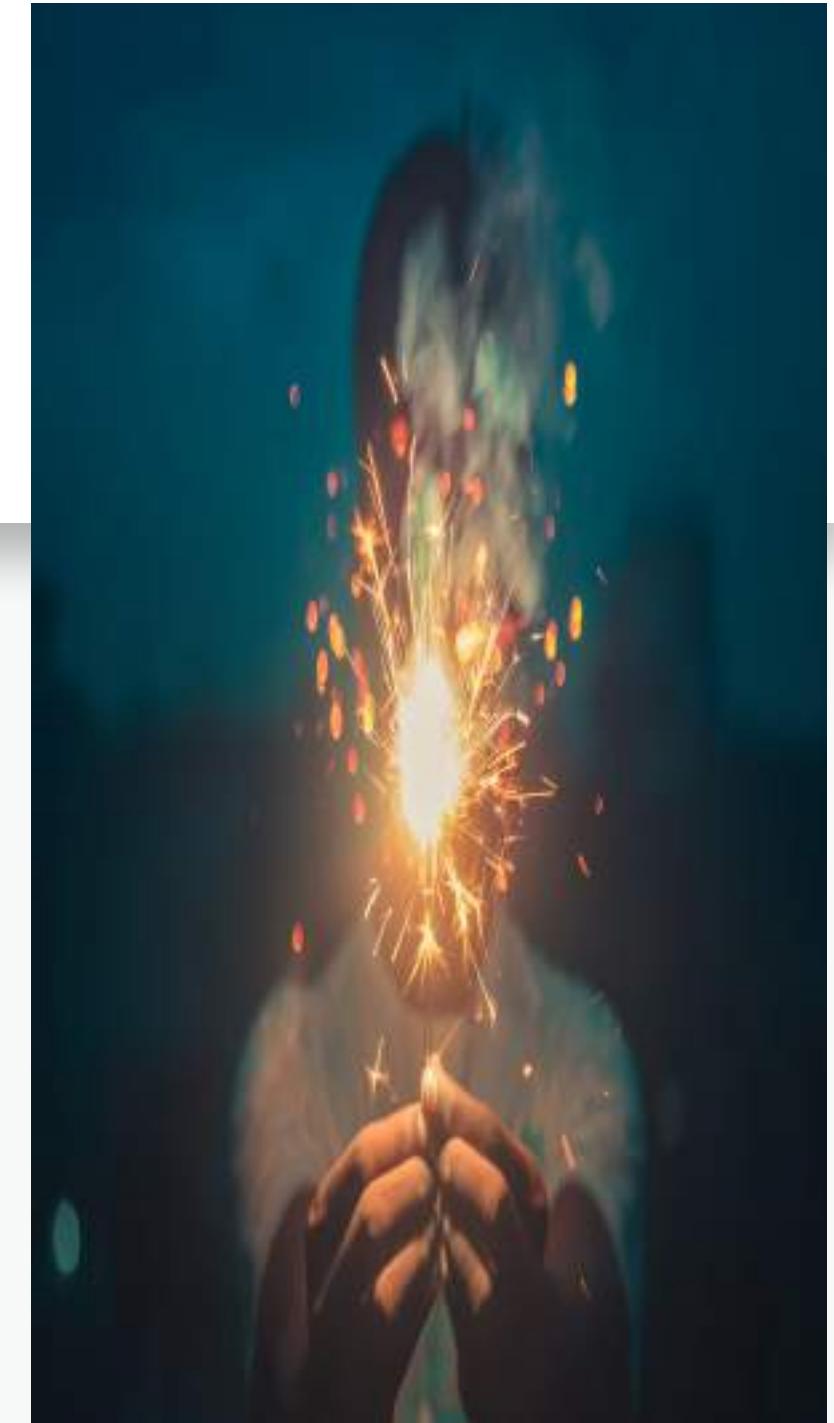
وزارة التعليم العالي والبحث العلمي  
الجامعة التقنية الجنوبية  
المعهد التقني التكنولوجي / قسم التقنيات الالكترونية

# ELECTRICAL CIRCUITS AND MEASUREMENTS

## الدوائر الكهربائية والقياسات

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ماجستير هندسة السيطرة والحسابات



# المنهاج الدراسي لمادة الدوائر الكهربائية

قسم التقنيات الالكترونية

المرحلة الأولى

لعام الدراسي 2024/2025





بسم الله الرحمن الرحيم

"ربی اشرح لي صدري ويسر لي امري واحلل  
عقدة من لسانني يفقهوا قولی"

صدق الله العظيم

**عنوان الحقيبة : الدوائر الكهربائية والقياسات**

**الفئة المستهدفة : طلبة المرحلة الأولى قسم التقنيات الالكترونية**

**المؤسسة التعليمية : الجامعة التقنية الجنوبية /المعهد التقني  
التكنولوجي قسم التقنيات الالكترونية**

**الأنشطة التدريبية: حضوري + أنشطة تفاعلية + أنشطة الكترونية**



## وصف الحقيبة

حقيبة دراسية لمدة ثمانية أسابيع بواقع ساعة ونصف في الأسبوع لطلبة المرحلة الأولى من قسم التقنيات الالكترونية . سيكتسب الطالب من خلال هذه الحقيبة التعليمية العديد من المهارات التي سيستفاد منها خلال مسيرته الدراسية للسنوات القادمة .

تضمنت الحقيبة بعض وسائل الايضاح ومقاطع الفيديو التوضيحية والمهام والنشاطات والواجبات التي ستعزز من مقدرة الطالب في تحليل الدوائر الكهربائية وتعزز من امكانياته العقلية والرياضية والعصف الذهني من خلال حل العديد من المعادلات الرياضية.



## الأهداف العامة :

- فهم المبادئ الأساسية للدوائر الكهربائية
- تحليل الدوائر الكهربائية البسيطة والمعقدة
- دراسة عناصر الدوائر الأساسية
- فهم استجابة الدوائر الكهربائية
- تمكين الطلبة من استخدام برامج المحاكاة
- تعزيز التفكير المنطقي والتحليلي لدى الطالب



**المخرجات التعليمية لمقرر مادة الدوائر الكهربائية**  
في نهاية هذا المقرر يتوقع ان يكون الطالب قادرًا على :



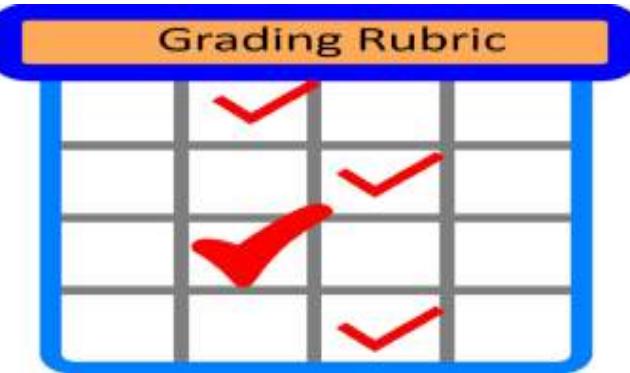
# الفهرست

الاسبوع	عنوان المحاضرة	
الأسبوع الأول	قانون اوم وأنواع الربط	
الأسبوع الثاني	الربط المختلط	
الأسبوع الثالث	ربط دلتا ستار	
الأسبوع الرابع	قوانين كيرشوف	
الأسبوع الخامس	نظرية ثيفن	
الأسبوع السادس	نظرية نورتن	
الأسبوع السابع	نظرية تحويل المصادر	
الأسبوع الثامن	نظرية التراكب	

# الجدول الزمني

رقم القاعة	المدة الزمنية (ساعة)	طريقة التدريس	الاسبوع	سلسل المحاضرة
ق 1	ساعة ونصف	حضورى+نشاط تفاعلى +اختبار الكترونى(مهمه جماعية)	الأول	المحاضرة الأولى(قانون اوم)
ق 1	ساعة ونصف	حضورى+ نشاط تفاعلى+ مقطع فيديو توضيحي + واجب الكترونى	الثاني	المحاضرة الثانية(أنواع الربط)
ق 2	ساعة ونصف	تفاعلی+ واجب الكترونى+ رابط الكترونى لفيديو تعليمي	الثالث	المحاضرة الثالثة (ربط دلتا-ستار)
القاعة المركزية	ساعة ونصف	حضورى+نشاط تفاعلى + رابط فيديو توضيحي + اختبار الكترونى	الرابع	المحاضرة الرابعة(قوانين كيرشوف)
القاعة المركزية	ساعة ونصف	حضورى+نشاط تفاعلى + مقطع فيديو توضيحي +اختبار الكترونى	الخامس	المحاضرة الخامسة(نظرية ثيفن)
القاعة المركزية	ساعة ونصف	حضورى+نشاط تفاعلى +اختبار الكترونى	السادس	المحاضرة السادسة(نظرية نورتن)
ق 2	ساعة ونصف	حضورى+نشاط تفاعلى+اختبار الكترونى	السابع	المحاضرة السابعة( تحويل المقاومات)

## المنهج التقويمي :



يعتبر تقويم البرنامج التعليمي لمادة الدوائر الكهربائية مهم جدا لنجاح برنامج الحقيقة والوصول الى الأهداف المطلوبة ويبين مدى اكتساب المتربين للمهارات العلمية في تحليل الدوائر الكهربائية اختبار قبلي



أنشطة اثناء التدريب



اختبار بعدي

# دليل الفيديوهات



اسم الفيديو	اسم ورقم المحاضرة
فديو قصير + رابط الفيديو على اليوتيوب لتوضيح قاعدة مقسم التيار	الحاضر رقم 2 / الرابط المختلط ص 10
رابط فديو توضيحي لمحاضرة دلتا - ستار	الحاضر رقم 3 / الرابط النجمي المثلثي (دلتا- ستار)
رابط فديو توضيحي لتحليل الدوائر الكهربائية باستخدام تيارات ماكسويل الدوارة	الحاضر رقم 4 / قوانين كيرشوف
فديو قصير + رابط الفيديو على اليوتيوب شرح مختصر لنظرية ثفنن	الحاضر رقم 5 / نظرية ثفنن
رابط المحاضرة على منصة التدريبو	الحاضر رقم 8 / نظرية التراكب

المحاضرة الأولى

# Unit system

Rational :

- its very important to study units system
- also to study the elements effects of a  
.resistance

# :Central idea

Define voltage , current and resistance -

Define unit system -

The element effect at resistance -



# :Aim of lecture

To let the student be able to identify and analysis different elements effects at resistance value

# :Pretest

define : current , potential difference -1

write Ohm`s law -2

# Unit system

Quantity	unit	symbol
Length	meter	M
Mass	Kilogram	Kg
Time	Second	S
Current	Amper	A
درجة الحرارة Temperature	Kelvin	K
Luminous intensity شدة الإضاءة	candela	cd

:From the basic quantity we can derive

Quantity	unit	symbol
Electric charge	Coulomb	C
Electric potential	Volt	V
Resistance	Ohm	$\Omega$
Capacitance	Farad	F
Inductance	Henry	H
Conductance	Siemens , mho	S
Frequency	Hertz	Hz
Power	watt	W

# :nations

$$1 = 10^0$$

$$10 = 10^1$$

$$100 = 10^2$$

$$1000 = 10^3$$

$$1/10 = 0.1 = 10^{-1}$$

$$1/100 = 0.01 = 10^{-2}$$

$$1/1000 = 0.001 = 10^{-3}$$

Power of 10	prefix	symbol
$10^6$	Mega	M
$10^3$	Kilo	K
$10^{-3}$	mille	m
$10^{-6}$	Micro	$\mu$
$10^{-9}$	Nano	n
$10^{-12}$	pico	p
$10^9$	gaga	G

## :The elements effect at rssistance value

- . Resistance varies directly with ( Length ) { L }
- . It varies inversely with ( the cross section area) { A } -2
- .It depends on the nature of the material { specificin ( p ) } -3
- . It also depends on the temperature of the conductor { T } -4

$$m \Omega = 2.m \Omega = R. A / L \quad \rho , \quad ) \Omega . I/A ( \rho \therefore R = R \times L/A .$$

m

.When R: resistance,  $\rho$ = specificin or resistivity , L= length  
A=cross section area

**Ex1:** A rectangular carbon block has dimensions ( 1 cm ,1 cm ,50 cm ) .

- 1- what is the resistance measured between the two square ends .
- 2- Between two opposing rectangular faces if  $P = 3.5 \times 10^{-5} \Omega \cdot m$

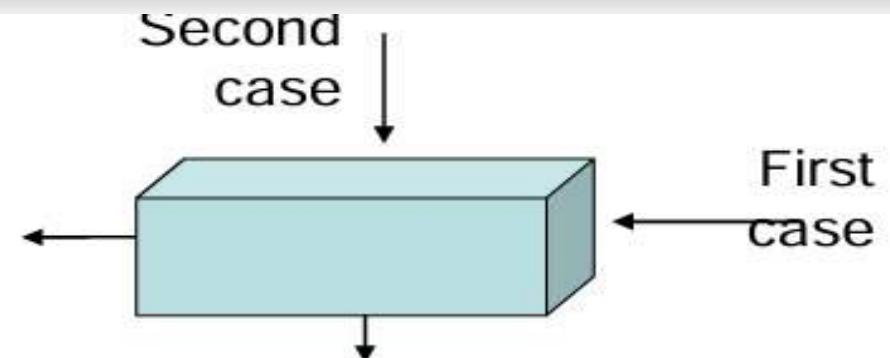
**Solution:** •

$$1- R = P \cdot L / A \ (\Omega) = 3.5 \times 10^{-5} \times 0.5 / (1 \times 10^{-2} \times 1 \times 10^{-2})$$

$$\therefore R = 0.175 \ \Omega$$

$$2- R = P \cdot L / A \ \Omega = 3.5 \times 10^{-5} \times 1 \times 10^{-2} / (1 \times 10^{-2} \times 50 \times 10^{-2})$$

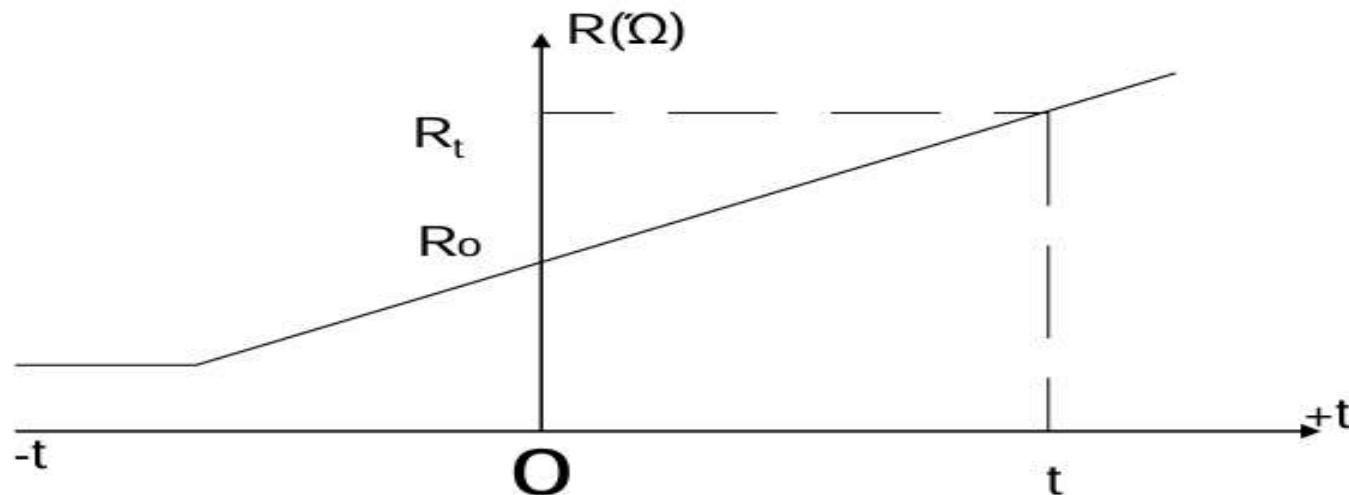
$$\therefore R = 0.00007 \ \Omega$$



**Ex 2:** The wire resistance equal to (40  $\Omega$ ) and length (1km) if the resistivity=  $2 \times 10^{-8} \Omega \cdot m$  , calculate: the diameter of the circular type wire.

**Solution :** Area =  $(r^2 / 2) \cdot \pi$  ,  $R = P \cdot L / A \ \Omega$   $\therefore A = P \cdot L / R = (2 \times 10^{-8} \times 1 \times 10^3) / 40 = 0.5 \times 10^{-6} \ m^2$

The temperature effects at the resistance  
The resistance of the material depends on the temperature, When ( $T$ ) increased,  $R$  also increased



Let the resistance of a conductor at  $0^\circ\text{C}$  =  $R_0 \Omega$

Let the resistance of a conductor at  $t^\circ\text{C}$  =  $R_t \Omega$

Let the temperature coefficient of material at  $0^\circ\text{C}$  =  $\alpha_{e0} / \text{k}$

Let the temperature coefficient of material at  $t^\circ\text{C}$  =  $\alpha_{et} / \text{k}$

1-  $R_t = R_0(1 + \alpha_{e0}t)$

2-  $R_2 = R_1(1 + \alpha_{e1}(t_2 - t_1))$

3-  $\alpha_{et} = \alpha_{e0} / (1 + \alpha_{e0} \cdot t)$

4-  $\alpha_{et} = (R_t - R_0) / R_t \cdot t$

**Ex.3:** A lamp of (100 watt) power, (240 volt) reaches ( $2000^{\circ}\text{C}$ ) if the temperature coefficient of the lamp at ( $15^{\circ}\text{C}$ ) is  $\alpha=5\times10^{-3} / \text{K}$  calculate the current through the lamp



**Solution:**  $P = V^2 / R \quad \therefore R = (240)^2 / 100 = 576\Omega$

$$R_2 = R_1(1 + \alpha e_1(t_2 - t_1)) \quad \therefore 576 = R_1[1 + 5 \times 10^{-3} (2000 - 15)]$$
$$576 = R_1(1 + 9.92), \quad R_1 = 576 / 10.92 = 52.7 \Omega \quad \therefore I = V / R = 240 / 52.7 = 4.55A$$

∴

**Ex.(4):** Palatine coil of resistance ( $3.717\Omega$ ) at ( $100^{\circ}\text{C}$ ). Calculate  
1-The resistance at zero degree. 2- the temperature coefficient of  
resistance at  $40^{\circ}\text{C}$  **( H.W )**

**Notes:** 1-  $R_0 = 2.781 \Omega$   
2-  $\alpha e t = 0.00284/\text{k}$

**Ex5 :** A(1A) pass through a copper conductor the Potential difference through it is (10 v) at (20°C) after Sam times the current decrease to (0.95A) , (Potential difference not changed ) , Find the temperature of the conductor if the temperature coefficient of the copper at zero °C ( $\alpha_{e0}$ )=  $4.28 \times 10^{-3}/k$

**Solution:**  $R_1 = V/I_1 = 10/1 = 10\Omega$  ,  $R_2 = V/I_2 = 10/0.95 = 10.53\Omega$  ,

$$R_t = R_0(1 + \alpha_e \cdot t) \quad \therefore R_1/R_2 = R_0(1 + \alpha_e \cdot t_1)/R_0(1 + \alpha_e \cdot t_2)$$

$$\therefore 10/10.53 = (1 + 4.28 \times 10^{-3} \times 20) / (1 + 4.28 \times 10^{-3} \times t_2) \quad \therefore t_2 = 33.4^\circ C$$

Ex:(7) An electric heater takes a current of (15A) from a (115v) source. The cables connecting the heater to the supply are each (43m) long. If the voltage drop along the cables is not exceed (12v) .Determine the diameter of suitable copper wire and select  $\rho=1.72\times10^{-8} \Omega\cdot m$

### Solution

$$R = E/I = 12/15 = 0.8 \Omega \quad , \text{total length of wire} = 2 \times 43 = 86 \text{m}$$

$$R = \rho \cdot L / A \quad \therefore A = \rho \cdot L / R = (1.72 \times 10^{-8} \times 86) / 0.8 = 1.849 \times 10^{-6} \text{ m}^2$$

$$A = [(1/2) \cdot d]^2 \cdot \pi$$

$$A = (d^2/4) \cdot \pi \quad \therefore d^2 = 4A/\pi \quad \therefore d = \sqrt{4A/\pi}$$

$$d = \sqrt{4 \times 1.849 \times 10^{-6} / \pi} = 1.5 \text{mm}$$

# :Second lecture

Direct current circuits

Resistance connection

$$\phi(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{\frac{(x-\mu)^2}{2\sigma^2}}$$

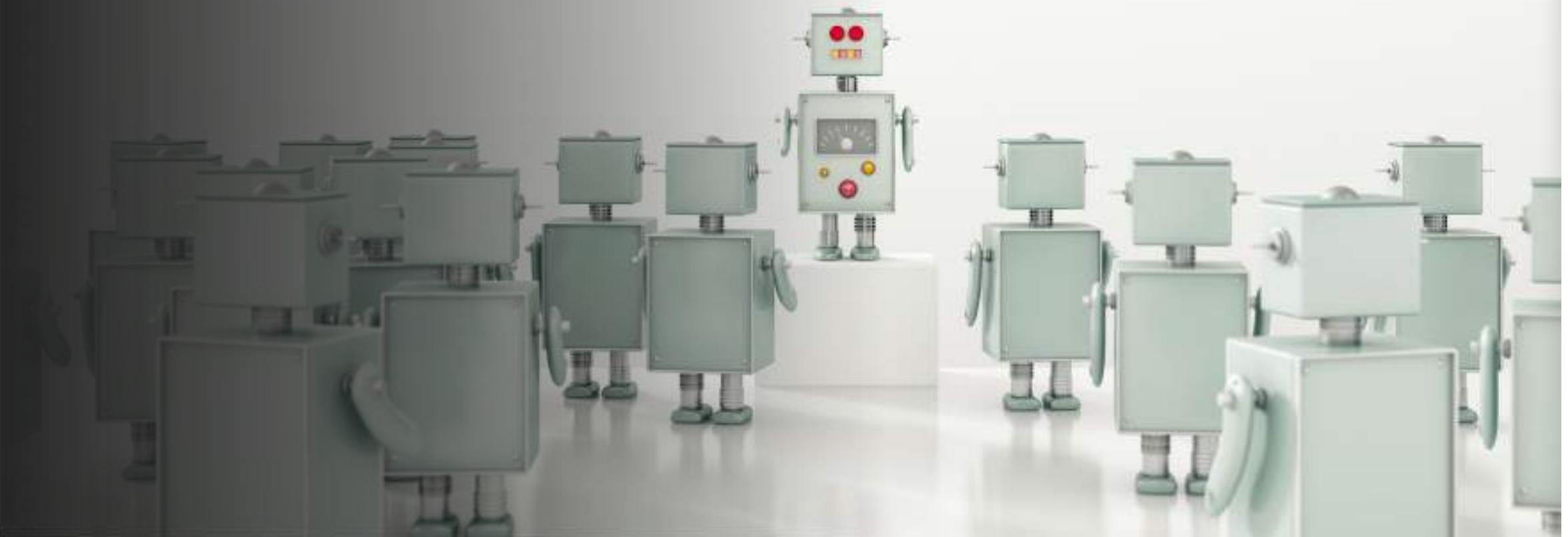
$$E = mc^2$$

$$dS \geq 0$$

$$\frac{df}{dt} = \lim_{h \rightarrow 0} \frac{f(t+h) - f(t)}{h}$$

الاختبار القبلي :

ماذا تعرف عن ربط التوالى؟



## مبررات الوحدة

### B –Rationale

- It is very important to study  
**Resistances connection:**  
Series circuit, Parallel circuits and complex connection
- Also to study **Voltage divider rule ,**  
**the current divider rule and Ohms' law**

# :Central idea

connect the resistance as series -

.parallel and complex,

.Ohms, law •

.

.Voltage divider rule, the current divider rule •

## : Aim of lecture

To let the student be able to identify the analyses different kind of resistance connection (series, parallel ,complex)

## Pretest

الاختبار القبلي

1): If number of resistances connection in series write total voltage , current laws .

2 ) If number of resistances connection in Parallel wrights total voltage , current laws .

## solution

$$1) V_T = V_1 + V_2 + \dots + V_n , I_T = I_1 = I_2 = I_n$$

$$2) I_T = I_1 + I_2 + \dots + I_n , V_T = V_1 = V_2 = V_n$$

# **:CLASSIFICATION OF ELECTRIC CIRCUIT**

**.Series Circuit-1**

**.Parallel Circuit-2**

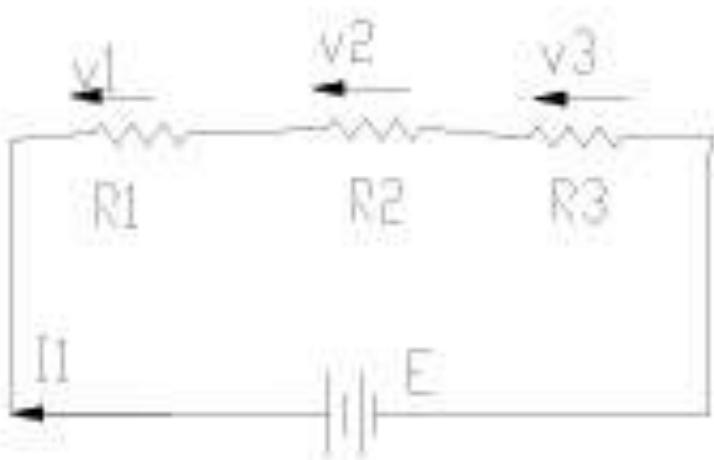
**.Series Parallel Circuit-3**

**.Mesh or Network Circuit-4**



1

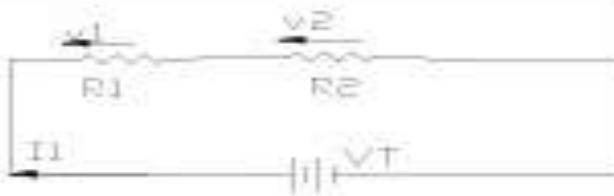
# Series circuit



$$I = I_1 = I_2 = I_3 = \dots = I_n$$

$$V_T = V_1 + V_2 + V_3 + \dots + V_n$$

# قانون تقسيم الفولتية Voltage divider rule



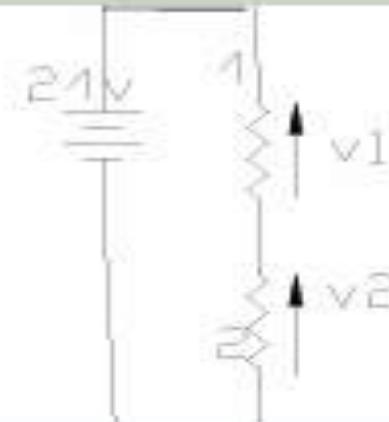
$$V_1 = I \cdot R_1 = V_T \cdot R_1 / (R_1 + R_2)$$

$$V_2 = I \cdot R_2 = V_T \cdot R_2 / (R_1 + R_2)$$

Ex: By using V.d. r. Find V<sub>1</sub>, V<sub>2</sub>

$$\begin{aligned} V_1 &= V_T \cdot R_1 / (R_1 + R_2) \\ &= 24 \cdot 4 / (4 + 2) = 16 \text{v} \end{aligned}$$

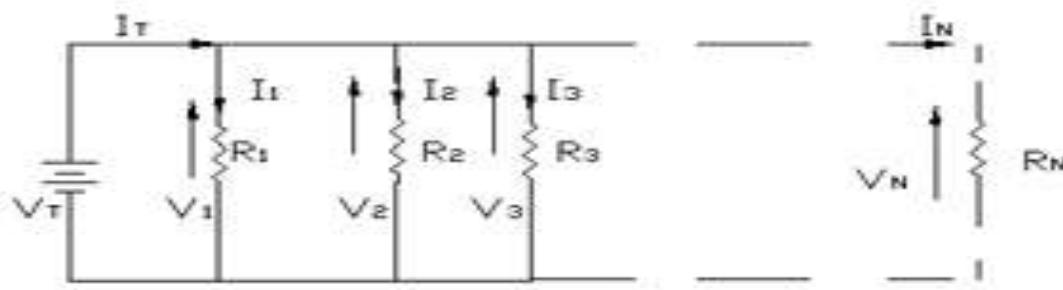
$$\begin{aligned} V_2 &= V_T \cdot R_2 / (R_1 + R_2) \\ &= 24 \cdot 2 / (4 + 2) = 8 \text{v} \end{aligned}$$



2

## Parallel circuits

دوائر التوازي



$$V_T = V_1 = V_2 = V_3 = \dots = V_N$$

$$I_T = I_1 + I_2 + I_3 + \dots + I_N$$

$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots + \frac{1}{R_N}$$

$$G_T = G_1 + G_2 + G_3 + \dots + G_N , \quad \{G = \frac{1}{R}\}$$

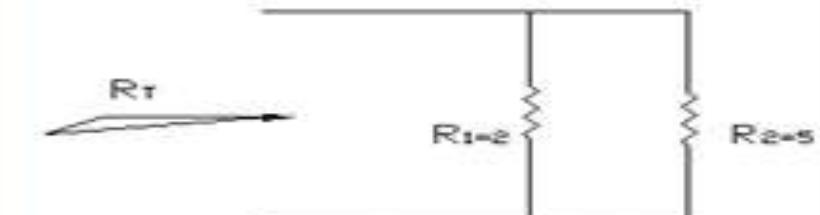
(مو) الموصليات

For two resistance parallel connected as shown in fig.

$$\frac{1}{R_T} = \frac{1}{2} + \frac{1}{5} = \frac{7}{10} \therefore R_T = \frac{10}{7} = 1.4\Omega$$

OR:  $R_T = \frac{R_1 \cdot R_2}{R_1 + R_2}$

$$= \frac{2 \times 5}{(2+5)} = \frac{10}{7} = 1.4\Omega$$

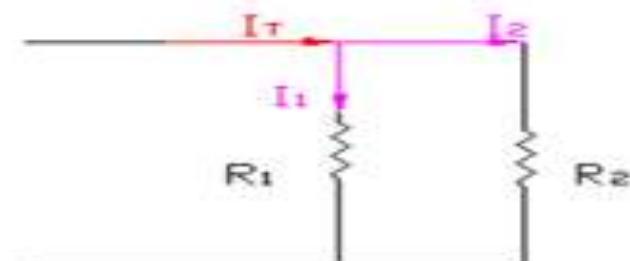


## The current divider rule (قانون تقسيم التيارات)

$$I_1 = \frac{V}{R_1} = I_T \times \frac{R_1 \cdot R_2}{R_1 + R_2}$$

$$\therefore I_1 = \frac{R_2}{R_1 + R_2} \cdot I_T$$

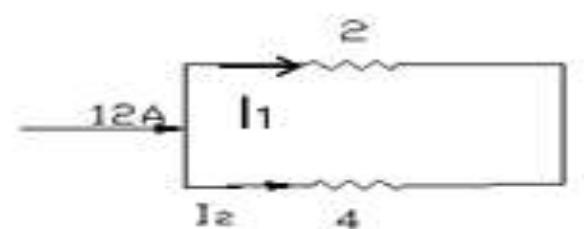
Also:  $I_2 = \frac{R_1}{R_1 + R_2} \cdot I_T$



**EX(1) :Find I<sub>1</sub>, I<sub>2</sub> For the cct. Shown ;**

Solution;  $I_1 = \frac{R_2}{R_1 + R_2} \times I_T = \frac{4}{2+4} \times 12 = 8A$

$$I_2 = \frac{2}{2+4} \times 12 = 4A$$

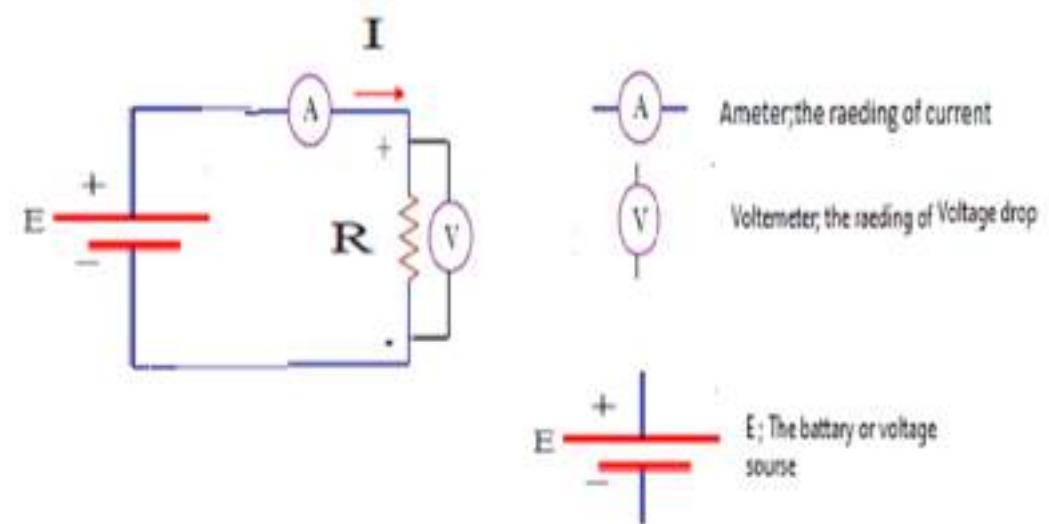


# قانون اوم : OHM's LAW

At a constant temperature; the current flowing through the circuit is directly proportional to the voltage and inversely proportional to the resistance

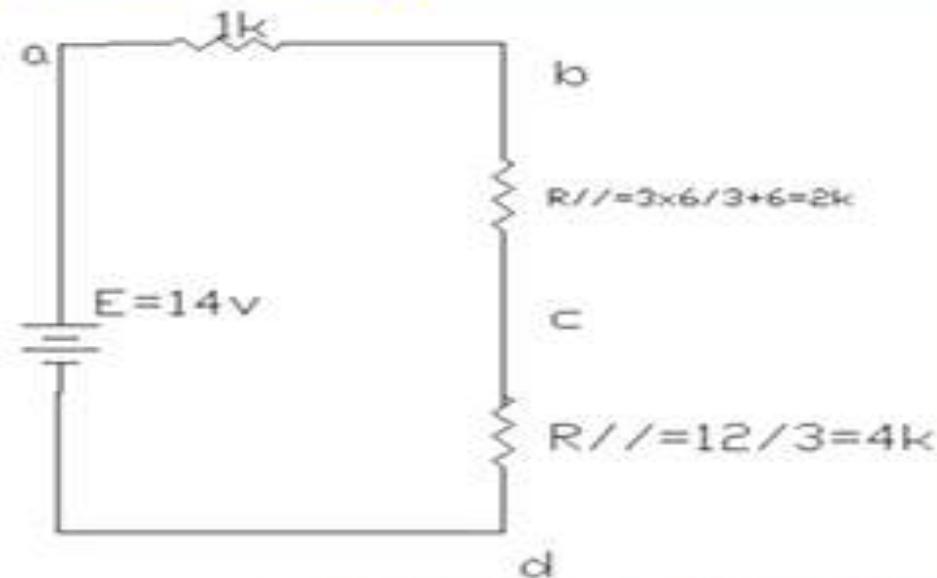
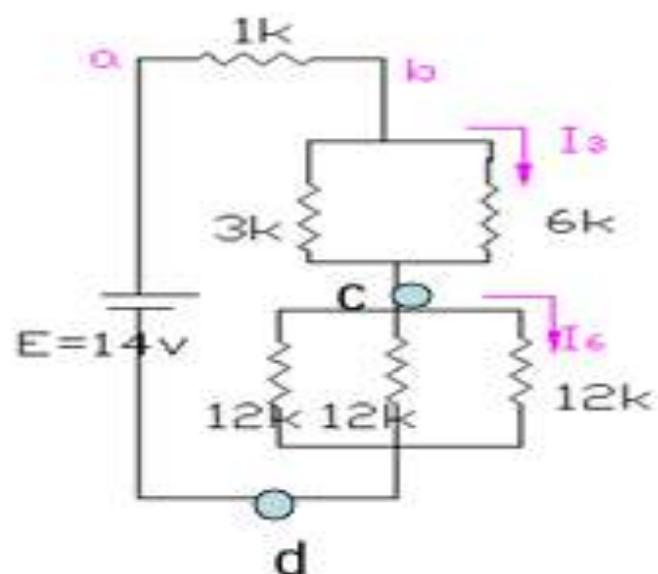
**Current = Voltage/ Resistance**

or:  $I=V/R$  (A)



Ex(2); Find  $V_{ad}$ ,  $V_{ab}$ ,  $V_{bc}$ ,  $V_{cd}$ ,  $I_3$ ,  $I_6$

solution



$$\therefore RT = 7k \Omega \therefore I_T = 14 / 7k = 2mA$$

$$\therefore V_{ab} = 2mA \times 1k = 2V \quad V_{bc} = 2mA \times 2k = 4V$$

$$V_{cd} = 2mA \times 4k = 8V$$

$$I_3 = 2mA \times 3k / (3k + 6k) = 0.666mA$$

$$I_6 = 8V / 12k = 0.666mA$$

# EXAMPLE :

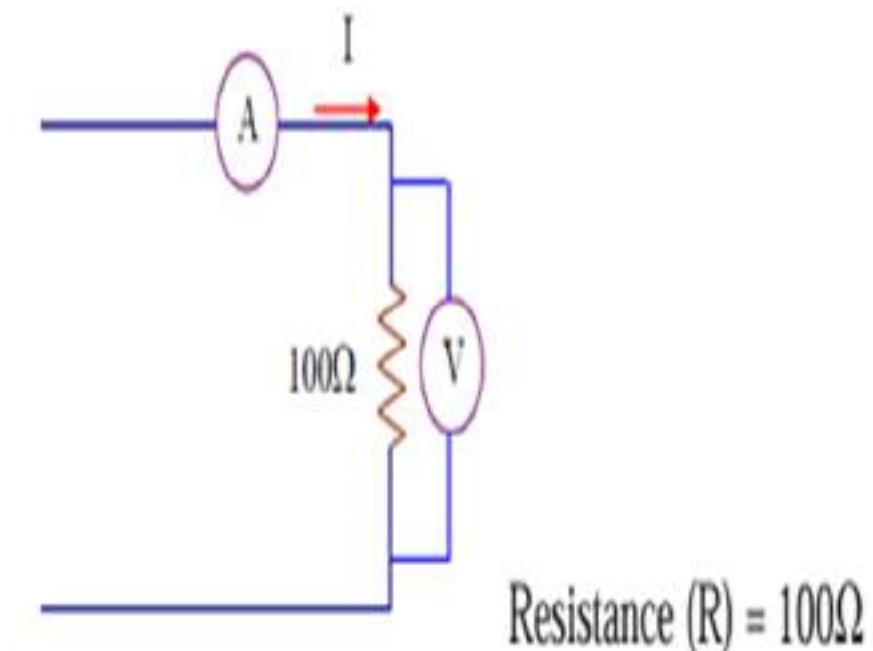
The supply voltage of the circuit is 50V (reading of voltemetr ) and the resistance value is  $100 \Omega$ . Calculate the current flowing through this circuit  
( reading of ameter ).(V=50V)

## :SOLUTION

:By using ohms law

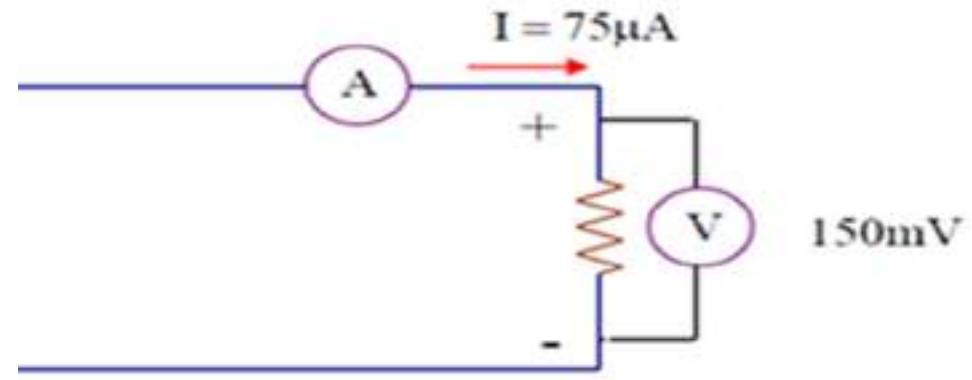
$$I = V/R$$

$$I = 50/100 = 0.5 \text{ A}$$





For a given circuit the reading of voltmeter is 150mV. and the reading of ammeter is  $75\mu\text{A}$  . Calculate the resistance value of the circuit

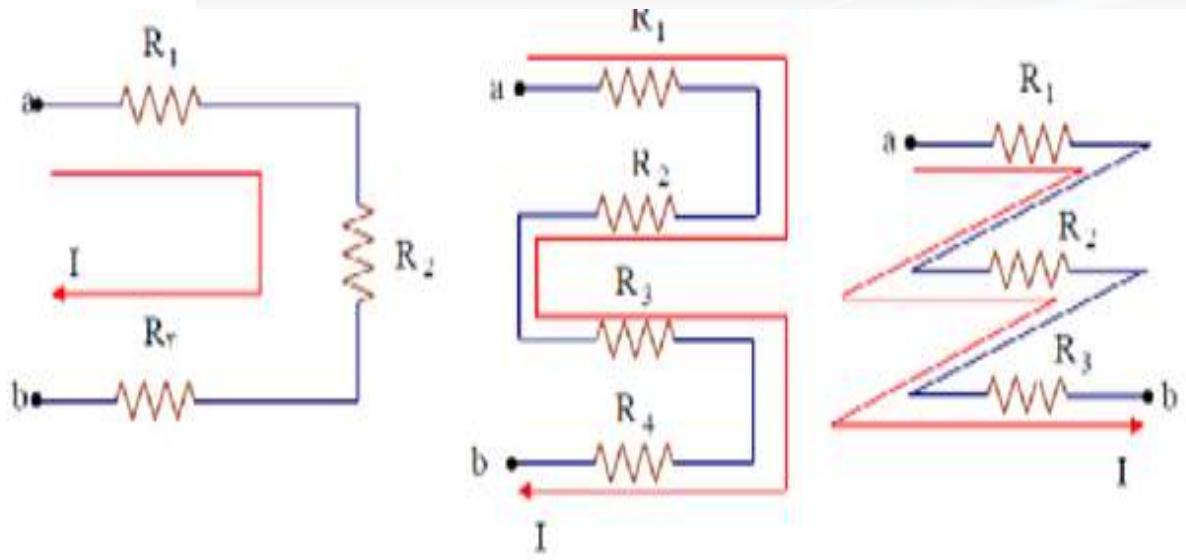


نشاط  
نشاط تفاعلي داخل  
المحاضرة



# :SEIRIES CIRCUITS

I" ampere current flows in all" resistors" ,For agivin circuit ( E )is electromotive force of power supply ,V is total voltage of source or ( VS )



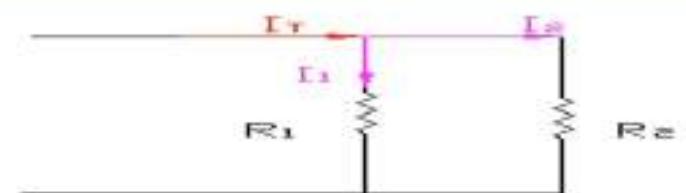
# محاضرة فديویه قصيرة لتوضیح قانون مقسم التيار

[https://youtu.be/g4GNb6TCZho?  
si=0vwPZWjSAuQMzK0I](https://youtu.be/g4GNb6TCZho?si=0vwPZWjSAuQMzK0I)

$$I_1 = V/R_1 = I_T \times \frac{R_1, R_2}{R_1}$$

$$\therefore I_1 = \frac{R_2}{R_1 + R_2} \cdot I_T$$

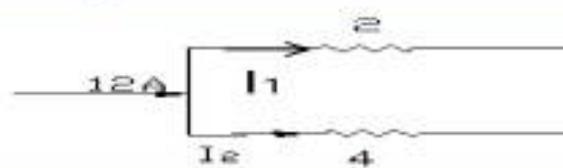
$$\text{Also: } I_2 = \frac{R_1}{R_1 + R_2} \cdot I_T$$



**EX(1) :Find I<sub>1</sub>, I<sub>2</sub> For the cct. Shown ;**

Solution:  $I_1 = \frac{R_2}{R_1 + R_2} \times I_T = \frac{4}{2+4} \times 12 = 8A$

$$I_2 = \frac{2}{2+4} \times 12 = 4A$$



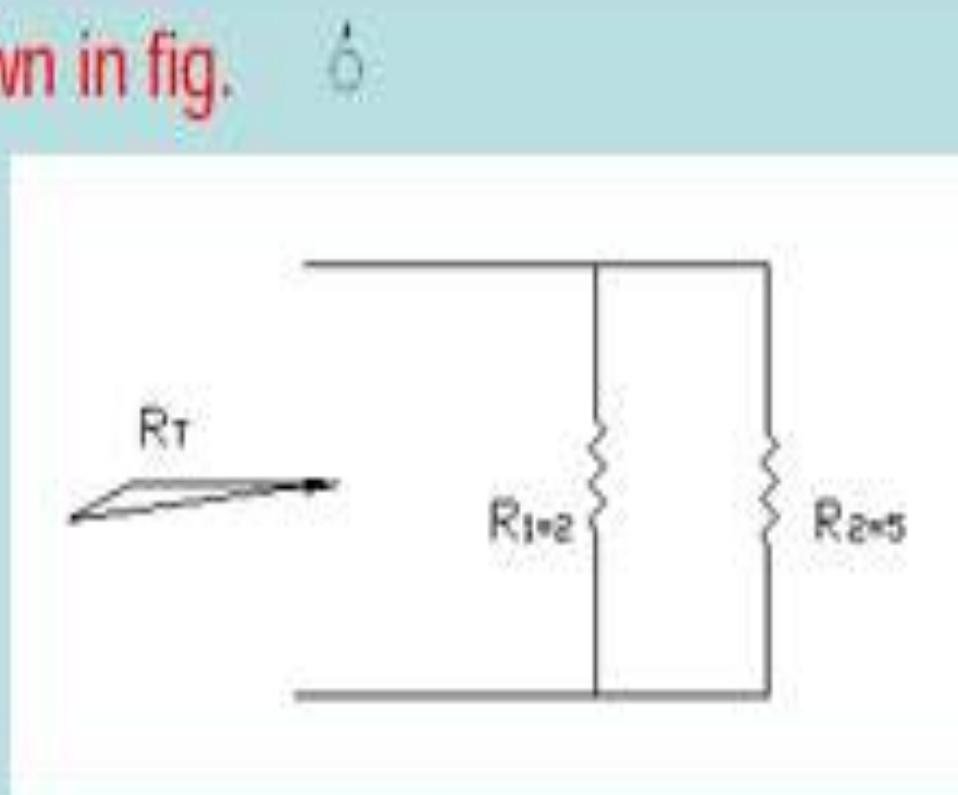
## :EXAMPLE2

For two resistance parallel connected as shown in fig.

$$1/R_T = 1/2 + 1/5 = 7/10 \therefore R_T = 10/7 = 1.4\Omega$$

OR:  $R_T = R_1 \cdot R_2 / (R_1 + R_2)$

$$= 2 \times 5 / (2 + 5) = 10/7 = 1.4\Omega$$



## الاختبار البعدى:

قم باعداد تقرير عن ربط التوالى وربط التوازى والفرق بينهما معزوا بالامثلة. الحل على مجاميع (كل خمس طلاب ضمن مجموعه)



ملاحظة : يسلم التقرير على رابط قناتنا على الكوكل كلاس روم

<https://classroom.google.com/c/NzcxOTQ3MjE5MTc5>



يرجى فتح ال QR code أدناه ملء الاستبيان

رأيك يهمنا



شكرا لحضوركم وتفاعلكم



الأسبوع الثالث

ربط دلتا-ستار

**DELTA-STA  
CONNECTION**

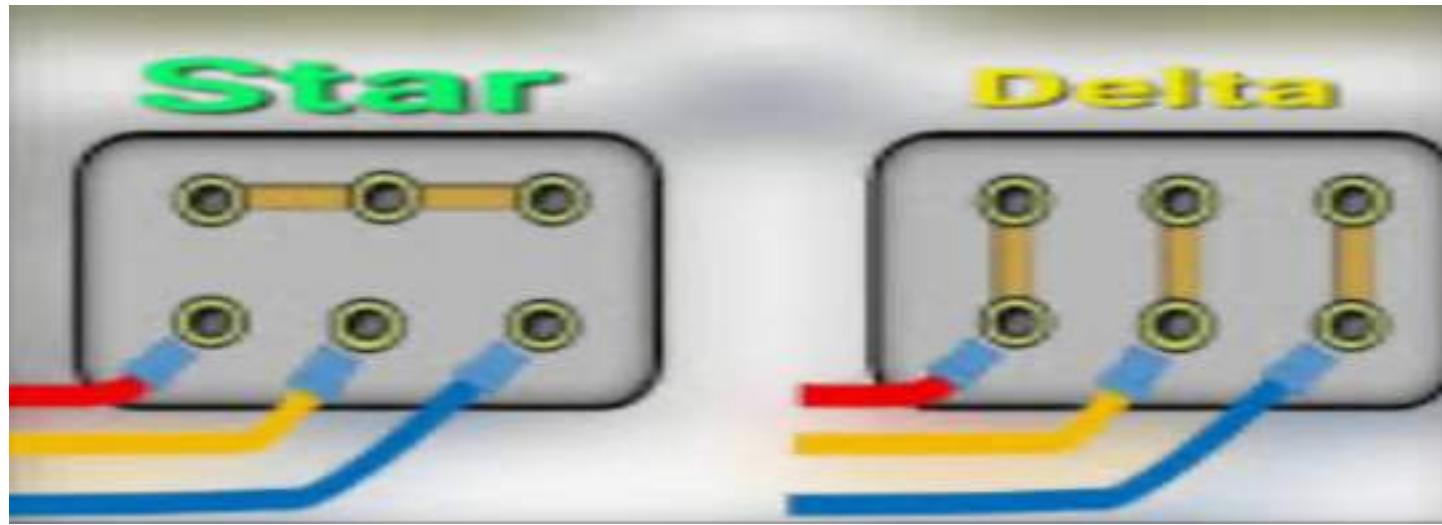


# الأهداف السلوكية

- سيكون الطالب قادرا على تبسيط الشبكات ذات الربط دلتا او ستار
- سيكون الطالب قادرا على تحويل الربط من دلتا الى ستار والعكس بالعكس



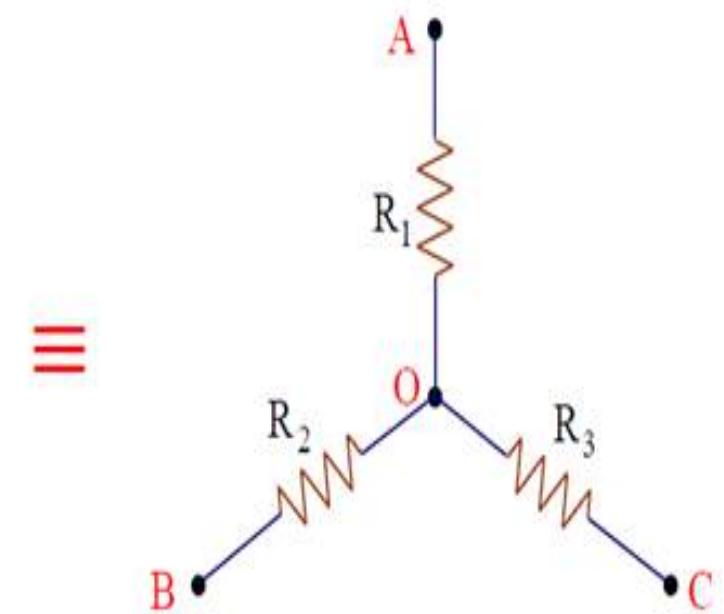
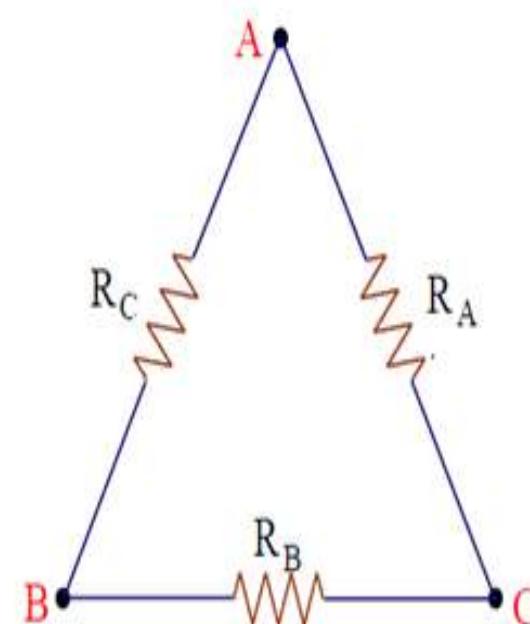
# الاختبار القبلي



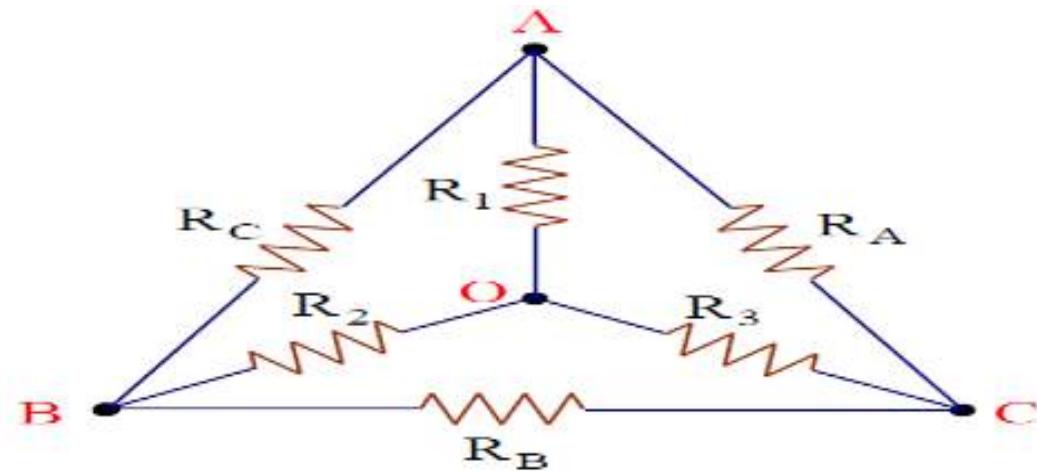
هل سألت نفسك يوماً عن نوع الربط المستخدم في قاطع الدورة المستخدم في المنازل؟ وهل توصلت إلى إجابة؟

# DELTA-STAR CONNECTION

In solving networks having considerable number of branches; one same times due to a large number of equations that have to be solved. This complicated network can be simplified by



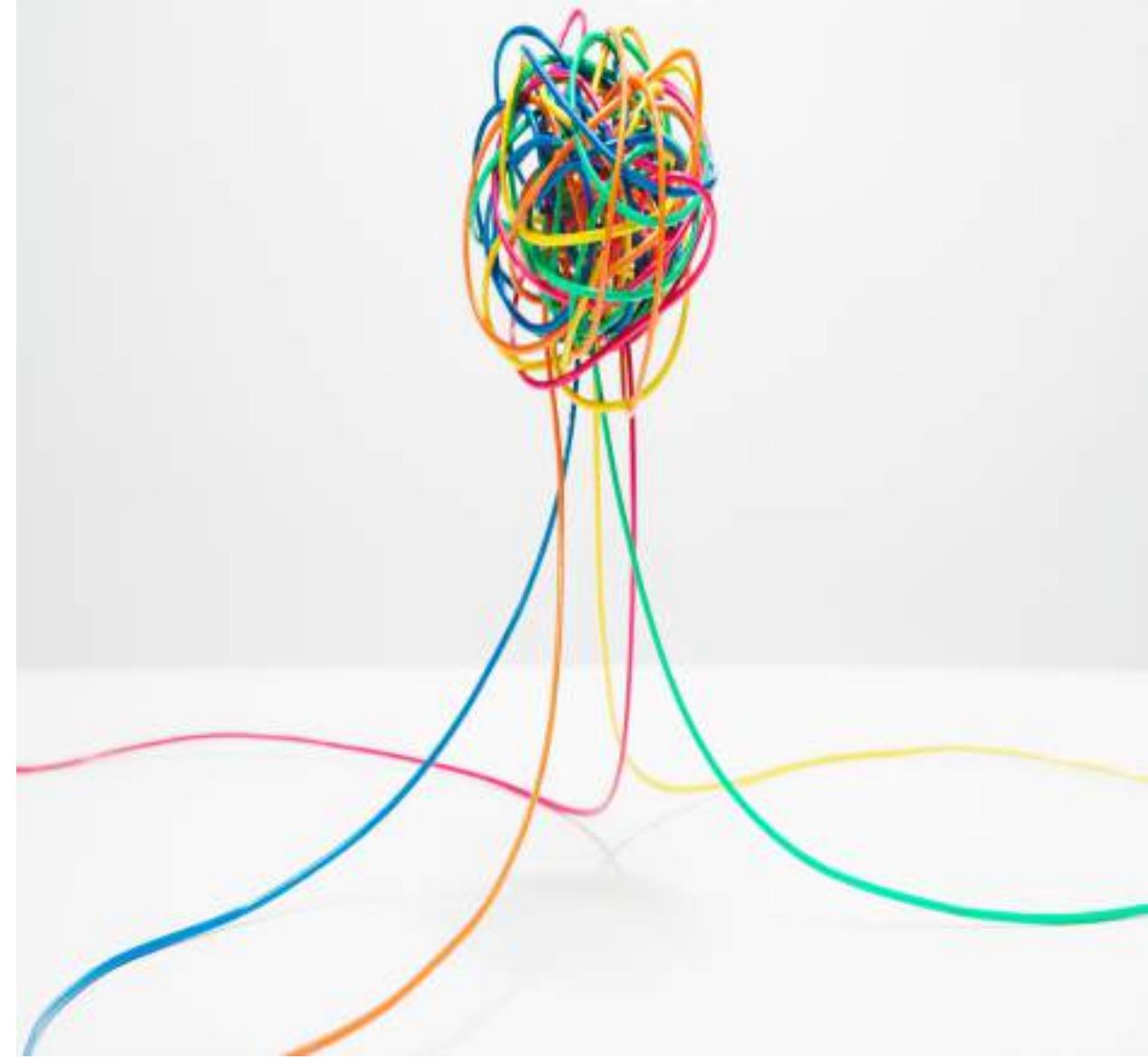
# DELTA TO STAR CONNECTION



$$R_1 = \frac{R_A R_C}{R_A + R_B + R_C}$$

$$R_2 = \frac{R_B R_C}{R_A + R_B + R_C}$$

$$R_3 = \frac{R_C R_A}{R_A + R_B + R_C}$$



## DELTA TO STAR CONVERSSION

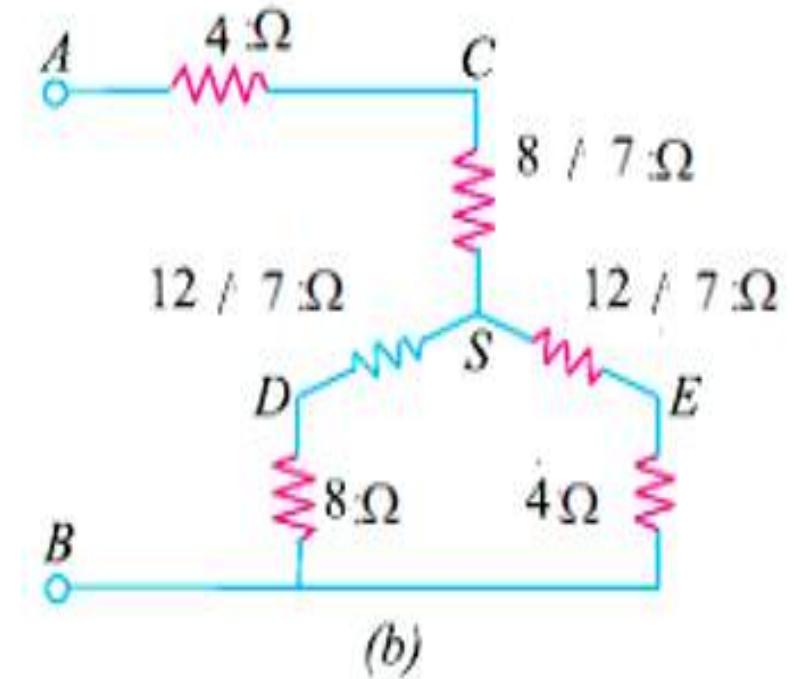
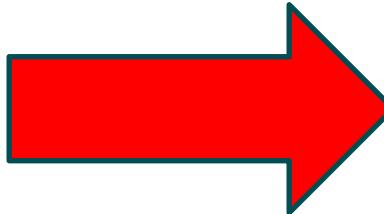
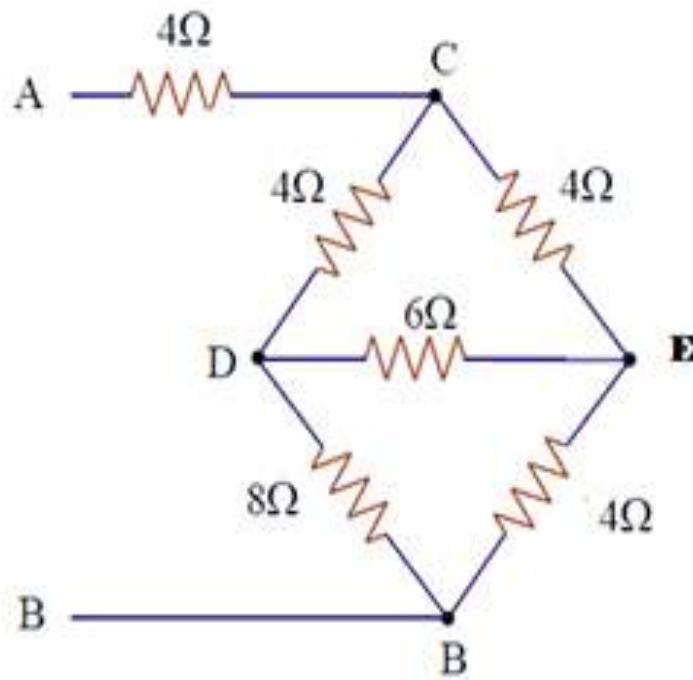
$$R_A = R_1 + R_3 + \frac{R_1 R_3}{R_2}$$

$$R_B = R_2 + R_3 + \frac{R_2 R_3}{R_1}$$

$$R_C = R_1 + R_2 + \frac{R_1 R_2}{R_3}$$

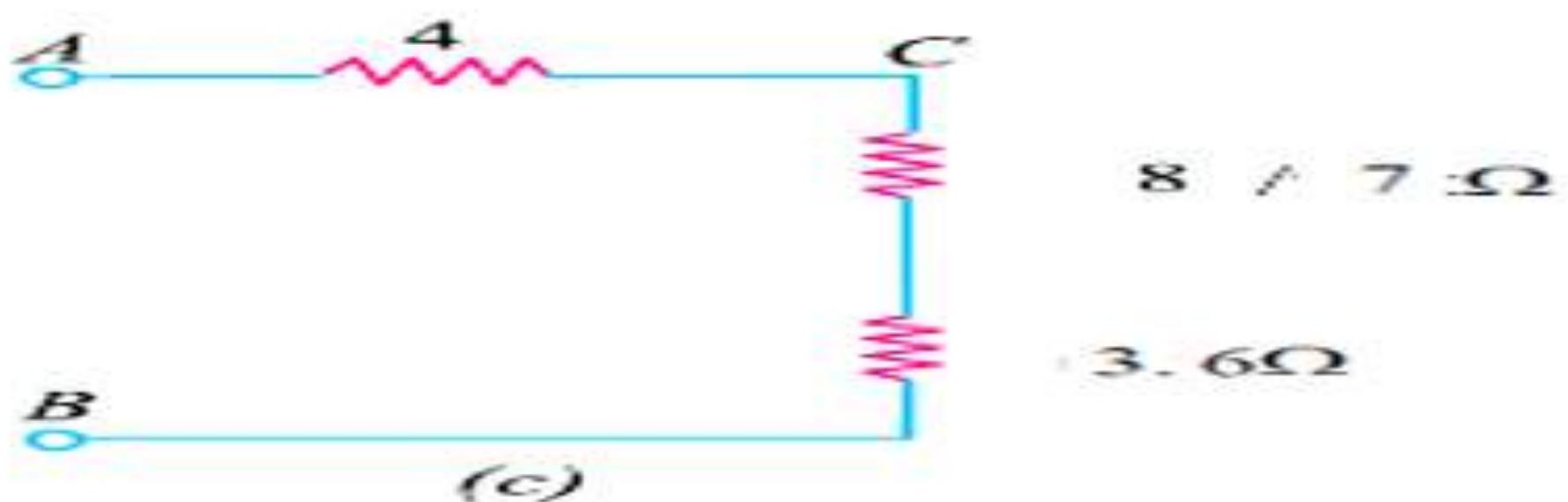
**EXAMPLE 1:** Find the total resistance between the points A and B of figure below

:SOLUTION

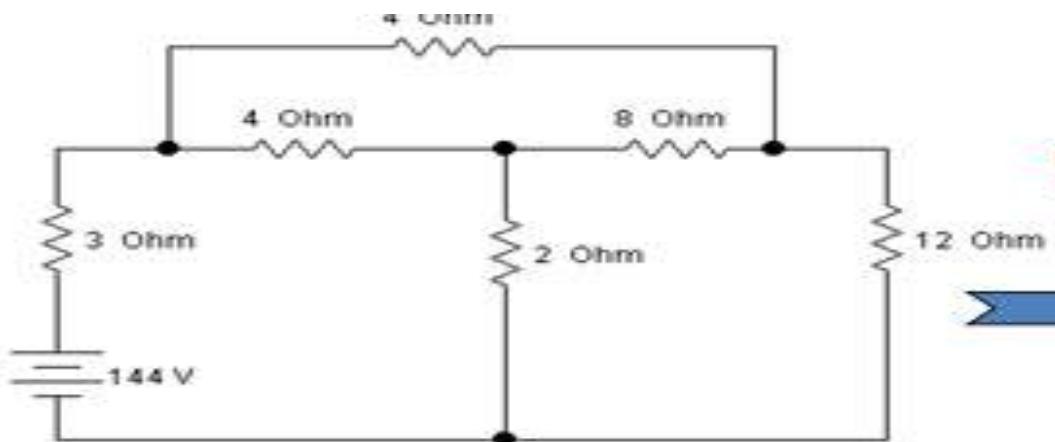


As seen from figure(c):

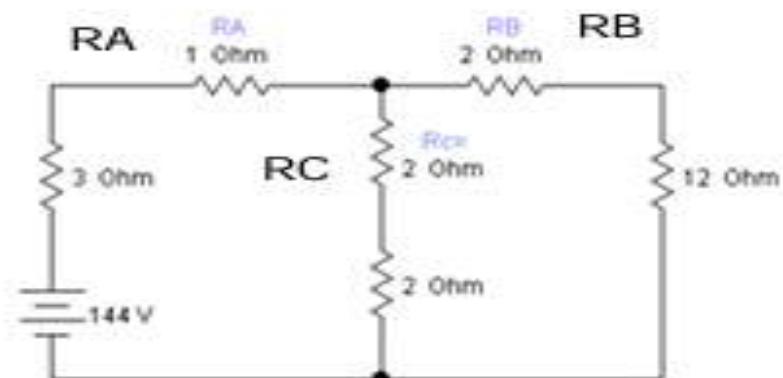
$$R_{AB} = 4 + (8 \parallel) + (3.6) = 8.6\Omega$$



**Example 2:** For the cct. shown below  
calculate ( $I_T$ )

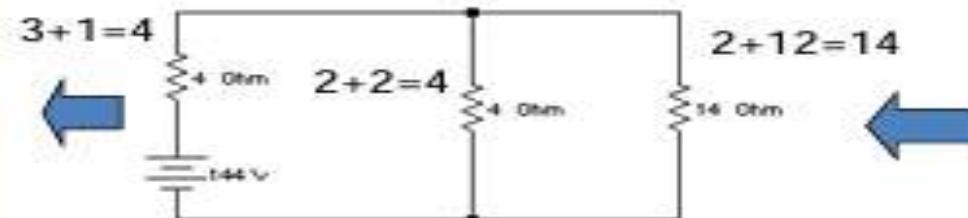


Solution :



$$R_T = \frac{4 \times 14}{4 + 14} + 4 = 7.111$$

$$I_T = 144 / 7.111 = 20.25 \text{ A}$$



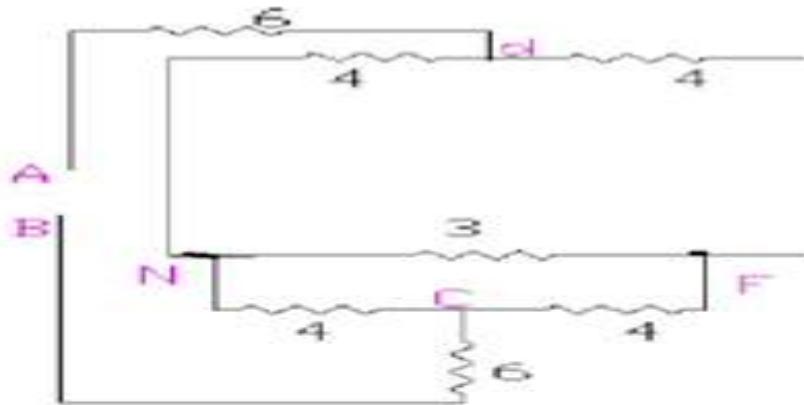
$$RA = \frac{4 \times 4}{16} = 1 \text{ ohm}$$

$$16$$

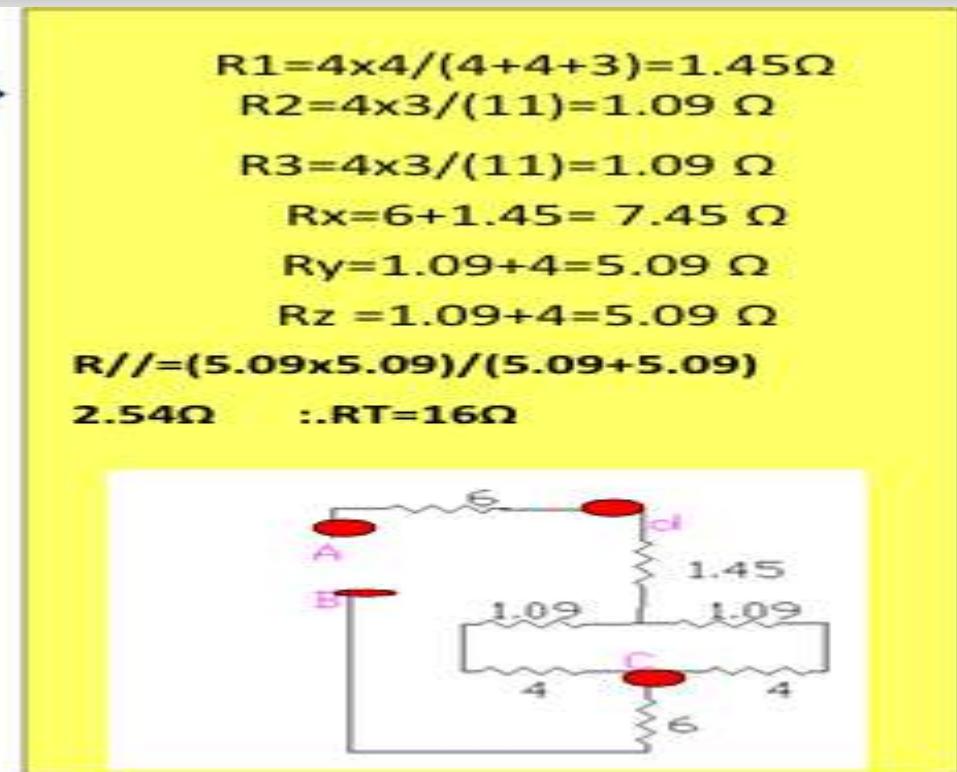
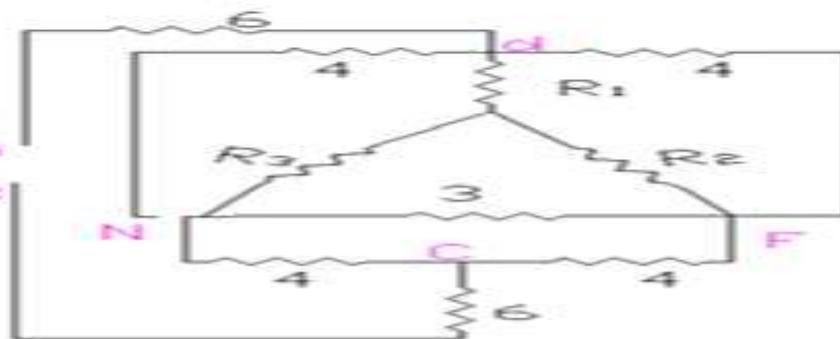
$$RB = \frac{4 \times 8}{16} = 2 \text{ ohm}$$

$$RC = \frac{4 \times 8}{16} = 2 \text{ ohm}$$

For the circuit shown below find  $R_t$  between A&B

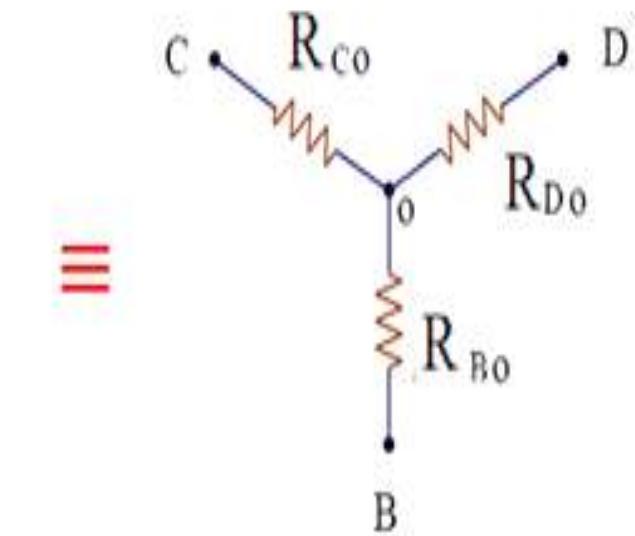
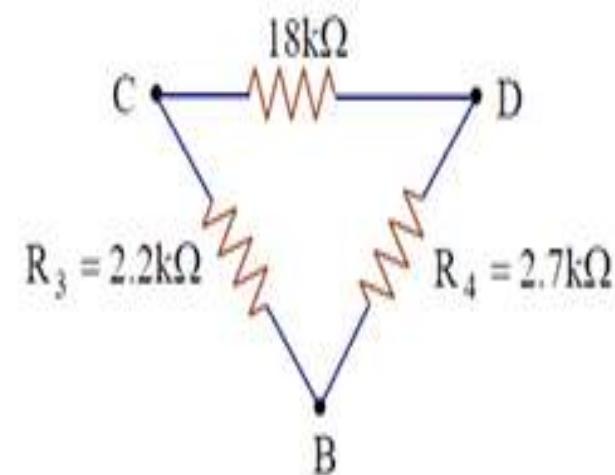
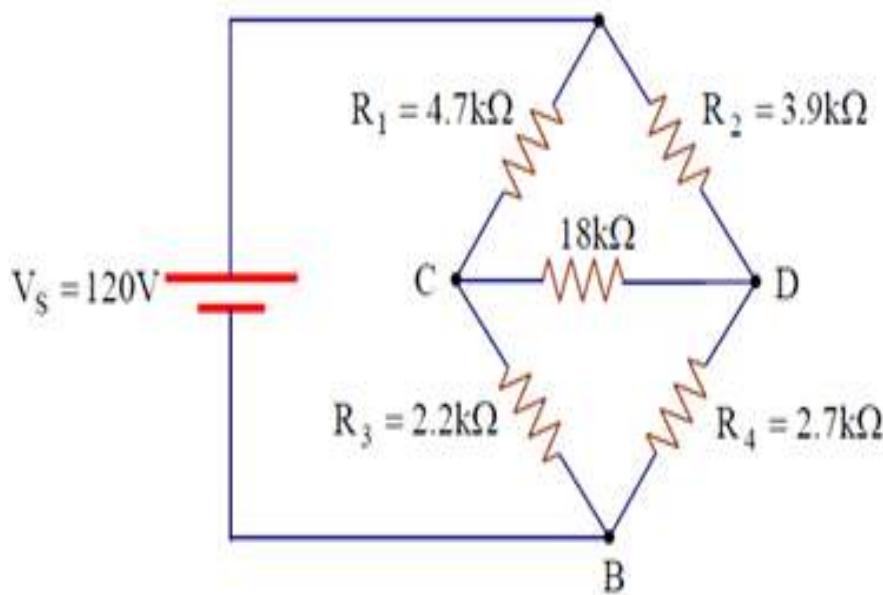


solution



## نشاط تفاعلي مع الطلبة

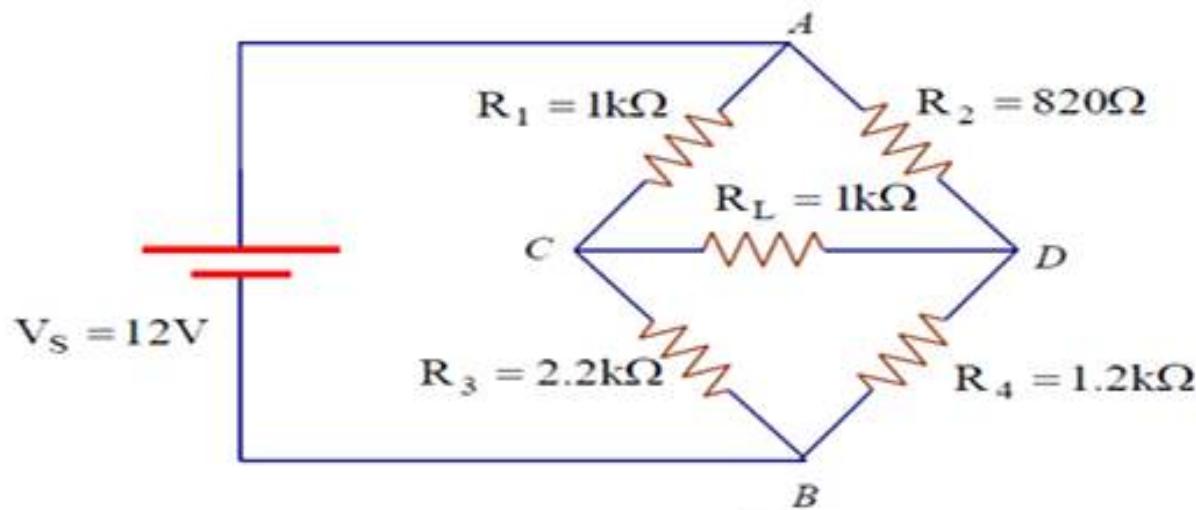
for the circuit shown in figure ; find the current passing through (  $R_L = 18 \text{ k}\Omega$  )



## الاختبار البعدى

**H.W :**For the circuit shown in figure find the current passing through (  $RL=1\text{k}\Omega$  ).

يرجى رفع الإجابة على الرابط أدناه ( سبقى الرابط مفتوحاً لمدة 24 ساعة )



[https://classroom.google.com/c/NzcxOTQ3MjE5MTc5/a/  
NzY1NzE1MTAxMDc4/details](https://classroom.google.com/c/NzcxOTQ3MjE5MTc5/a/NzY1NzE1MTAxMDc4/details)





لفهم المحاضرة اكثـر يمكنك الاستفادة من رابط  
اليوتيوب المبـين أدناه

<https://youtu.be/YJISmJp2wAw?si=V2-2GtWNuSBrz3q>

# ال أسبوع الرابع قوانين كيرشوف



## :RATIONAL

It is very important to study -

Kirchhoff's laws

.Also to study Maxwell's method -

# :CENTRAL IDEA

Definition Kirchhoff's current law in •

- . any electric point

Definition Kirchhoff's voltage law in •

- . any electric closed circuit

To learn Maxwell's loops by using •

- .Kirchhoff's voltage law

# الأهداف السلوكية

AT THE END of this lecture the student  
be able to identify the analyses net work  
by using Kirchhoff's laws



# اللختبار القبلي

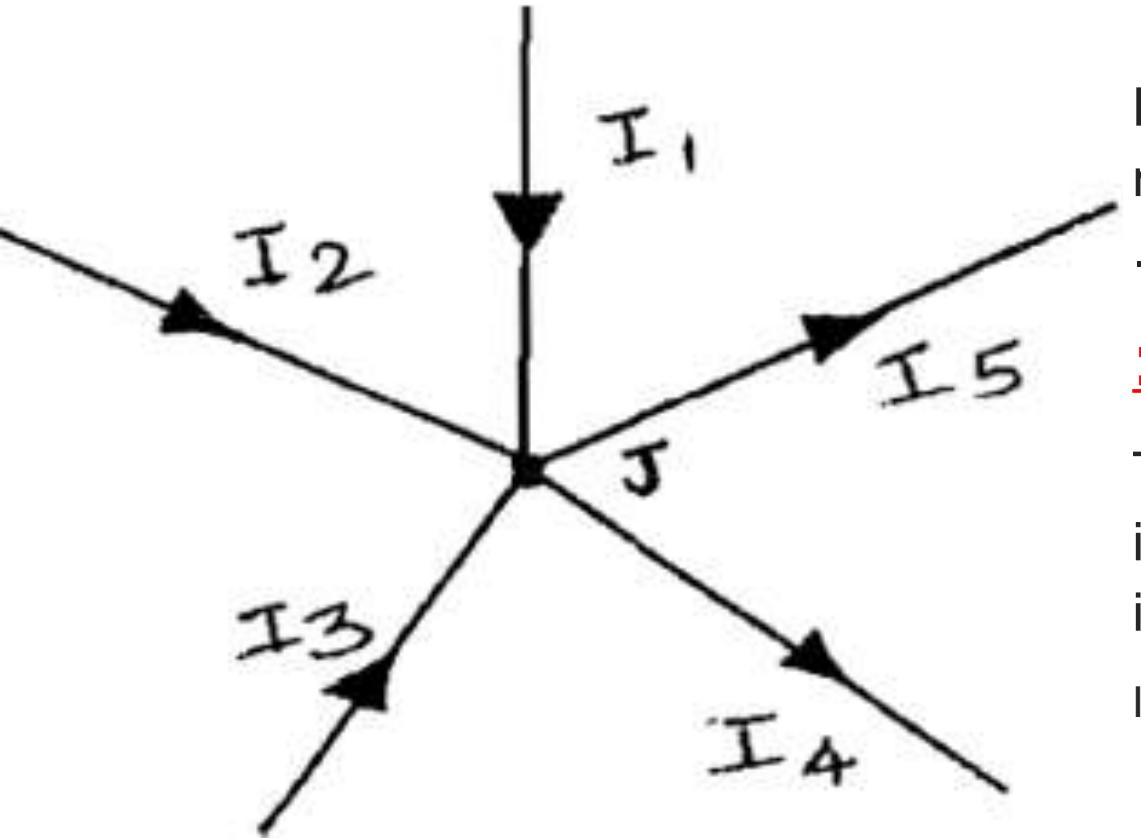


ماذا تعني لك المعادلة أدناه؟

**Kirchhoff's first law**

$$\sum I_{in} = \sum I_{out}$$

# :Kirchoff's law



Kirchoff's law is used to find out the current flow in the network circuits easily where Ohm's law is not applicable. It is applicable both for DC and AC circuits

## :Current law

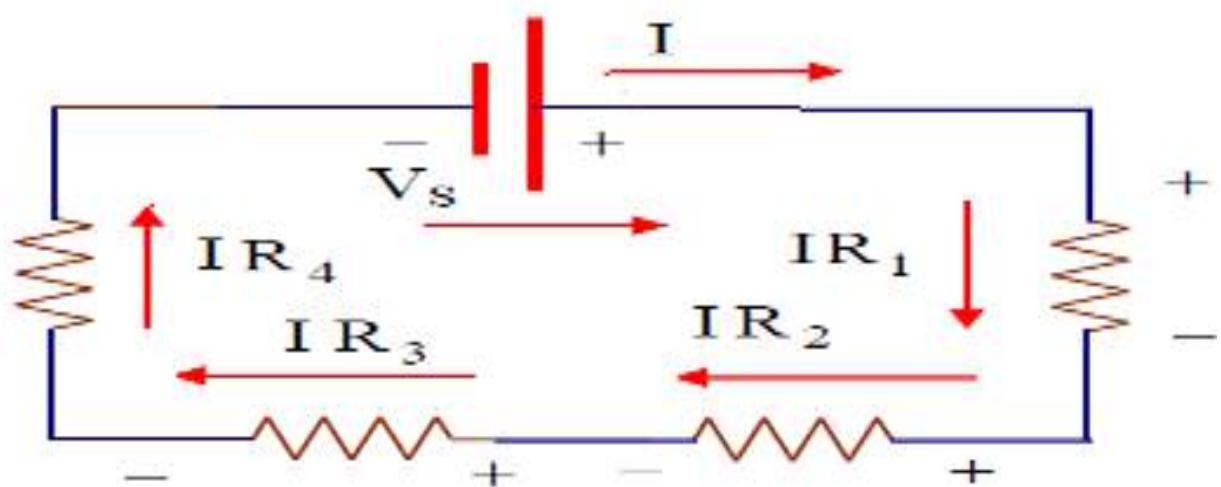
The sum of the current flowing towards a junction ( node ) is equal to the sum of the currents flowing away from it. This is called Kirchoff's current Law( K.C.L)

$$I_1 + I_2 + I_3 - I_4 - I_5 = 0 \quad (\text{this is known KCL equation})$$

# :Voltage Law

At any closed circuit the potential drop ( $IR$ ) at each resistance is equal to the total voltage given to the circuit. In a closed circuit, the sum of the potential drop is equal to the sum of the potential rises

$$VS=IR_1+IR_2+IR_3+IR_4$$



**Example:** In the circuit of figure using Kirchoff's laws, find the current in the various elements

:SOLUTION

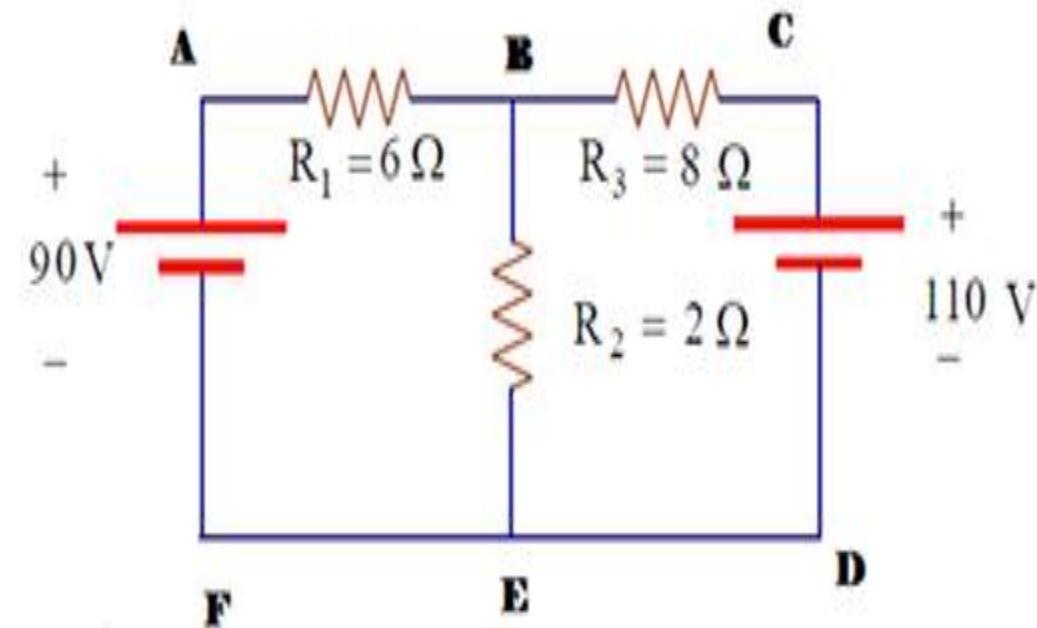
According to Kirchoff's first law mark the direction of current flow. According to second law, Write down the KVL equation in the closed circuits

ABEFA forms a closed circuit (LOOP 1)

$$6I_1 + 2(I_1 + I_2) = 90$$

$$6I_1 + 2I_1 + 2I_2 = 90$$

$$8I_1 + 2I_2 = 90 \text{ ---- (1)}$$



CBEDC forms another closed circuit( LOOP2)

$$8I_2 + 2(I_1 + I_2) = 110$$

$$8I_2 + 2I_1 + 2I_2 = 110$$

$$2I_1 + 10I_2 = 110 \text{ --- (2)}$$

To solve, equation(2) is multiplied by 4

$$8I_1 + 40I_2 = 440 \text{ ---(3)}$$

subtracted eq (1)from eq (3)

$$8I_1 + 2I_2 = 90 \text{ ---(1)}$$

$$8I_1 + 40I_2 = 440$$

$$38I_2 = -350 -$$

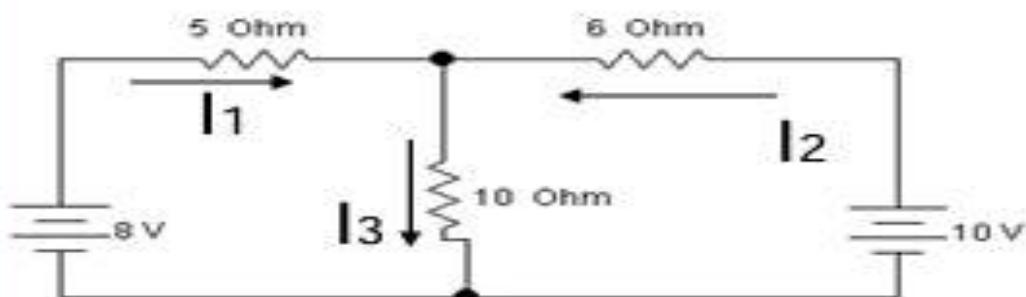
$$8I_2 = 350 \implies I_2 = 350 / 8 = 9.211A$$

Substitute the I<sub>2</sub> value in equation (1)  $I_1 + 2(9.211) = 90$

$$I_1 + 18.422 = 90$$

$$I_1 = 90 - 18.42$$

For the circuit shown find the current through each resistance



$$\begin{aligned}
 I_1 + I_2 &= I_3 \dots (1) & 8 &= 5I_1 + 10I_3 \dots (2) \\
 10 &= 10I_3 + 6I_2 \dots (3) & \text{then } 8 &= 5I_1 + 10(I_1 + I_2) \\
 8 &= 15I_1 + 10I_2 \dots (4) & \text{and at eq.(3)} \\
 6I_2 + 10(I_1 + I_2) &= 10 & 6I_2 + 10I_1 + 10I_2 &= 10
 \end{aligned}$$

Then  $16I_2 + 10I_1 = 10 \dots (.. /2)$  ,  $5I_1 + 8I_2 = 5$  ,(x3)  $15I_1 + 24I_2 = 15$

الطرح  $-15I_1 - 10I_2 = -8$

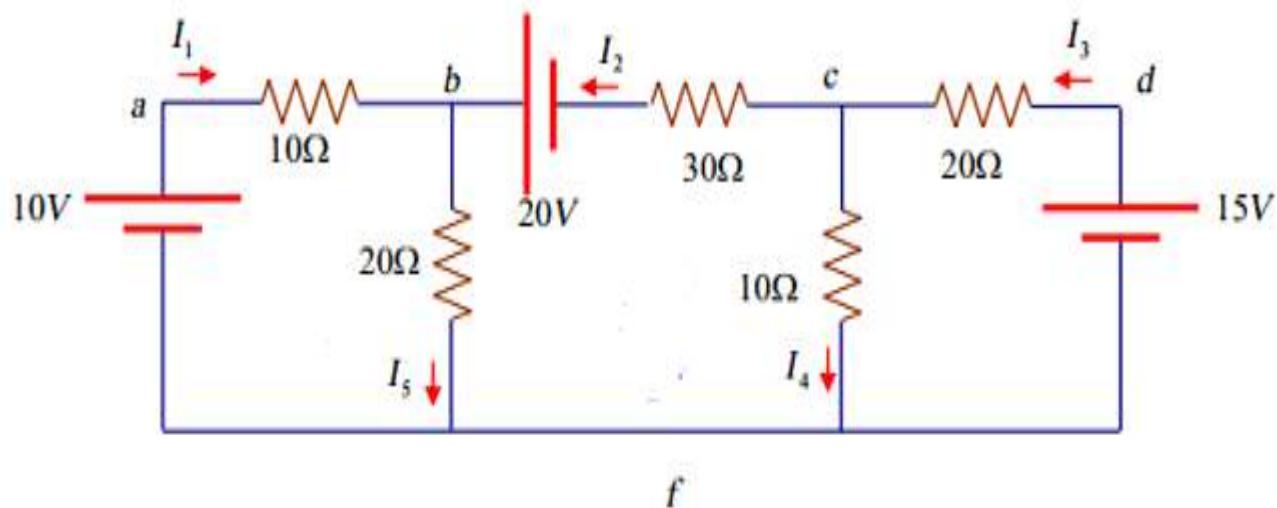
$14I_2 = 7$  ,  $I_2 = 0.5A$  and in eq ..(4)  $15I_1 + 5 = 8$  ,  $I_1 = 0.2A$  ,  $I_3 = 0.2 + 0.5 = 0.7A$

# نشاط جماعي

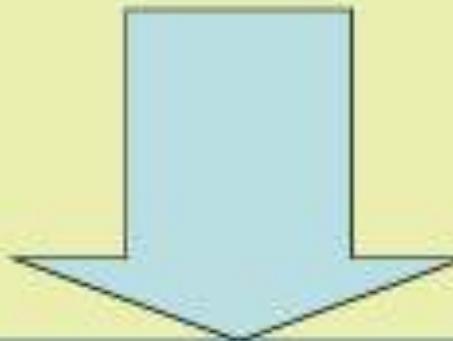
3

نشاط تفاعلي داخل القاعة مدة النشاط  
(3 دقائق فقط)

by using Kirchoff's laws find the currents  
. in each resistors for the circuit shown



# Currents method



مدارات ماكسويل

## طريقة التيارات

**Aim of lecture :** To let the student be able to identify the analyses net work by using Maxwell's method.

# تيارات ماكسويل الدوارة

:Solution

:At loop(1)

$$I_1 - 3I_2 = 20 - 5 \quad 8I_1 - 3I_2 = 15 \dots\dots (1)(5+3)$$

:At loop (2)

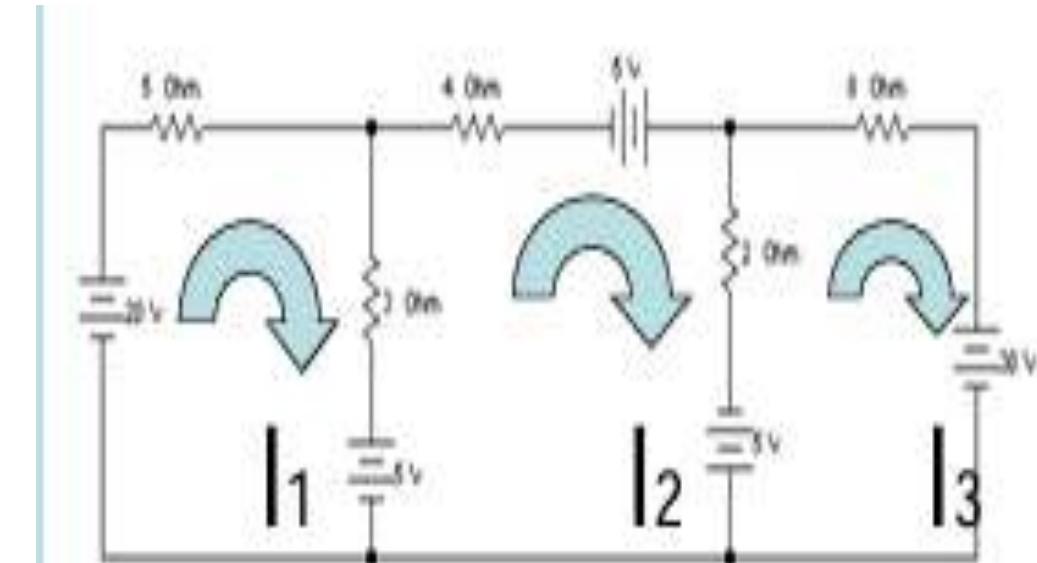
$$I_2 - 3I_1 - 2I_3 = 5 + 5 + 5 - 3I_1 + 9I_2 - 2I_3 = 15 \dots\dots (2)(3+4+2)$$

:At loop (3)

$$I_3 - 2I_2 = -30 - 5 - 2I_2 + 10I_3 = -35 \dots\dots (3)(2+8)$$

Then we find  $I_1, I_2, I_3$

**$I_1 = 54.64A$  ,  $I_2 = 145.3A$  ,  $I_3 = 24.64A$**



**(B) : For the circuit shown using Maxwell's loop to find ( $I_1, I_2, I_3$ )**

**Solution**

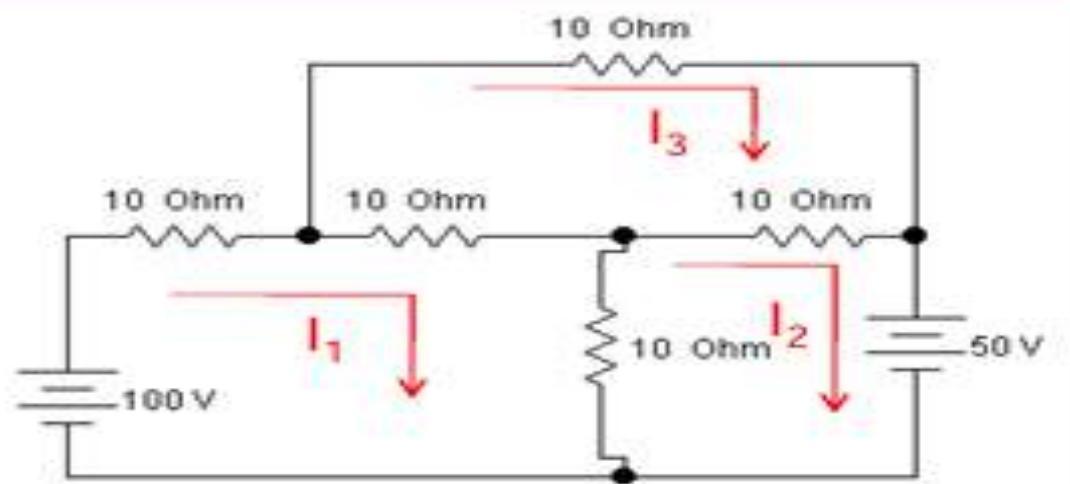
$$30I_1 - 10I_2 - 10I_3 = 100 \dots (1)$$

$$20I_2 - 10I_1 - 10I_3 = -50 \dots (2)$$

$$30I_3 - 10I_1 - 10I_2 = 0 \dots (3)$$

$$\therefore 10I_3 - I_1 - I_2 = 0 \quad , \quad (\text{eq.2-eq.1});$$
$$40I_1 - 30I_2 = 150$$

$$\therefore 4I_1 - 3I_2 = 15 \dots (4) \quad \text{eq.(1)x3 and the result + with eq.(3);}$$

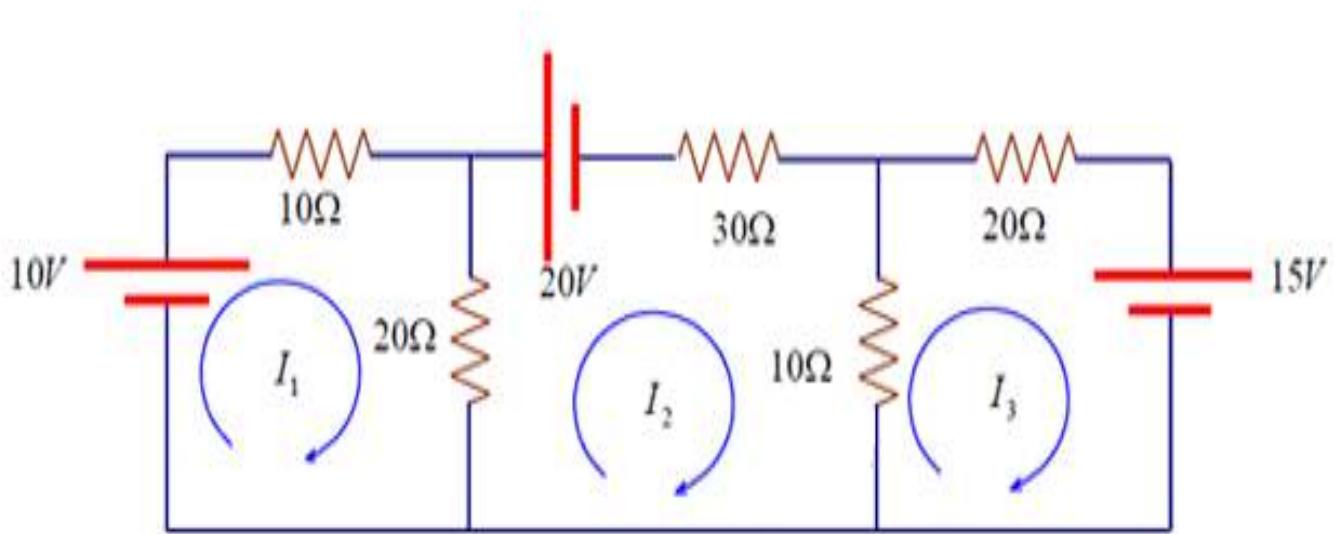


# الاختبار البعدى

**H.W.** find the current in each resistor by using MAXWELL`s current loop.



Google Classroom



ملاحظة : يرفع الحل على منصة الكلاسرووم على الرابط أدناه خلال 24 ساعة

[https://classroom.google.com/c/NzcxOTQ3MjE5MTc5/a/  
NzgzOTI0NTUyMDk5/details](https://classroom.google.com/c/NzcxOTQ3MjE5MTc5/a/NzgzOTI0NTUyMDk5/details)



للاستفادة اكثـر يمكـنك الاطـلاع علـى رابـط الـيوتيوب المـوجود  
ادنـاه:

[https://youtu.be/Swem4jghWZM?  
si=Eo0pJHPbedpVLU17](https://youtu.be/Swem4jghWZM?si=Eo0pJHPbedpVLU17)

رابط توضيحي لتحليل الدوائر الكهربائية باستخدام  
تيارات ماكسويل الدوارة

المحاضرة الخامسة

نظريّة ثيفرن

Thevenin theorem



A collection of colorful paper stars (red, green, blue, yellow, grey) arranged in a grid pattern on a white surface. The stars are scattered across the frame, with some overlapping each other.

## :Rational

It is very important to study  
.Thevinins theorem  
Also to study how apply the three  
. step to the save theorem



# :Centeral idea

- . Definition Thevinins theorem •  
How we find the current at each•  
resistance in the net work by the  
.above theorem



## الأهداف السلوكية

في نهاية هذه المحاضرة سيكون الطالب قادرا على

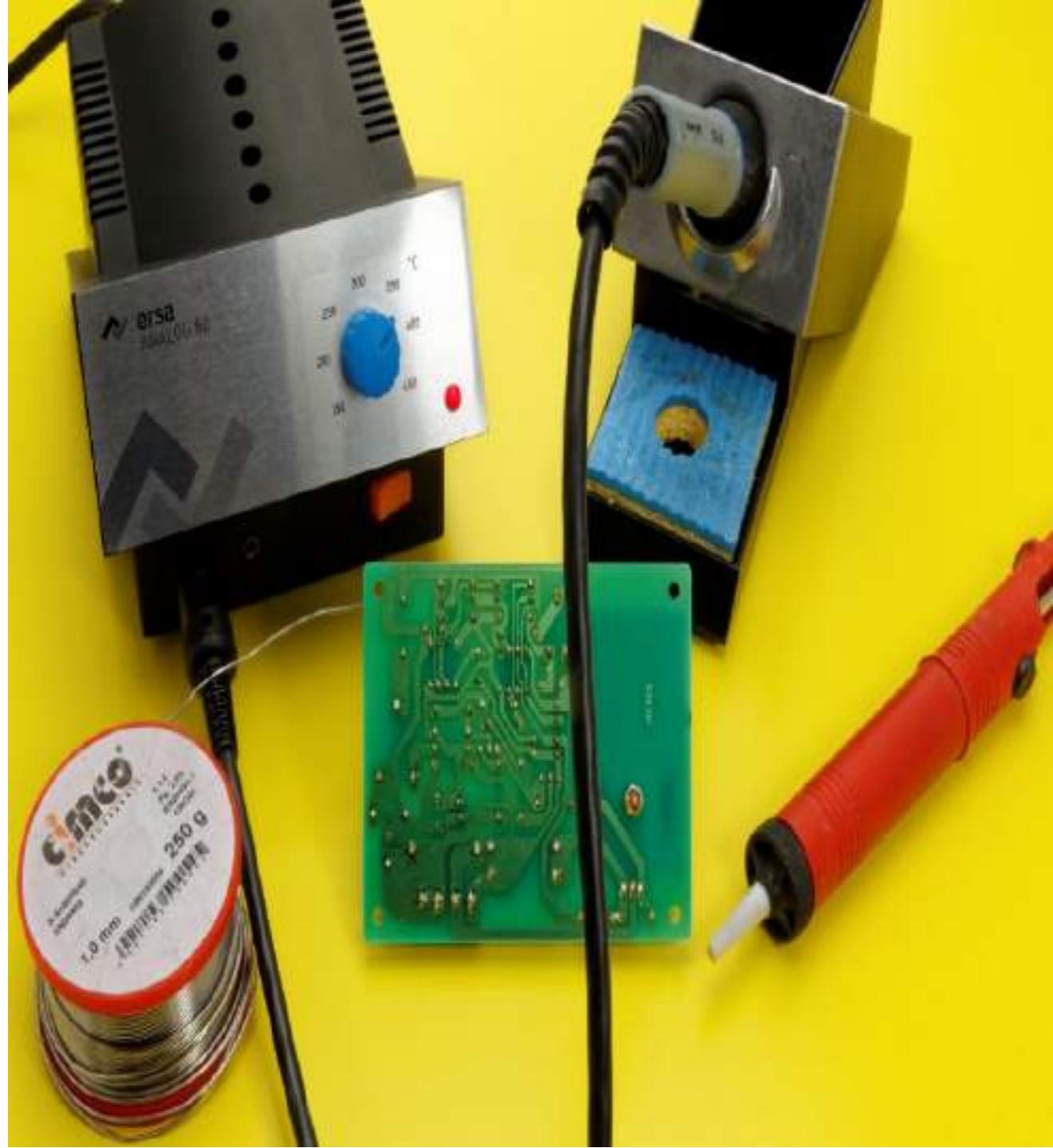
تحليل الدوائر الخطية باستخدام نظرية ثفنن

معرفه المبادئ الأساسية لنظرية ثفنن

## الاختبار القبلي:

هل يمكن ان نختزل دائرة كهربائية تحتوي على العديد من المصادر والمقاومات الى دائرة تحتوي على مصدر فولتية واحد على التوالي مع مقاومة ؟  
كيف ؟

(الإجابة مباشرة داخل القاعه )



## Thevenin's theorem

Statement: A linear network consisting of a number of voltage sources and resistances can be replaced by an equivalent network having a single voltage source called Thevenin's voltage ( $V_{Th}$ ) and a single resistance called Thevenin's resistance (  $R_{Th}$ )

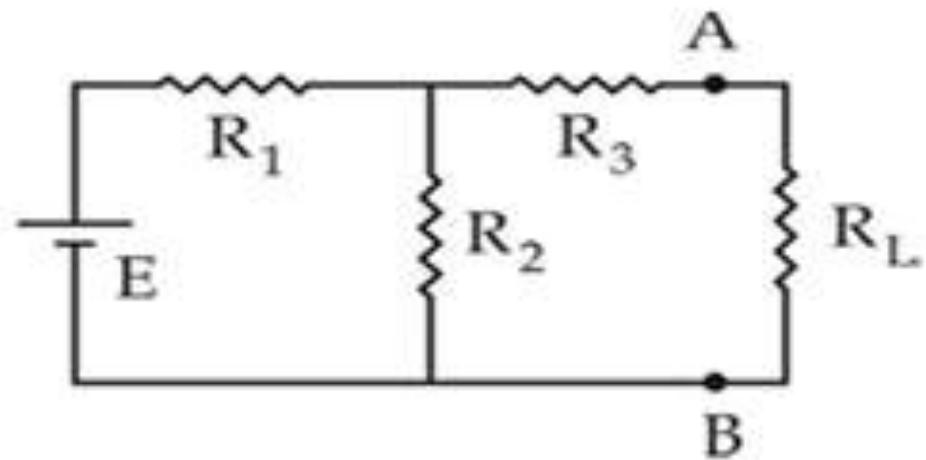
## EXPLANATION

Consider a network or a circuit as shown figure (a)  
Let  $E$  be the emf of the cell having its internal resistance  $r = 0 \dots$   
RLload resistance The load resistance ( $R_L$ ) is removed figure  
(b).the current ( $I$ ) in the circuit is

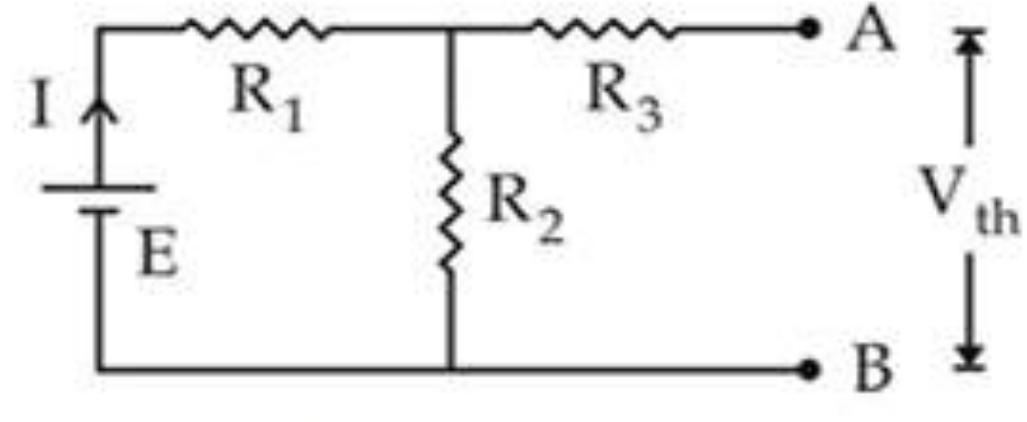
$$I = E / (R_1 + R_2)$$

The voltage across AB = Thevenin's voltage  
( $V_{Th}$ )  $V_{Th} = V_{AB} = I \times R_2 = E \times R_2 / R_1 + R_2$

$$V_{Th} = V_{AB} = I \times R_2 = E \times R_2 / R_1 + R_2$$

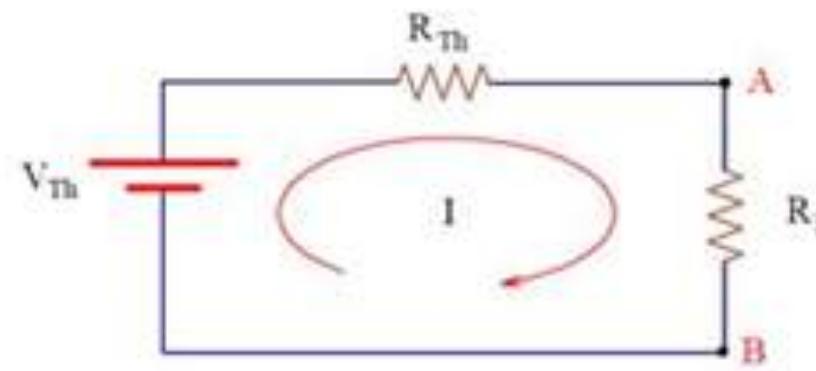
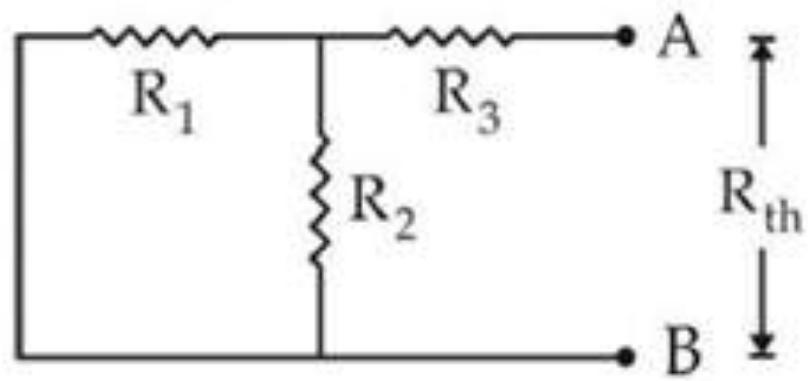


a



b

:To find R<sub>Th</sub>



$$R_{Th} = R_3 + \frac{R_1 \times R_2}{R_1 + R_2}$$

$$I = \frac{V_{Th}}{R_{Th} + R_L}$$

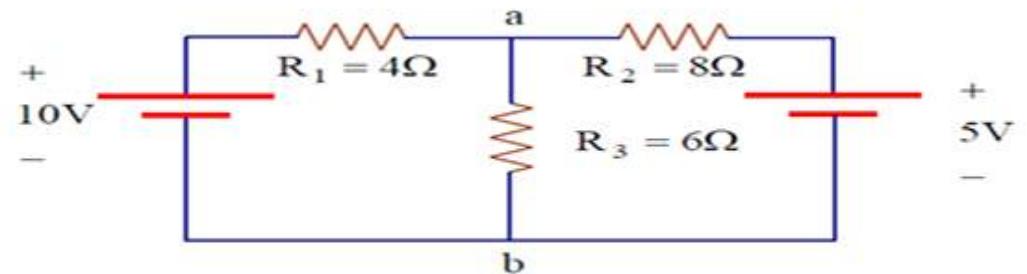
**Example:** For the circuit in figure find the current in ( $R=6\Omega$ ) by using Thevenin's theorem

**:SOLUTION**

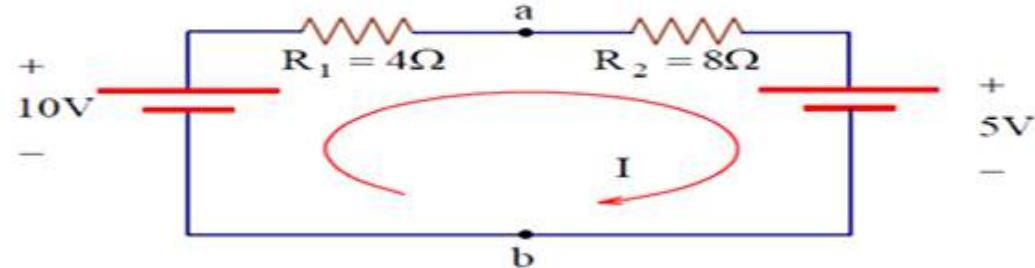
$$10 - 5 = I(4 + 8) \Rightarrow I = 5/12 \text{ A}$$

$$V_{Th} = 10 - 4 \times (5/12) = 8.33V$$

$$\text{or : } V_{Th} = 5 + 8 \times (5/12)$$



To find the ( $V_{Th}$ )



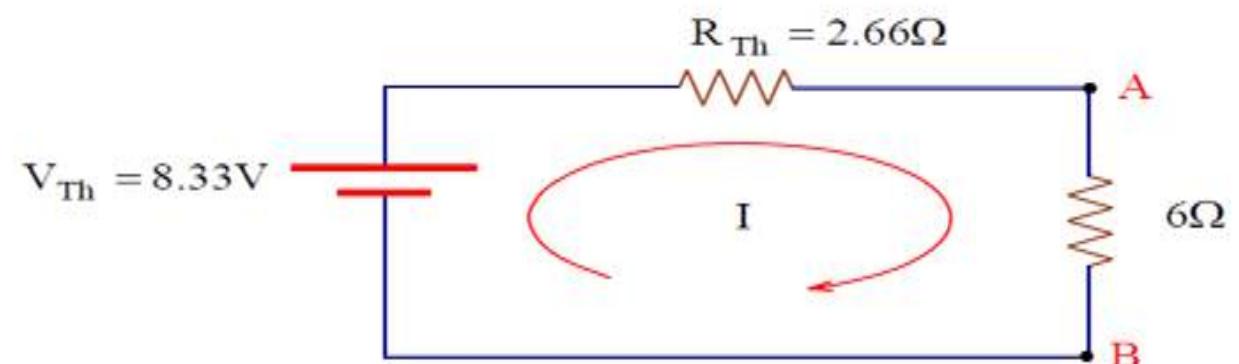
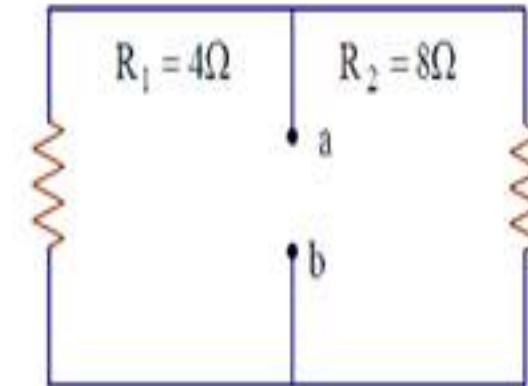
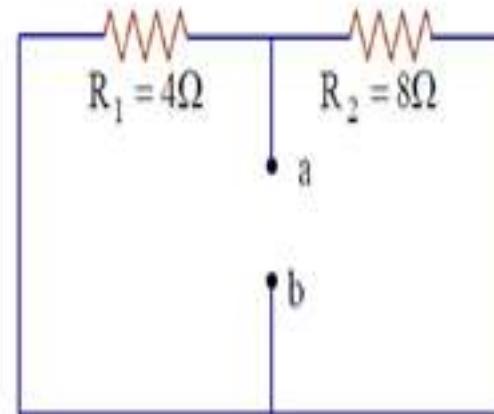
Now to find **R<sub>th</sub>**

$$R_{th} = (4 \times 8) / (4 + 8)$$

$$R_{th} = 2.66\Omega$$

$$I(6\Omega) = 8.33 / (2.66 + 6)$$

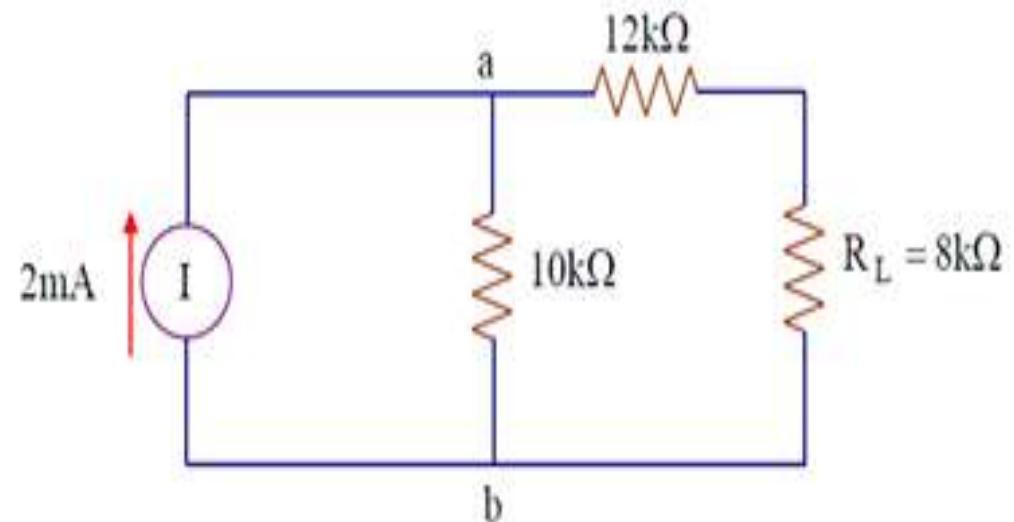
$$I = 0.96 \text{ A}$$



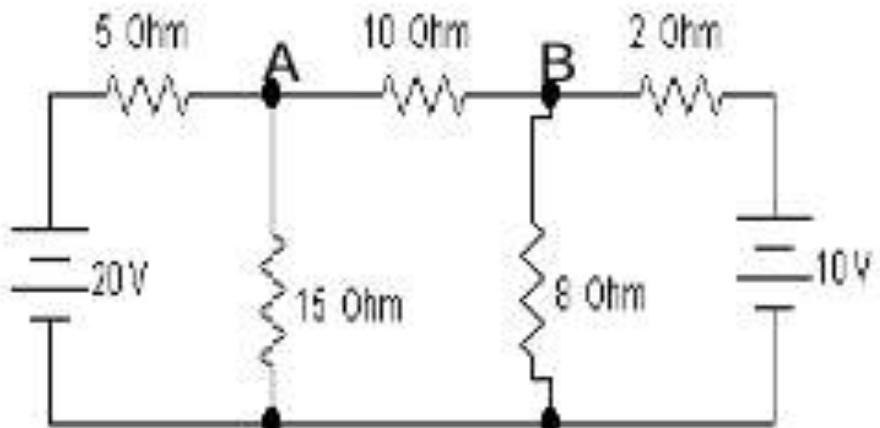
# نشاط تفاعلي (just 2S)



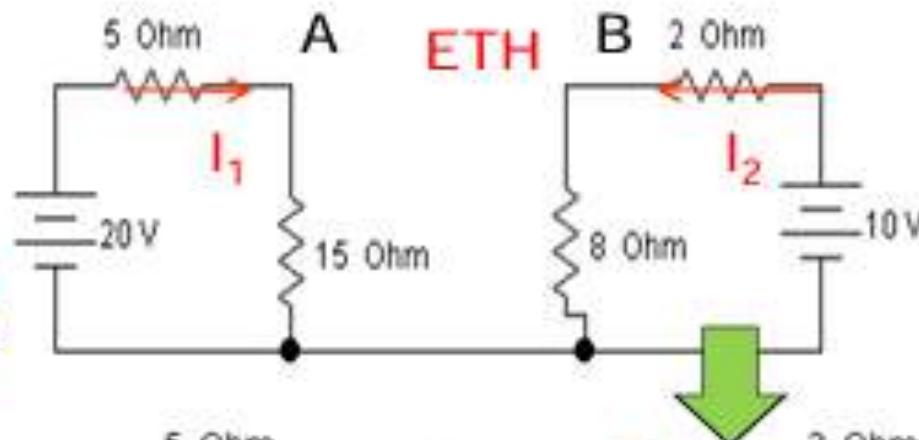
For the circuit in figure find the current in ( $R=8\Omega$ ) by using Thevenin's theorem



## Home work : Using Thevenins' theorem To Find ( I<sub>L</sub> ) .



Solution



$$I_1 = 20 / (5 + 15) = 1 \text{ A} \quad V_{\text{at } 15\Omega} = 1 \times 15 = 15 \text{ V}$$

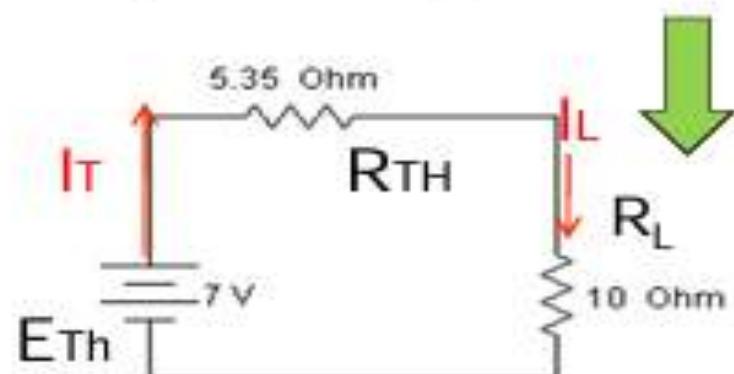
$$I_2 = 10 / (2 + 10) = 1 \text{ A} \quad \therefore V_{\text{at } 8\Omega} = 1 \times 8 = 8 \text{ V}$$

$$\therefore E_{\text{th}} = 15 - 8 = 7 \text{ V}$$

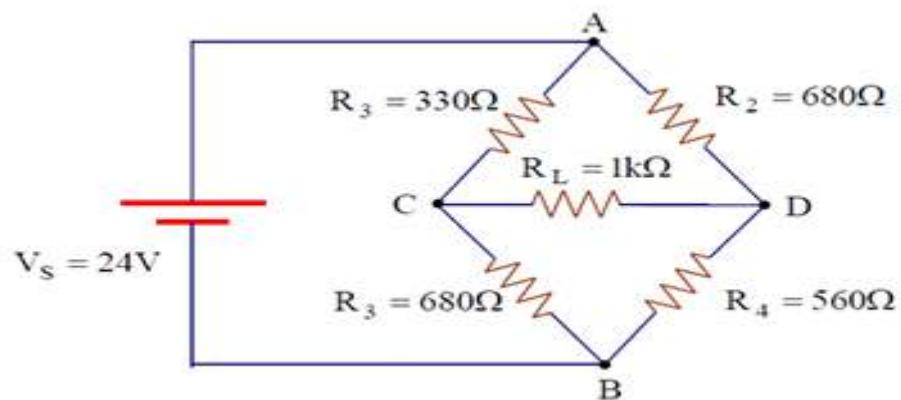
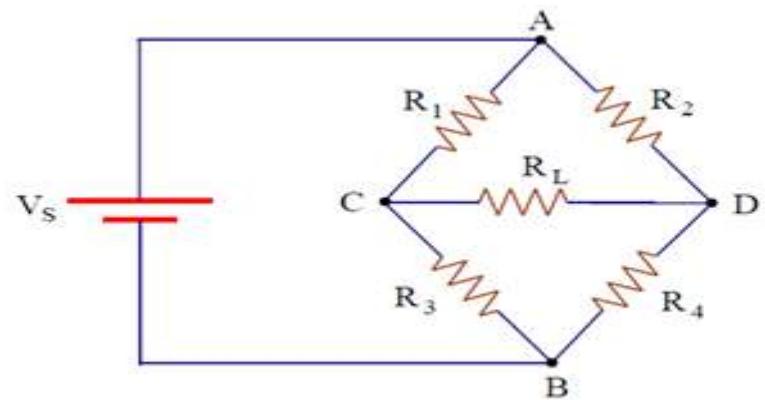


$$R_{\text{Th}} = (5 \times 15) / (5 + 15) + (8 \times 2) / (8 + 2) = 5.35 \Omega$$

$$\therefore I_L = I_T = 7 / (5.35 + 10) = 0.456 \text{ A}$$



## الاختبار البعدى



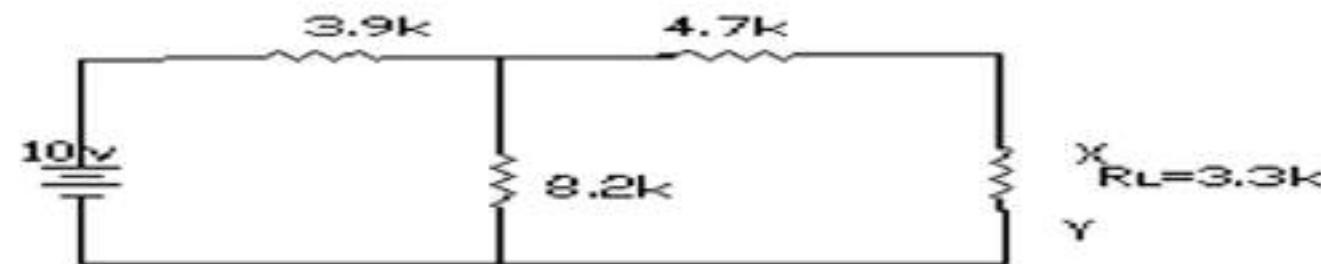
<https://classroom.google.com/c/NzcxOTQ3MjE5MTc5/a/NzY1NzU4NzU1NDEx/details>

ملاحظة : يرفع الحل على الرابط اعلاه ويكون التصحيح ذاتيا باستخدام معايير RUBRICS

يرجى الاطلاع على الفيديو أدناه (شرح مختصر لنظرية ثفنن)

<https://youtu.be/StMuQgBtA2M>

**Ex.(2) : For the cct shown below find  
(VL) by using Thevinins theorem**



المحاضرة السادسة  
نظريّة نورتن

**NORTON THEOREM**

# :Rational

It is very important to study -

.Norton's theorem

Also to study how apply the -

three step to the save

. theorem



# :Central idea

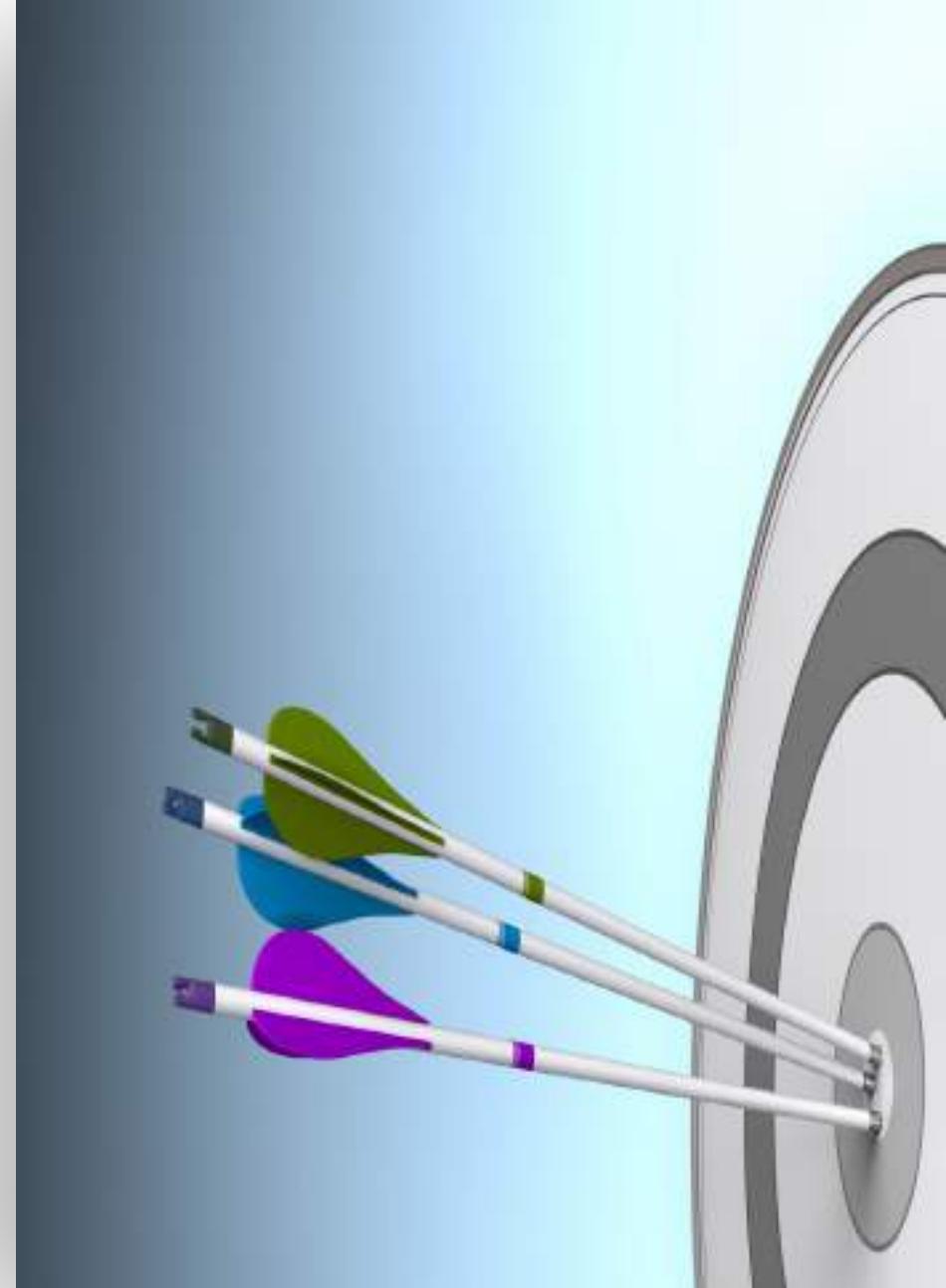


- . Definition Norton's theorem •
- How we find the current at each•
- resistance in the net work by the
- . above theorem

## **objectives**

after ending of this lecture the student will be able to:

- understanding principles of Norton theorem
- analysing leaner circuit by using Norton theorem



## Pretest

## الاختبار القبلي

Define : short circuit , Open circuit

solution

**Short circuit :** هي دائرة القصر التي يمر فيها جميع التيارات لنفس الدائرة الكهربائية لعدم وجود مقاومة فيها أي أن قيمة مقاومتها تكون صفراء .

**Open circuit :** هي الدائرة المفتوحة التي تكون مقاومتها مالا نهاية وقيمة التيار المار فيها يكون صفراء .

# :Norton's Theorem

This theorem is an alternative to the

.Thevenin's theorem

.In fact it is the dual of Thevenin's theorem

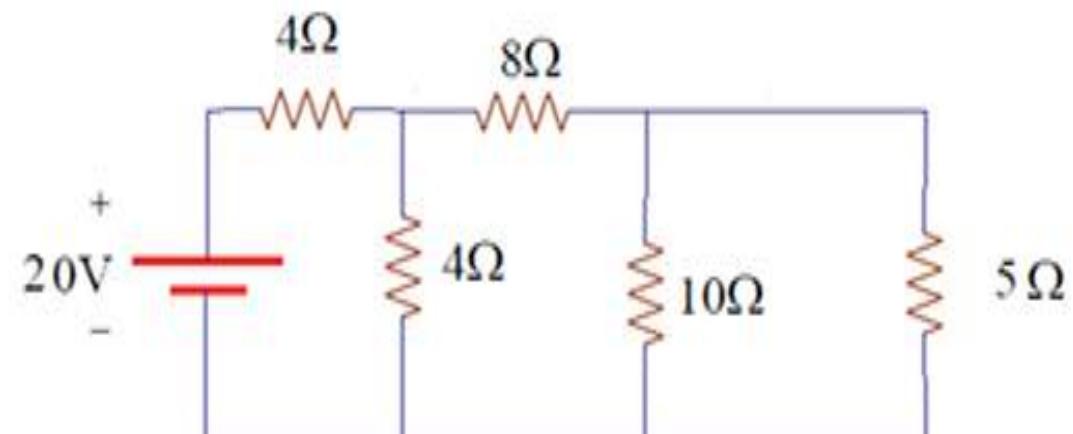
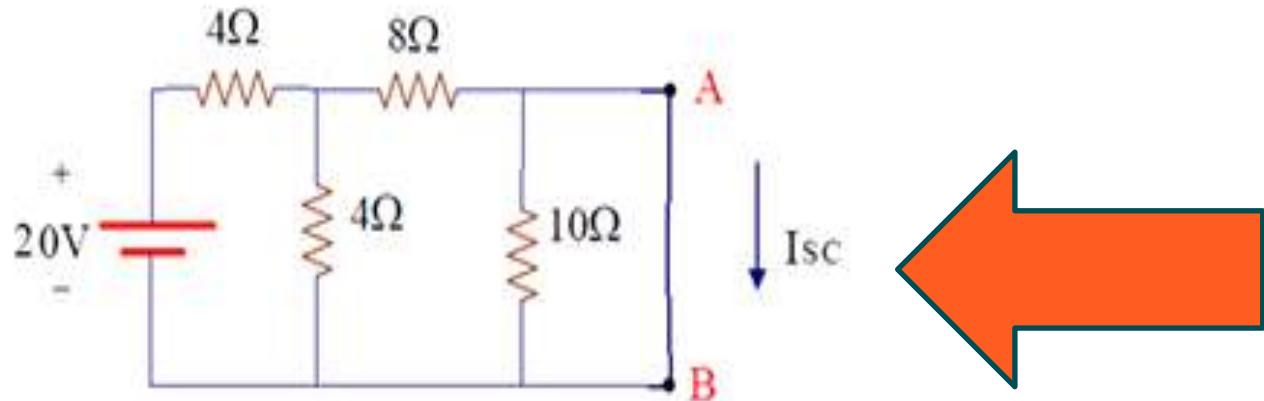
Whereas Thevenin's theorem reduces a two-terminal active network of linear resistances and generators to an equivalent constant-voltage source and series resistance. Norton's theorem replaces the network by an equivalent constant-current and a parallel resistance

## EXAMPLE:

Apply Norton's theorem to calculate current flowing through  $.5\Omega$  resistor of figure (a) below

:SOLUTION

Remove  $5\Omega$  resistor and put a short circuit across terminals A and B as shown in figure (b)



## نكمـلة الـحل :

.Let us find **ISC**

.I combination of(  $4\Omega$  and  $8\Omega$  ) in series with a  $4\Omega$  resistanc

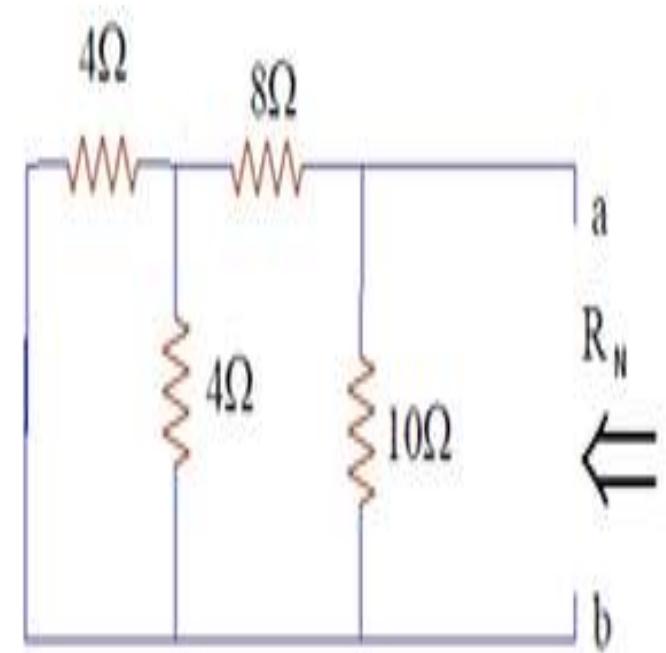
$$RT=4+(4\times8)/4+8=(20/3)\Omega$$

$$\text{Hence } I=20/RT=20/(20/3)=3A$$

$$|SC=3\times4/(4+8)=1A$$

In figure BESIDE battery has been removed by  
:short circuit and Norton's resistance is

$$5\Omega=10// [8+(4//4)]$$



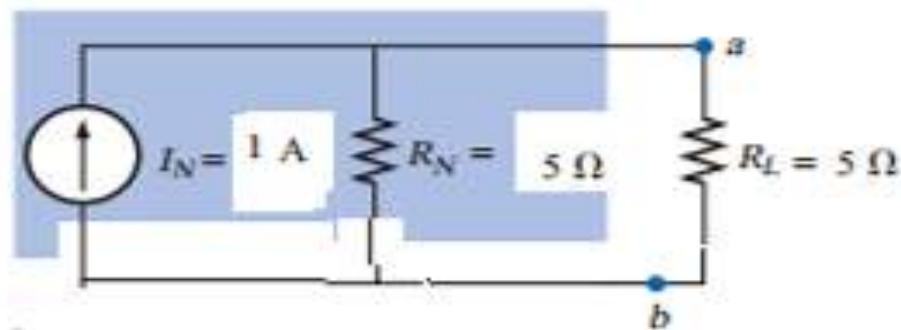
Hence; figure (e) gives Norton's equivalent circuit Now join  $5\Omega$  resistance back across terminals A and B.

: the current flowing through it is

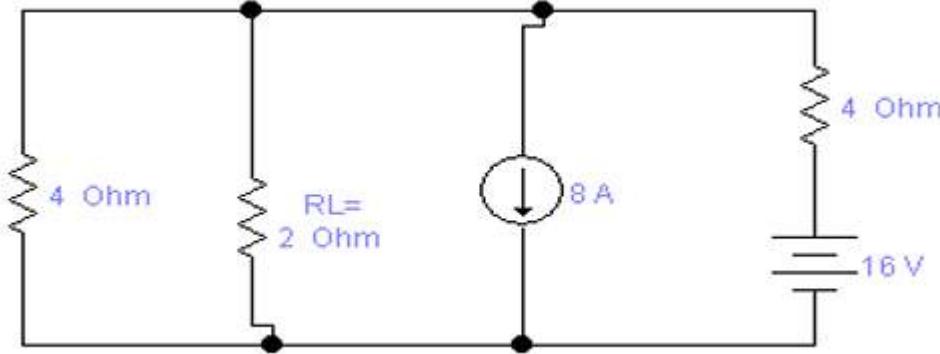
Hence; figure (e) gives Norton's equivalent circuit

Now join  $5\Omega$  resistance back across terminals A and B. the current flowing through it is:

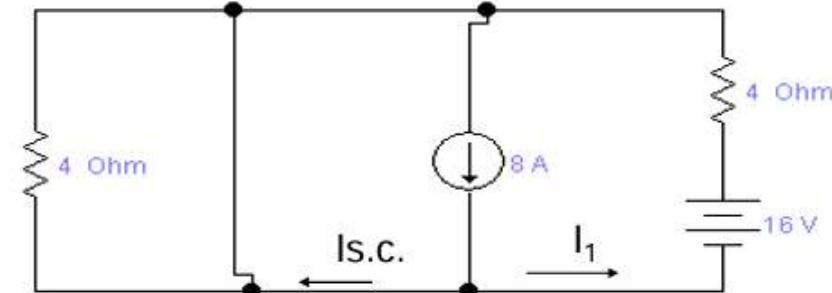
$$I = \frac{R_N I}{R_L + R_N} = \frac{(5\Omega)(1\text{ A})}{5\Omega + 5\Omega} = 0.5\text{ A}$$



Ex: find  $I_L$  FOR THE CIRCUIT SHOWN BY  
USING NORTON THEOREM



*Solution; 1- To find  $I_{s.c.}$*



$$I_1 = 16/4 = 4A$$

$$\text{then; } I_{s.c.} = 4A = I_N$$

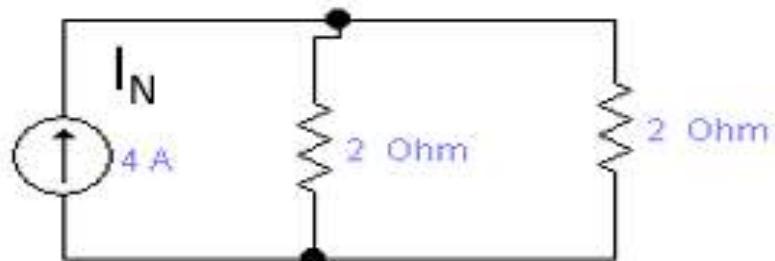
$$8 - I_1 - I_{s.c.} = 0 \text{ (K.c.L)}$$

2- TO find  $R_N$ :



$$R_N = (4 \times 4) / 8 = 2\Omega$$

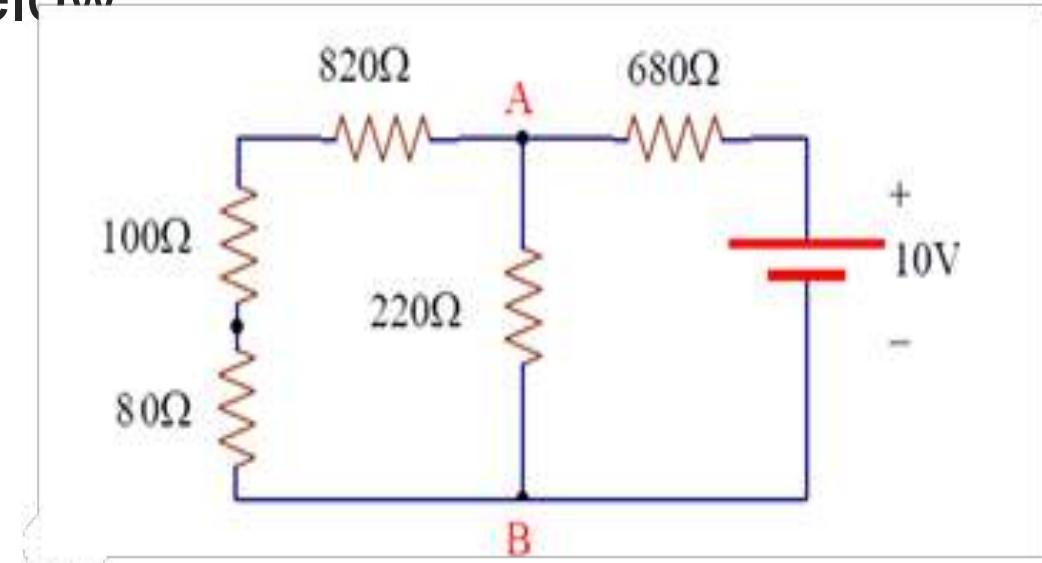
3- Drawing Norton's equivalent and calculate  $I_L$  at  $RL=2\text{ ohm}$



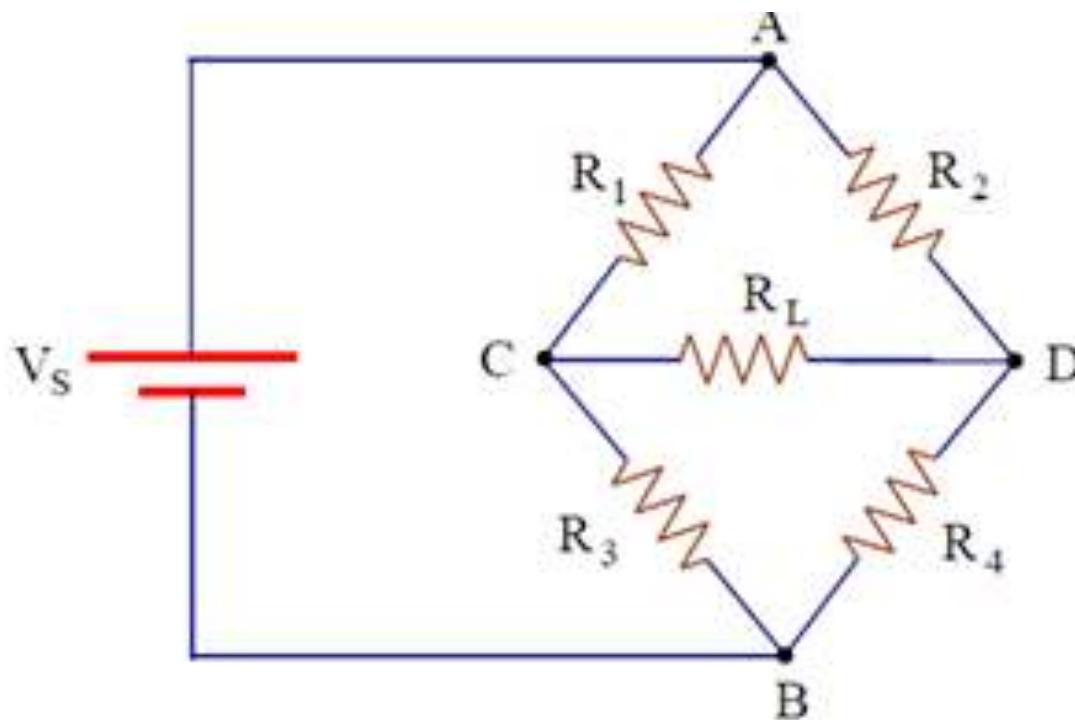
$$I_L = (4 \times 2) / (2 + 2) = 2A$$

# نشاط جماعي

Apply Norton's theorem to calculate current flowing through  $80\Omega$  resistor of fig. below



H.W. by using  
NORTON's theorem  
find the current  
through  $RL=1K\Omega$



[https://classroom.google.com/c/  
NzcxOTQ3MjE5MTc5/a/NzgzOTI4MzgxMTA0/  
details](https://classroom.google.com/c/NzcxOTQ3MjE5MTc5/a/NzgzOTI4MzgxMTA0/details)

ملاحظة: الحل يكون عبر منصتنا على الكلاسروم باستخدام الرابط  
اعلاه

رأيك يهمنا :



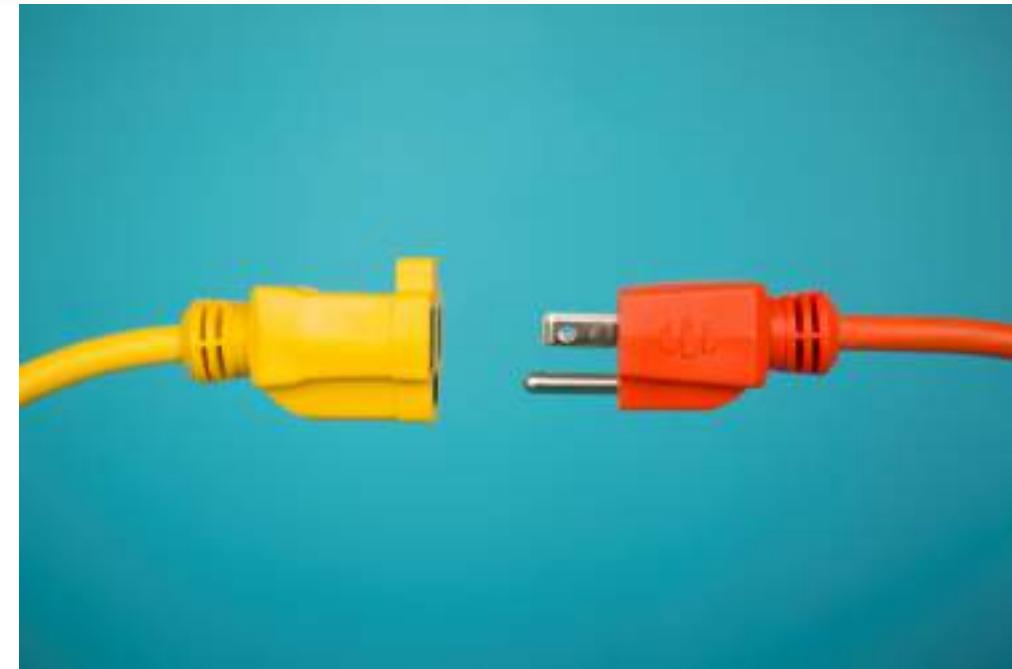
اعزائي الطالبة يرجى ملء الاستبيان  
ادناه :

المحاضرة السابعة  
**SOURCE  
TRANSFORMATION**



# :RATIONALS

ITS IMPORTANT TO  
STUDY SOURCE  
TRANSFORMATION  
THEOREM TO  
ANALYSING ELECTRICAL  
CIRCUITS



## الأهداف السلوكية

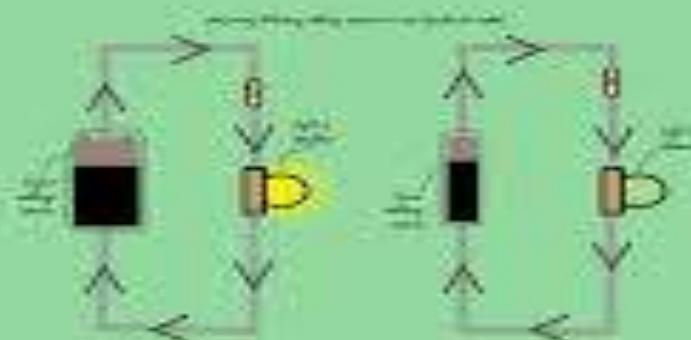


في نهاية المحاضرة سيكون الطالب  
قادرا على :

- فهم المبادئ الأساسية لنظرية تحويل المصادر
- تحليل الدوائر الكهربائية التي تحتوي على أكثر من مصدر فولتية او تيار او كلاهما

# الاختبار القبلي

برايك هل من الممكن تحويل مصدر التيار الى مصدر فولتية ؟



الجهد الكهربائي  
Voltage  
المدى الكهربائي

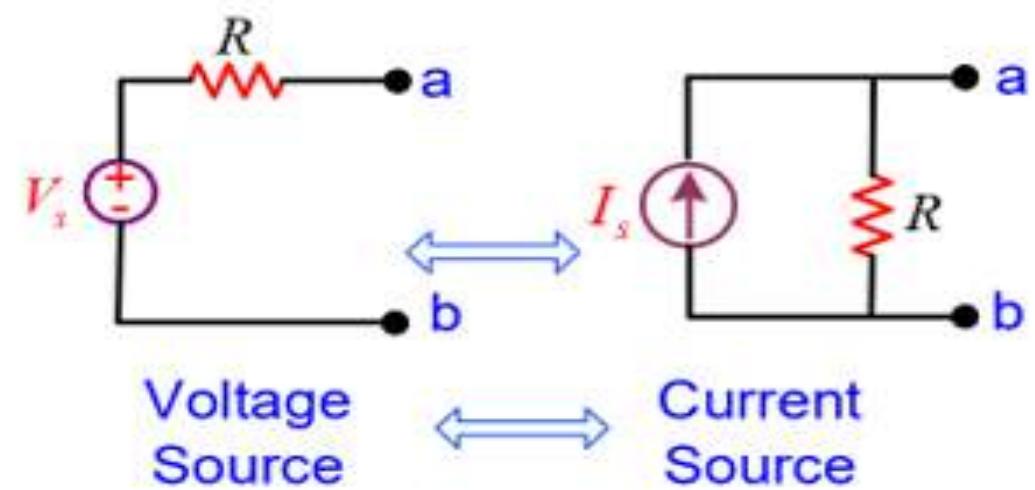
# :Source Transformation

Equivalent sources can be used to simplify the analysis of some circuits.-

A voltage source in series with a resistor is transformed into a current-source in parallel with a resistor.

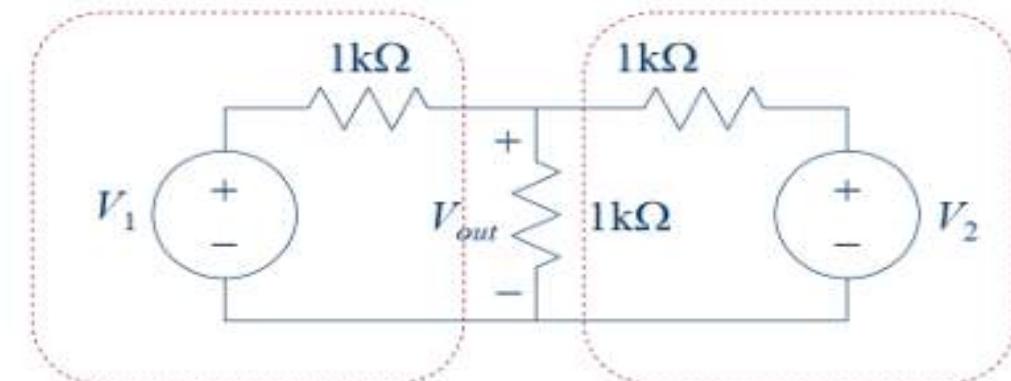
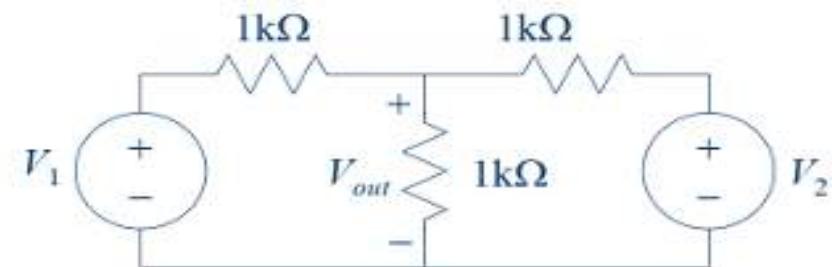
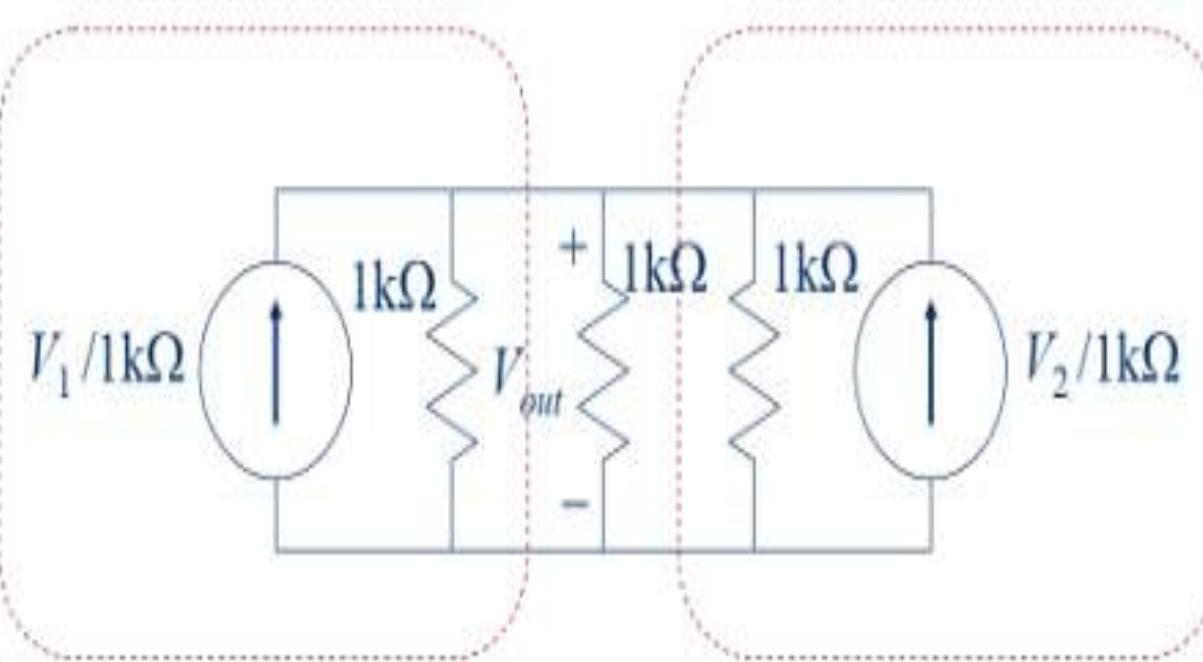
A current source in parallel with a resistor is transformed into a voltage -  
.source in serie

$$V_S = I_S R$$
$$I_S = \frac{V_S}{R}$$



**For the circuit shown in the Figure below, how can source transformation make analysis of this circuit easier**

Which is a single node-pair circuit  
that we can use current division on



**EXAMPLE:** In the circuit shown below, use a source transformation to determine  $V_o$

**:SOLUTION**

Replace the current source 3A in parallel with 4Ω resistor

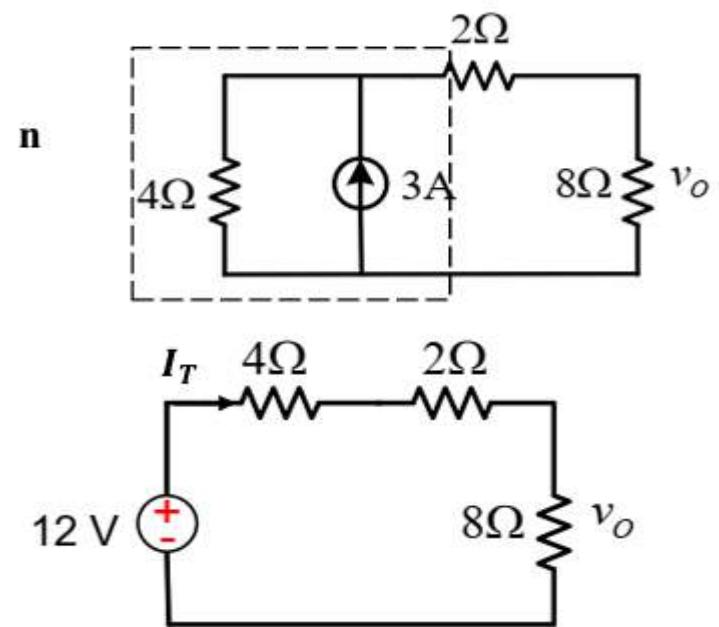
to a 12V voltage source in series with 4Ω resistor

$$VS = 3A \times 4\Omega = 12V$$

$$RT = 4\Omega + 2\Omega + 8\Omega = 14\Omega$$

$$IT = VS / RT = 12V / 14\Omega = 0.857A$$

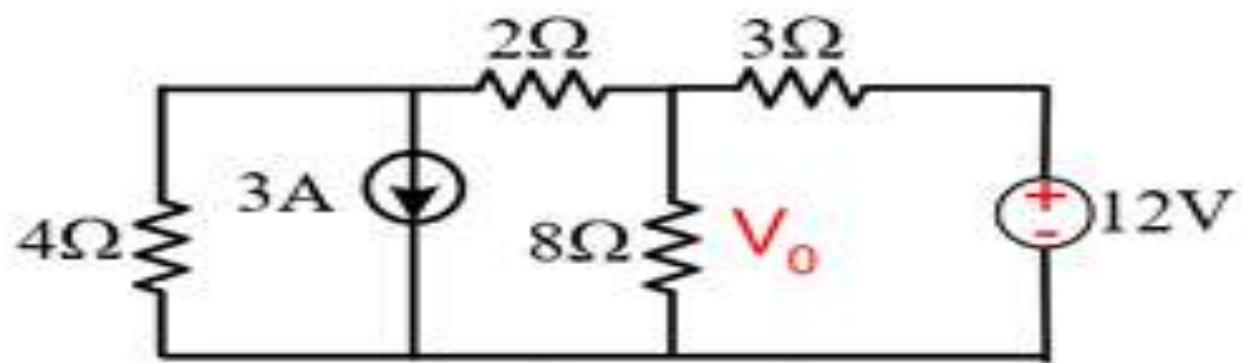
$$Vo = 0.857 \times 8\Omega = 6.856V \therefore$$





## نشاط تفاعلي(3 دقائق)

For the circuit shown in Figure determine  
.the  $V_o$  using source transformation





اكتب تقريراً معززاً بالامثلة عن كيفية تطبيق  
نظريّة تحويل المصادر مع نظرية ثيفن

ملاحظة: ارفع الجواب على الرابط أدناه في منصة الكلاسرووم

[https://classroom.google.com/c/  
NzcxOTQ3MjE5MTc5/a/NzgzOTcwNjAxMDY5/details](https://classroom.google.com/c/NzcxOTQ3MjE5MTc5/a/NzgzOTcwNjAxMDY5/details)

# HOMEWORK

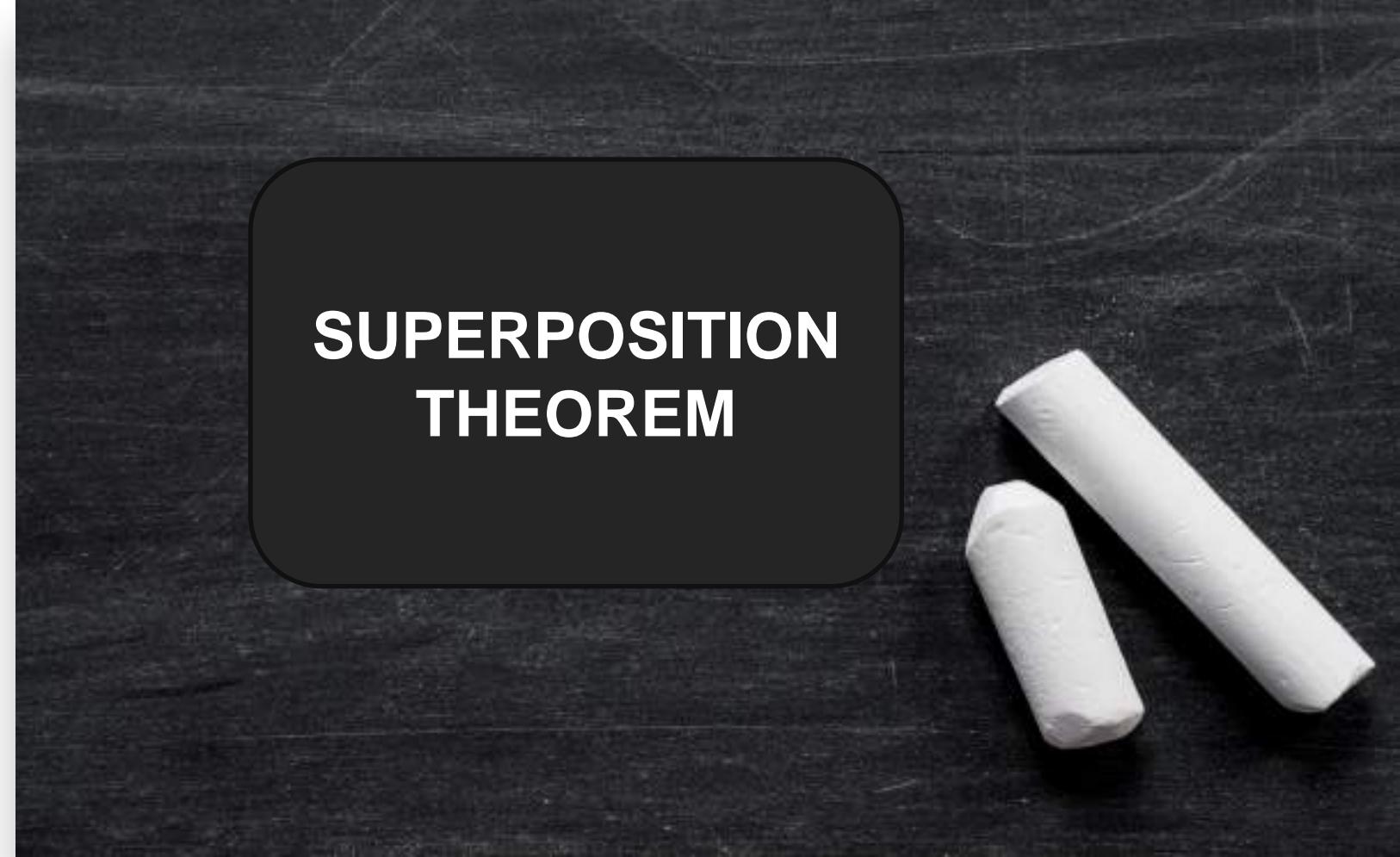
## الاختبار البعدى



# المحاضرة الثامنة

SUPERPOSITION  
THEOREM

SUPERPOSITION  
THEOREM



# :RATIONAL

Definition Suppers position theorem •

To calculate the load current flows from each source and to find the result •  
.from the total currents



## الأهداف السلوكية

- فهم المبادئ الأساسية لنظرية التراكب
- تحليل الدوائر الكهربائية الخطية التي تحتوي على أكثر من مصدر

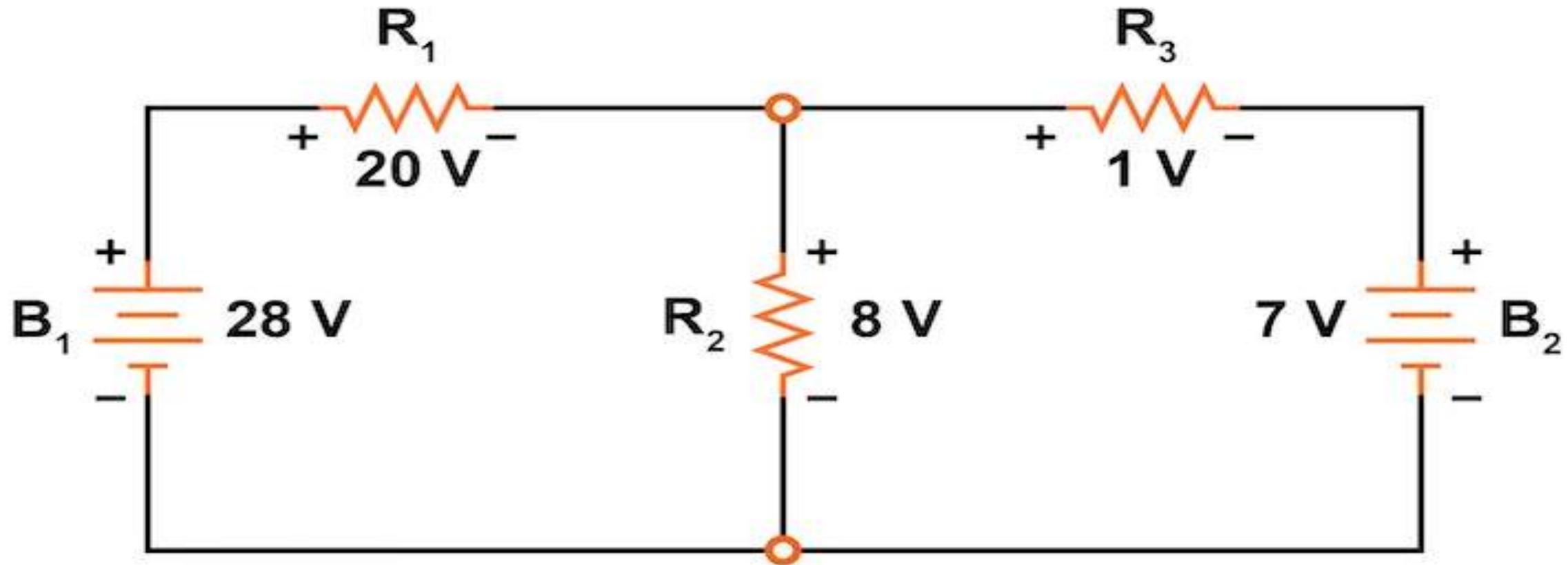


Did you have any information about super position  
?theorem

الاختبار القبلي

Raise **your hand before answer**

CAN you find the total current for the circuit below



# The superposition theorem states the :following

**The current through , or voltage across , at any element in a linear network is equal to the algebraic sum of the currents or voltages produced independently by each source**

**This is done by making voltage source as short circuit , and current source as open circuit**

# :Example 1

**Using superposition theorem ,to determine the current through 4-ohm resistor**

:Solution

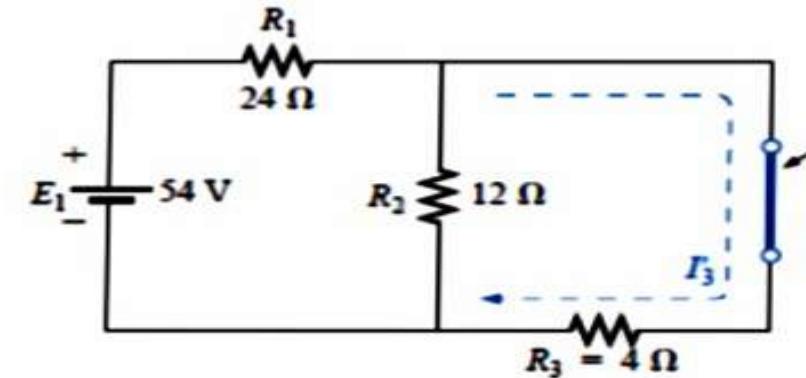
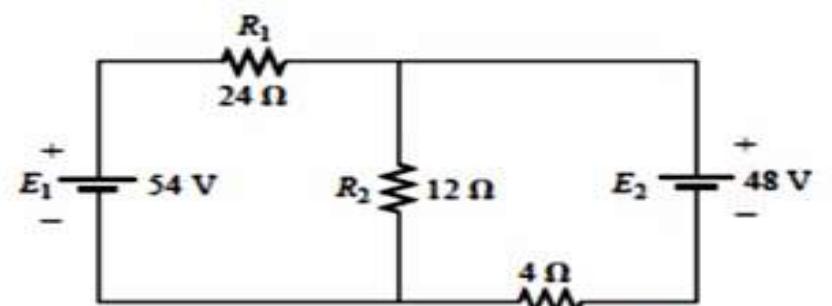
:Considering the effect of 54V Source

$$R_T = R_1 + (R_2 // R_3) = 24 + (12//4) = 27\Omega$$

$$I = E_1 / R_T = (54 / 27) = 2A$$

(NOW by using current divider we can calculate the current through (4Ω)

$$I' = 2 * (12 / 4 + 12) = 1.5 A$$



$$R_T = 4 + (12 // 24)$$

$$12\Omega = (24/12 + 24*12) + 4 =$$

$$I_t = 48/12 = 4A$$

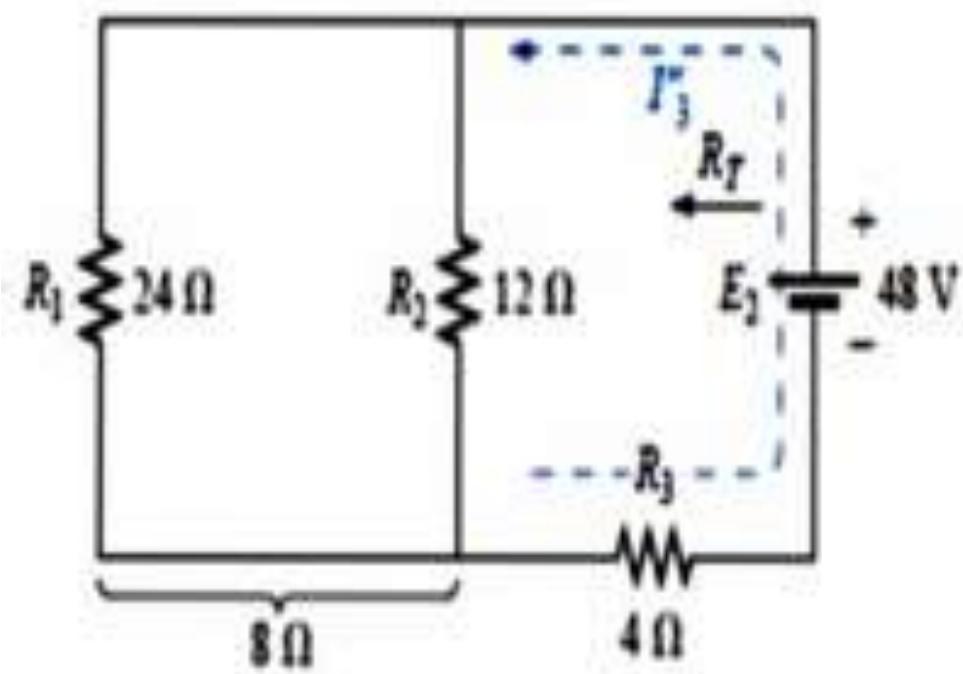
to find the current through  $4\Omega$  resistor

It's the same of total current

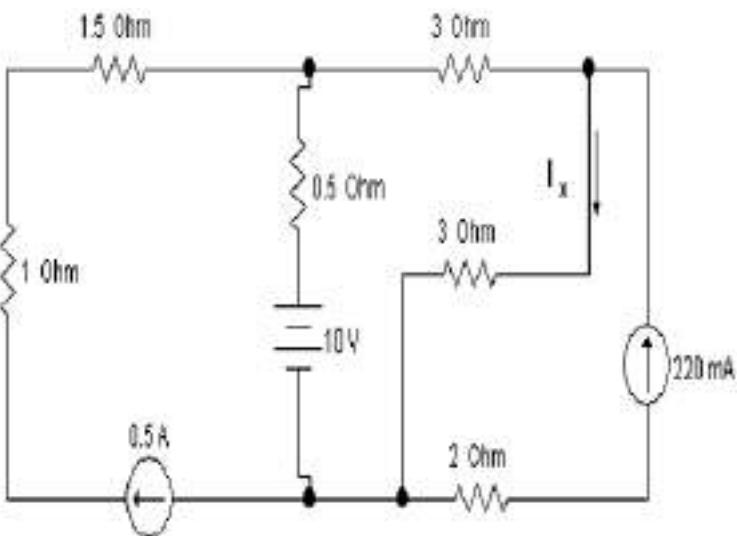
$$I'' = 4 A$$

Now the current through  $4 \Omega$  is the  
"algebraic sum of  $I'$  and  $I$ "

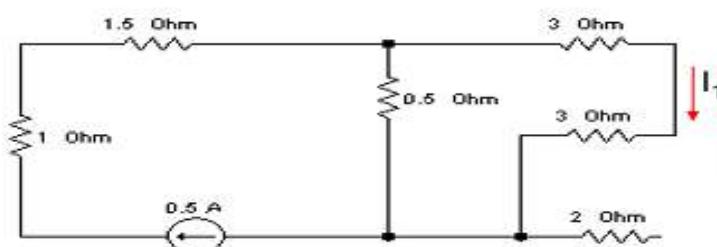
$$I''' = 4 - 1.5 = 2.5 A$$



For the cct. Shown using supper position theorem to find ( $I_x$ )

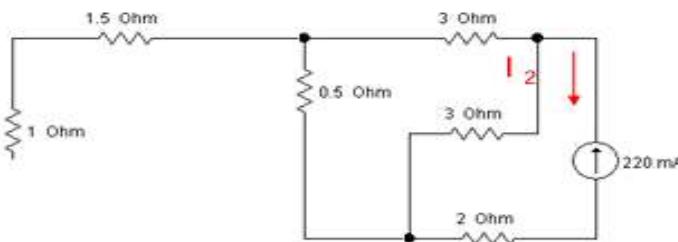


Solution:- 1- Effect of 0.5A only



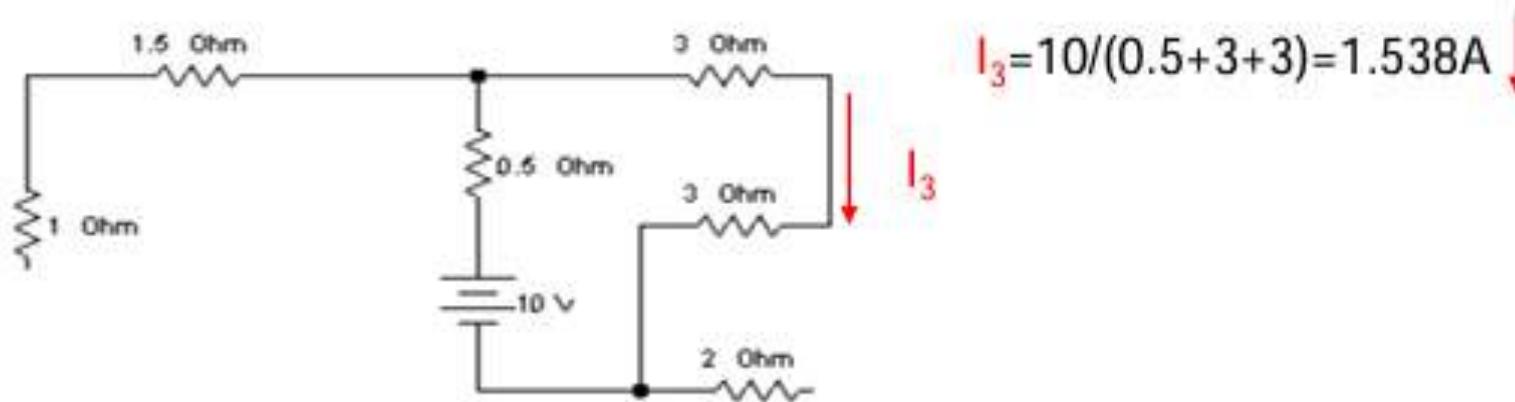
$$I_1 = 0.5 \times 0.5 / (0.5 + (3+3)) = 0.038 \text{ A}$$

2- Effect of 220mA only



$$I_2 = 0.22 \times (3+0.5) / (3.5+3) = 0.118 \text{ A}$$

### 3- Effect of 10v only



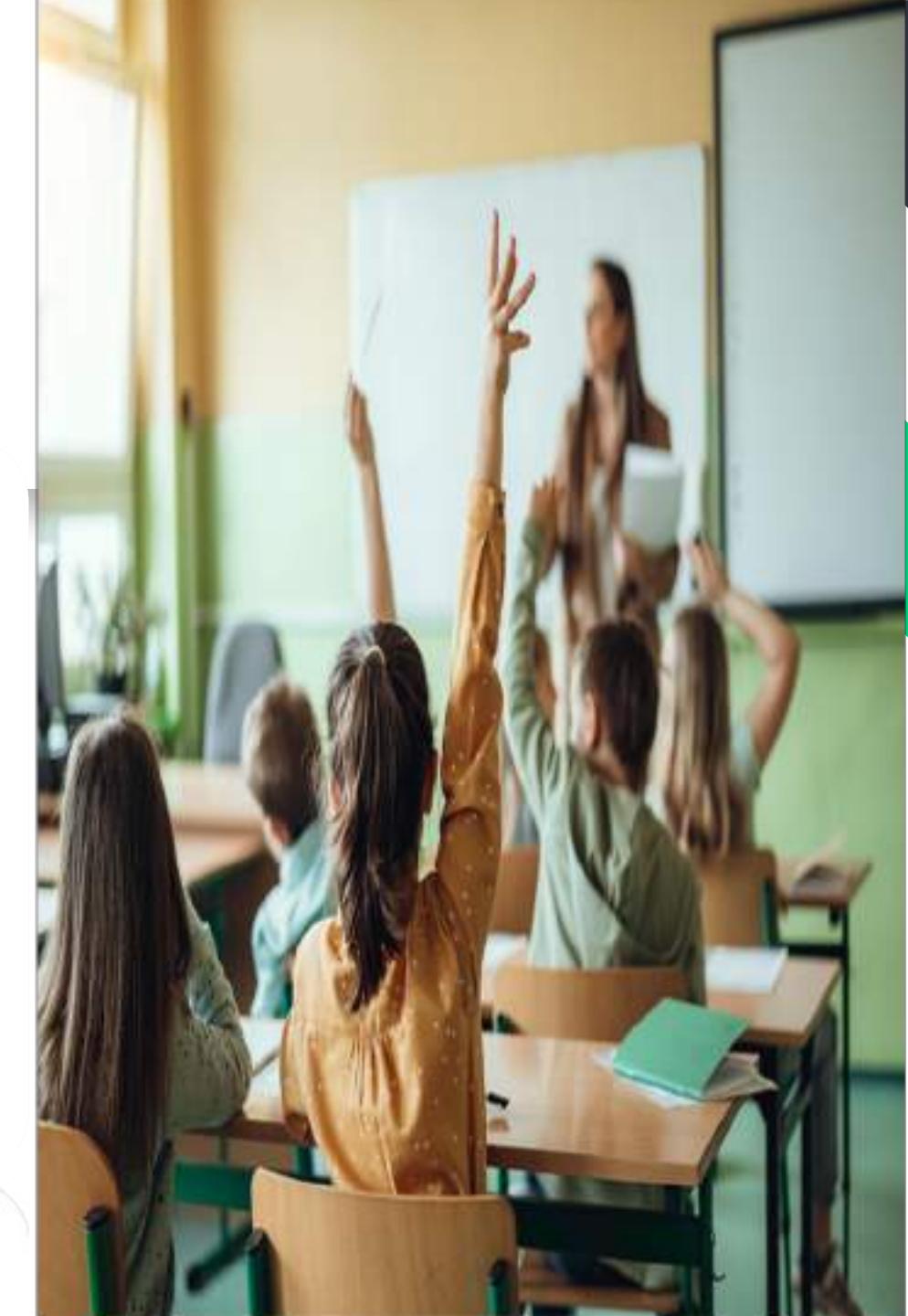
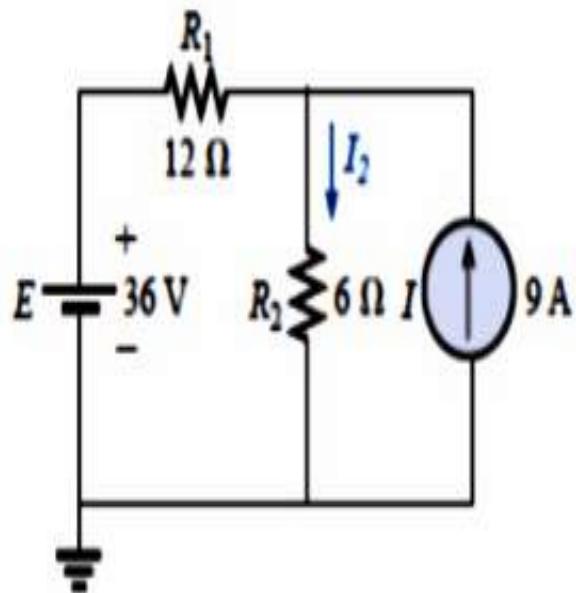
$$I_3 = 10 / (0.5 + 3 + 3) = 1.538 \text{ A}$$

Then  $I_x = I_1 + I_2 + I_3 = 1.694 \text{ A}$

## :Example 2



Using superposition, determine the current through the  $6\text{-}\Omega$  resistor ??



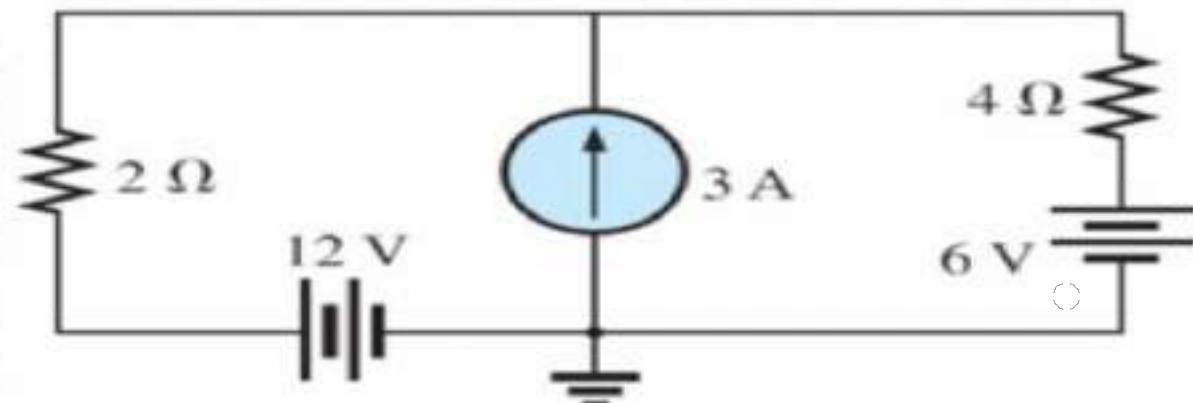
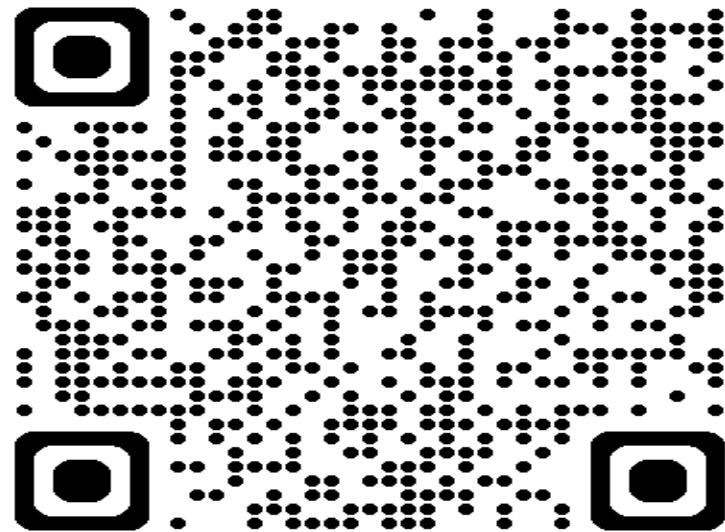
# الاختبار البعدى

H.W



BY USING SUPERPOSITION THEOREM ,FIND THE CURRENT THROUGH ( $2\Omega$ ) resistor

الواجب البيئي يرفع على  
منصة الكلاس روم على الـ  
QR CODE اعلاه



رابط المحاضرة على  
منصة النيير بود

<https://app.nearpod.com/?pin=X2VUP>

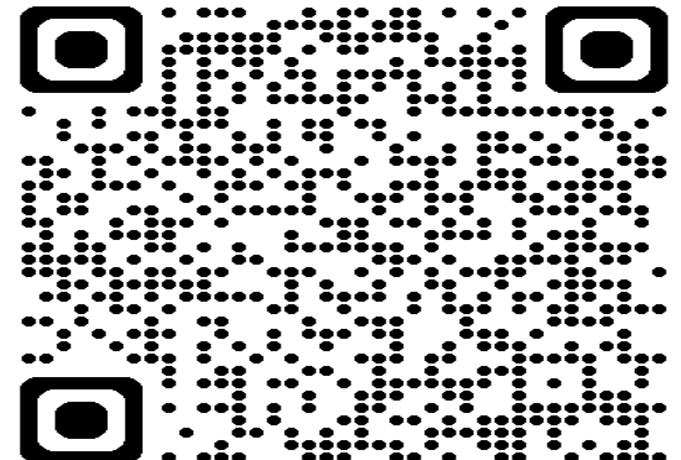


رابط المحاضرة على منصة  
الكوكل كلاس روم

[https://classroom.google.com/c/  
NzcxOTQ3MjE5MTc5/m/  
Njk5ODIxMzc2MTM1/details](https://classroom.google.com/c/NzcxOTQ3MjE5MTc5/m/Njk5ODIxMzc2MTM1/details)



Google Classroom





# YouTube

Before homework you can  
see this channel on youtube

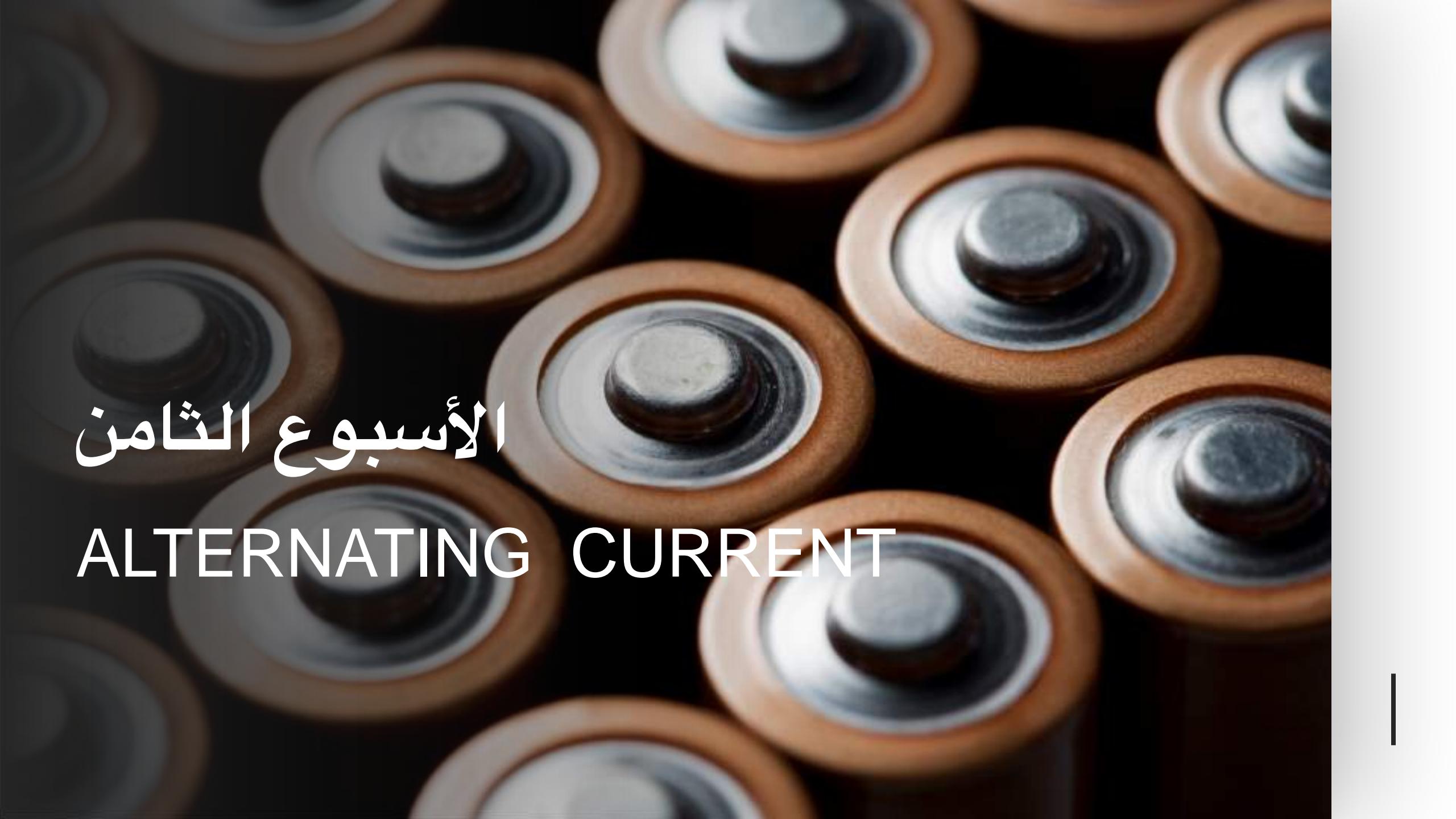
[https://youtube.com/playlist?  
list=PLpyY3RPgxKCKuMsdS-  
X6LXQMxpRlaGwFa&si=SkuVH63t0bzbUb  
fX](https://youtube.com/playlist?list=PLpyY3RPgxKCKuMsdSX6LXQMxpRlaGwFa&si=SkuVH63t0bzbUbfX)



رأيك يهمنا

يرجى فتح الـQR code  
ملء الاستبيان:





الاسبوع الثامن

ALTERNATING CURRENT

# :RATIONAL

It is very important to study  
Alternating current ( A . C )  
Also to analysis the sine  
wave

# :CENTERAL IDEA

Definition the sine wave

To learn how the sine wave generated •

- To learn how we find R.m.s current  
and average value

# الاختبار القبلي

## Pretest



Define : 1- frequency



2- Angular frequency

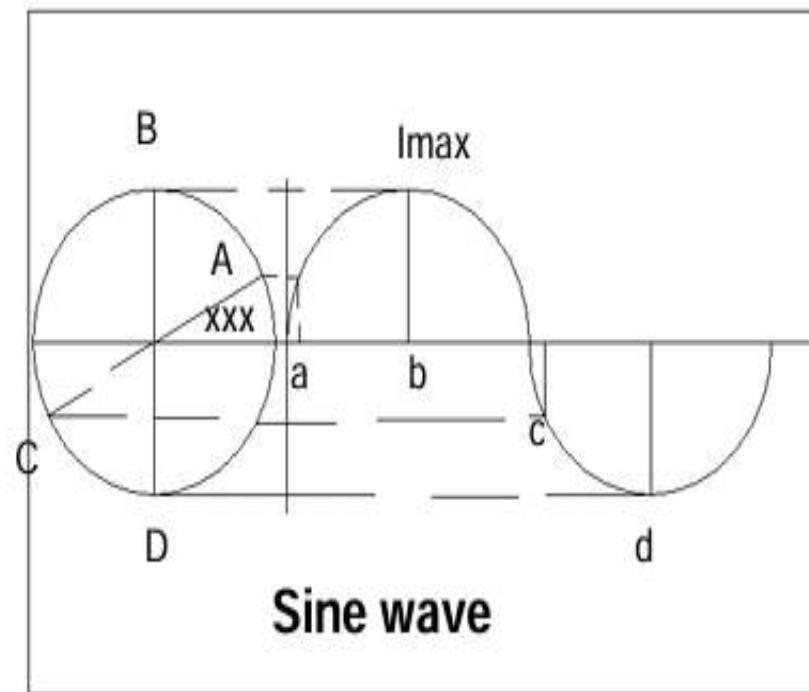
3-  $\pi$

### Solution

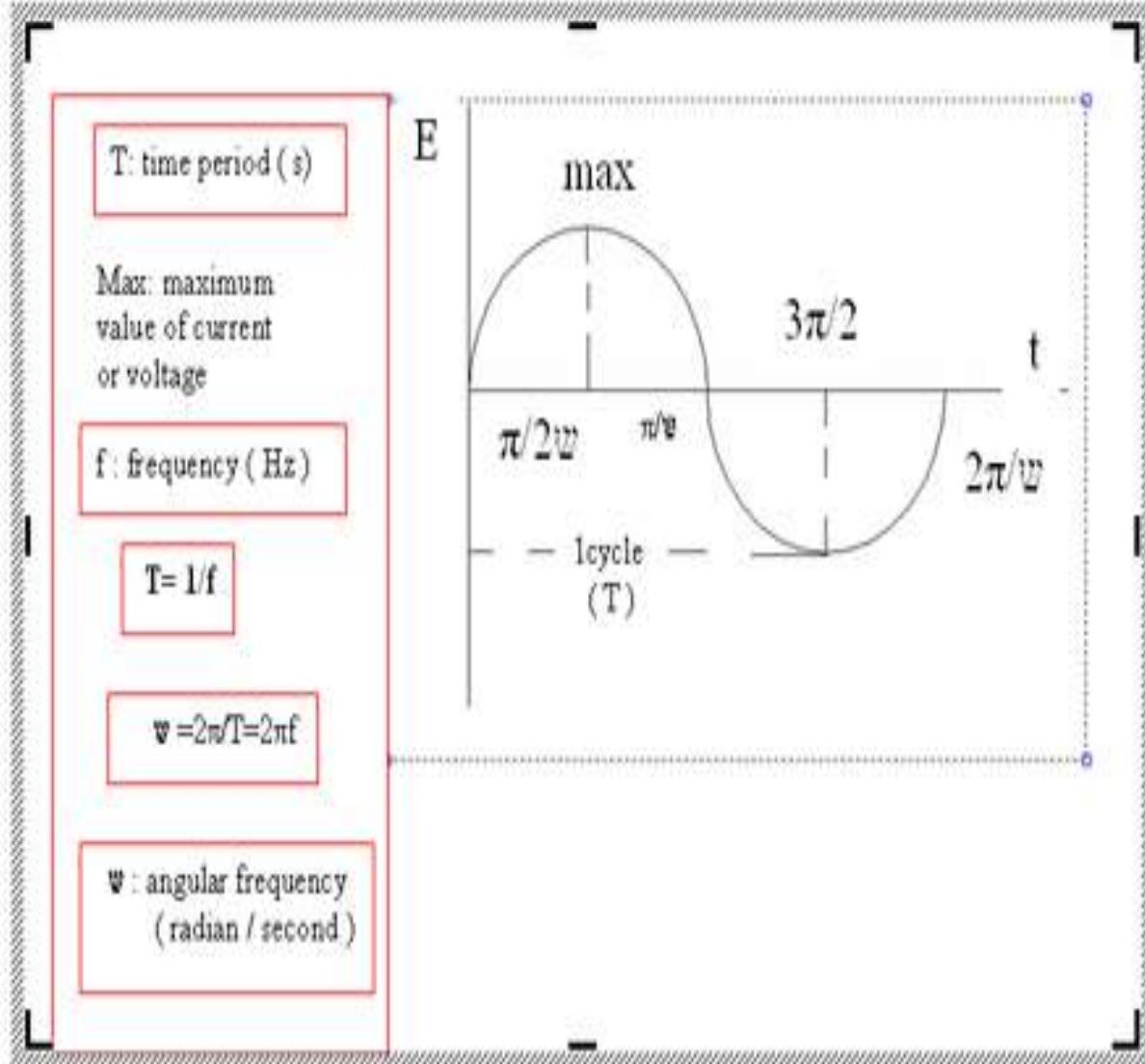
1-  $f$  : عدد الذبذبات الحاصلة خلال الثانية الواحدة ويقاس (د/ث) أو هرتز

التردد الزاوي / أي أن الموجة تتذبذب بشكل زاوي وليس بشكل خطى ويقاس (زاوية نصف قطرية/ثانية)  $\omega$  -  
وهي النسبة الثابتة ( $3,14$ ) أما بالزوايا فمقدارها ( $180$  درجة)

$$\omega = 2\pi f$$



$$\sin \theta = A / I_{\max} \therefore A = I_{\max} \sin \theta$$



## Average value (Means value )

$$I_{av.} = \frac{i_1 + i_2 + \dots + i_n}{n}$$

$$I_{av.} = \frac{1}{T} \int_0^T i_{(t)} dt ; V_{av.} = \frac{1}{T} \int_0^T e_{(t)} dt$$

## Instantaneous value

$$i(t) = I_{max.} \sin(\omega t) ; v(t) = V_{max.} \sin(\omega t)$$

i:- Instantaneous value of current

V :- Instantaneous value of voltage .

Maximum value :- It is the maximum Value of the instantaneous values . ( $I_{max.}, V_{max.}$  ) .

Root mean square (r.m.s.) ( $I_{r.m.s.} = I_{effect}$  ) .

$$I_{r.m.s.} = \sqrt{\frac{i_1^2 + i_2^2 + i_3^2 + \dots + i_n^2}{n}}$$

For full wave we fawned the effect value as follow :-

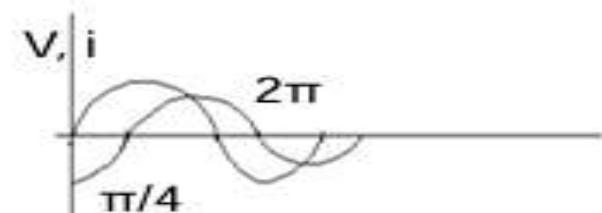
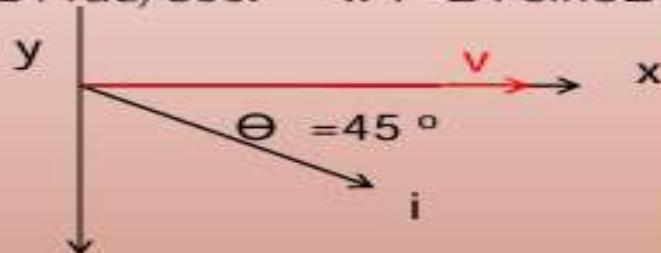
$$I_{r.m.s.} = \sqrt{\frac{1}{T} \int_0^T i^2 dt} ; V_{r.m.s.} = \sqrt{\frac{1}{T} \int_0^T v^2 dt}$$

Example (1): In A.c. sinusoidal voltage with peak (24v ) applied to a circuit then the current (3A) if the voltage lead the peak current by (45°) and frequency (50 . HZ ) write the equation for  $V(t)$ ,  $I(t)$  and draw form and phase diagram

Solution :-

$$V_m = 24 \text{ V} ; I_m = 3 \text{ A} ; \theta = 45^\circ ; f = 50 \text{ Hz}$$

$$v = V_m \sin \omega t \quad i = I_m \sin(\omega t - \pi/4) \quad \omega = 2\pi f = 2\pi \times 50 = 314 \text{ rad/sec.}$$
$$\therefore v = 24 \sin 314 t \quad i = 3 \sin(314t - \pi/4)$$



Ex 2: Find(r.m.s.) : Av. :Kf : Kp : f for the voltage

$$v = 100 \sin 314t$$

Solution:-

$$V = V_m \sin \omega t \quad V_m = 100 \quad \omega = 314$$

$$V_{r.m.s} = V_m / \sqrt{2} = 0.707 \times V_m = 0.707 \times 100 = 70.7 \text{ v}$$

$$V_{av.} = 2V_{max} / \pi = 0.636 \times V_{max.} = 0.636 \times 100 = 63.6 \text{ v}$$

$$K_f = V_{r.m.s.} / V_{av.} = 70.7 / 63.6 = 1.11$$

$$K_p = V_{max} / V_{r.m.s.} = 100 / 70.7 = 1.414, \omega = 2\pi f \therefore f = \omega / 2\pi = 314 / 2 \times 3.14 = 50 \text{ Hz}$$

لحساب القيمة الفعالة لموجة تيار جيبية نتبع الآتي :

$$I^2_{\text{r.m.s.}} = \frac{1}{2} \pi \int_0^{2\pi} I^2 d\theta = \frac{1}{2} \pi \int_0^{2\pi} (Im \sin \theta)^2 d\theta =$$

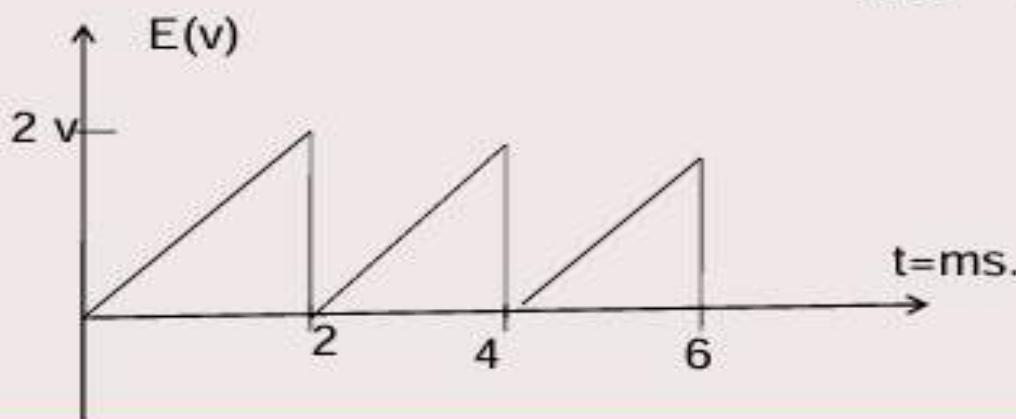
$$I^2 m / 2 \pi \int_0^{2\pi} \sin^2 \theta d\theta \quad \text{But: } \sin^2 \theta = \frac{1}{2}(1 - \cos 2\theta) \quad \text{then:}$$

$$I^2_{\text{r.m.s.}} = I^2 m / 4 \pi \int_0^{2\pi} (1 - \cos 2\theta) d\theta = I^2 m / 4 \pi \left[ (\theta - \frac{\sin 2\theta}{2}) \right]_0^{2\pi}$$

$$= I^2 m / 4 \pi [2\pi - 0] \therefore I_{\text{r.m.s.}} = Im / \sqrt{2} = 0.707 Im$$

وبنفس الطريقة يمكن ايجاد  $V_{\text{r.m.s.}}$  ←  $V_{\text{r.m.s.}}$

Ex : For the wave form shown find the Peak factor ( $k_p$ ) . Then find form factor ( $k_f$ ) .

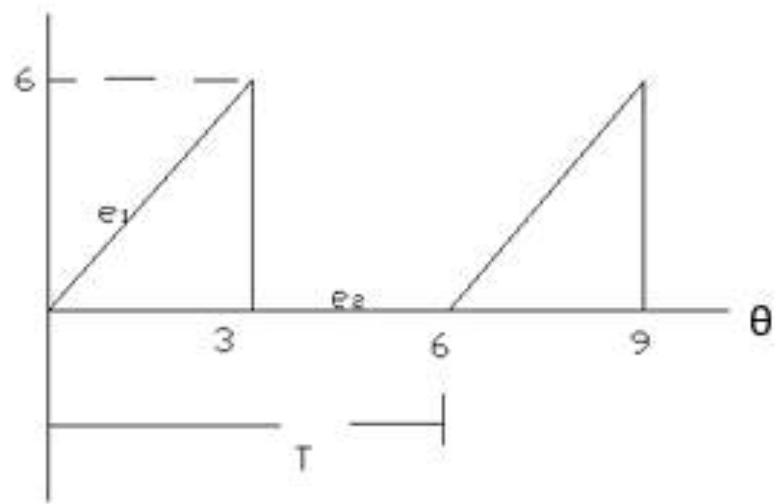


**Solution :-**  $k_p = E_m/E_{av.}$  :  $E_m = 2v$   $T = 2$   $E_{av.} = 1/T \int_0^T e(t) dt$  ,  $e = mx + y$   
 $= (2/2)t + y = t + 0 = t$   $\therefore E_{av.} = 1/2 \int_0^2 t dt = \frac{1}{2} \left( \frac{t^2}{4} \right)_0^2 = (1/4) \times 4 = 1 \text{ volt}$   $\therefore k_p = 2$

$$E_{r.m.s.} = \sqrt{1/T \int_0^T e^2(t) dt} , \therefore E^2_{r.m.s.} = 1/4 \left( \int_0^2 t^2 dt \right) = (1/4) \times \left( t^3/3 \right)_0^2$$

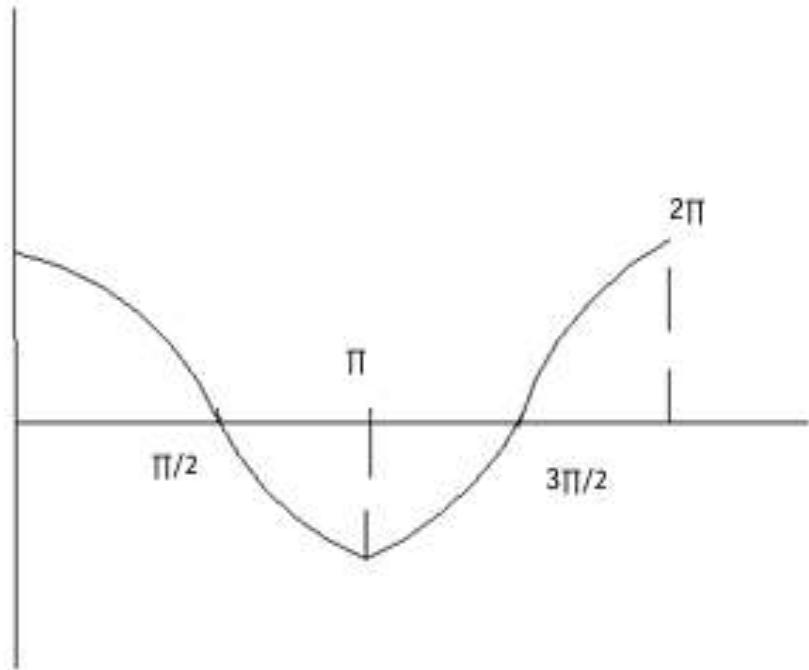
$$\therefore E^2_{r.m.s.} = 8/12 \therefore E_{r.m.s.} = 2/\sqrt{3}, k_f = E_{r.m.s.}/E_{av.} = 2/\sqrt{3}$$

H.W.FIND  $K_f$  ,  $K_p$  for current wave below



## الاختبار البعدى

Find average value , $K_f$  , $K_a$  for half wave shown :



# Effect of alternating current at circuit in seiries

الأسبوع التاسع

# Objectives

Aim of lecture To make the student should be able to determine the impact of AC circuits linking respectively, and to learn to find the relationship between the current and voltages in connecting respectively, and finding phase angle and total defiance of the electrical circuit



# pretest

, Define : Phase shift , Phase diagram ,Phase angle( $\phi$ )  
, inductance(L), Capacitance (c ), Inductive reactance (XL)  
Capacitive reactance (xc),Impedance(Z)

## R- L in series

$$V_R = I \cdot R, V_L = I \cdot X_L$$

$$V = \sqrt{V_R^2 + V_L^2}$$

$$= \sqrt{(I \cdot R)^2 + (I \cdot X_L)^2}$$

$$V = I \sqrt{(R^2 + X_L^2)}$$

$$\therefore Z = V/I = \sqrt{(R^2 + X_L^2)}$$

(Ω) Impedance of the cct.

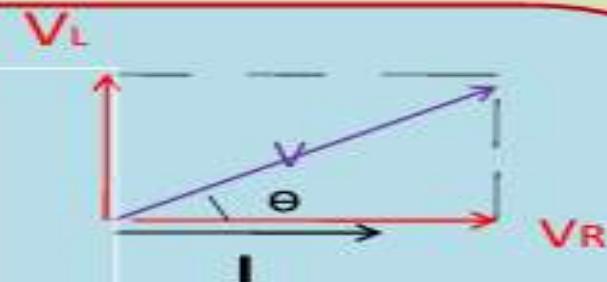
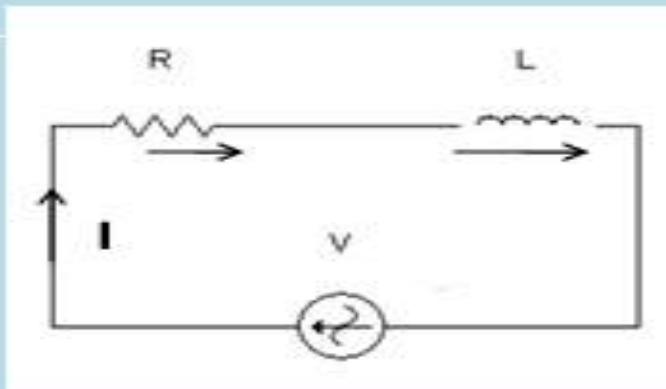
$$\tan \theta = V_L/V_R = I \cdot X_L / I \cdot R = X_L / R$$

$$\therefore \tan \theta = V_L/V_R \therefore \theta = \tan^{-1} V_L/V_R$$

$$\tan \theta = X_L/R \therefore \theta = \tan^{-1} X_L/R$$

$\theta$  = phase angle between  $V$  and  $I$

قيمة الزاوية تتراوح اكبر من الصفر واصغر من 90 درجة (موجبة) مثل  $+30$  او  $+45$  او  $60$  او  
 قيمة الزاوية الفولتية - قيمة  $\theta$  (مثل  $-30$  او  $-45$  او  $-60$ ) = زاوية التيار في حال زاوية الفولتية = 0



Triangle of Impedance

**Ex(1) :-** For the cct. Shown find the value and direction the current

$$Z = \sqrt{R^2 + XL^2}, XL = \omega \cdot L = 314 \times 0.1 = 31.4 \Omega$$

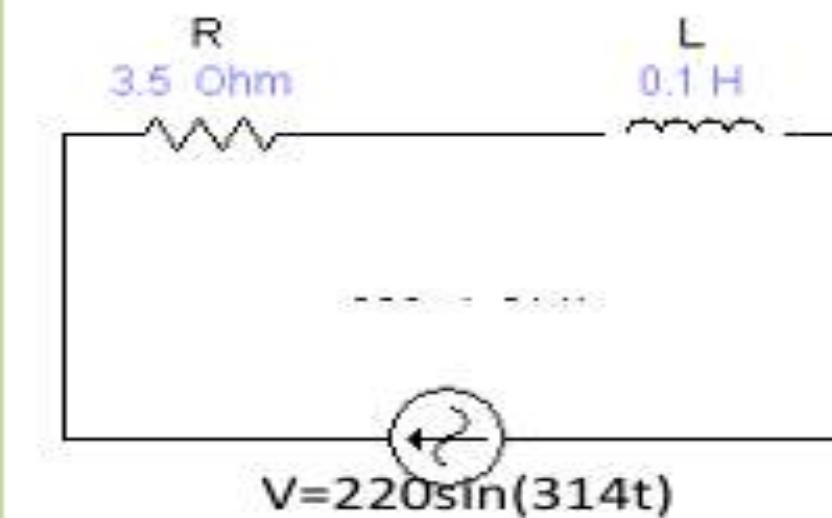
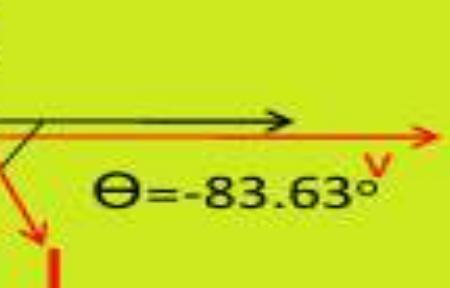
$$Z = \sqrt{(3.5)^2 + (31.4)^2} = 31.6 \Omega$$

$$I = V/Z = 220/31.6 = 6.96 A$$

$$\Theta = \tan^{-1} XL/R = \tan^{-1} 31.4/3.5 = \tan^{-1} 8.97$$

$$\therefore \Theta = 83.63^\circ \therefore i = 6.96 < -83.63^\circ$$

$$\therefore i = 6.96 \sin(314t - 83.63^\circ) A \text{ amper}$$



### R-C in series

$$V_R = I \cdot R, V_C = I \cdot X_C$$

$$V = \sqrt{V_R^2 + V_C^2} = \sqrt{(I \cdot R)^2 + (I \cdot X_C)^2}$$

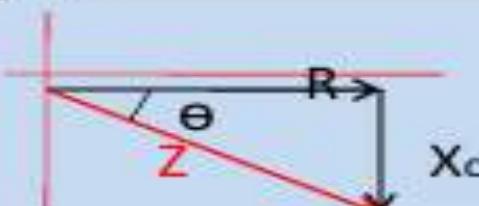
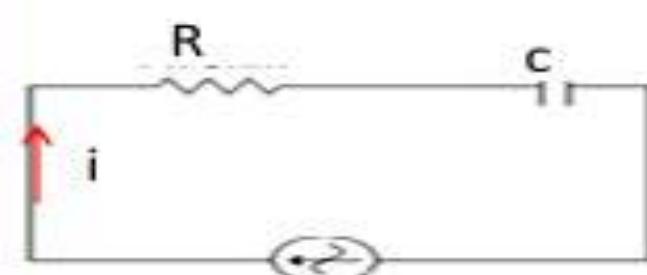
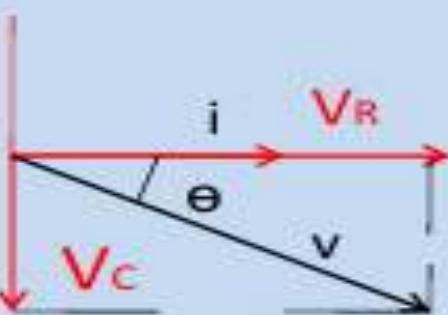
$$V = I \sqrt{R^2 + X_C^2}$$

$$\therefore Z = V/I = \sqrt{R^2 + X_C^2}, \quad X_C = 1/\omega \cdot C$$

$$\tan \theta = V_C/V_R = I \cdot X_C / I \cdot R = X_C / R$$

$$\therefore \theta = \tan^{-1} V_C/V_R \quad \text{Or}$$

$$\tan \theta = X_C / R \quad \therefore \theta = \tan^{-1} X_C / R$$



Ex(2) : For the cct. Shown if ( $I=1A$ ) find ( $f$ ), then what are the value of ( $R$ ) that connected with ( $C$ ) to reduce the current to ( $0.5A$ ) with the same frequency .

**Solution**

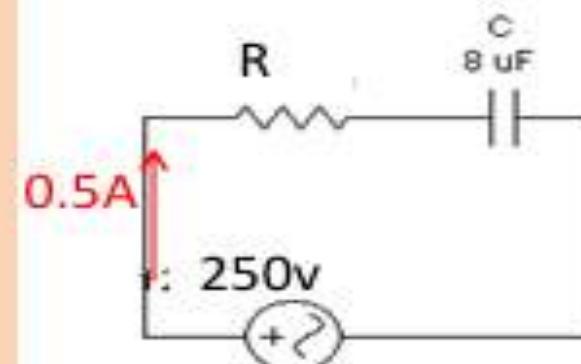
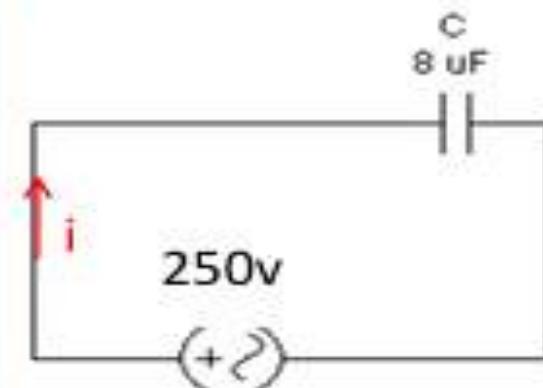
$$X_C = V_C / I_C = 250 / 1 = 250 \Omega$$

$$X_C = 1 / \omega \cdot C = 1 / 2\pi f C \quad \therefore f = 1 / (2\pi \cdot C \cdot X_C)$$

$$f = 1 / (2 \times 3.14 \times 8 \times 10^{-6} \times 250) = 79.5 \text{ Hz}$$

$$Z = \sqrt{(R^2 + X_C^2)} = \sqrt{(R^2 + 250^2)}, \quad Z = 250 / 0.5 = 500 \Omega$$

$$\therefore 500^2 = R^2 + 250^2 \quad \therefore R^2 = 500^2 - 250^2 \quad \therefore R = 433 \Omega$$



## R-L-C in series

1- If  $X_L > X_C \therefore V_L > V_C$

$$V_R = I \cdot R, V_L = I \cdot X_L, V_C = I \cdot X_C, V = \sqrt{V_R^2 + (V_L - V_C)^2}$$

$$V = I \cdot \sqrt{R^2 + (X_L - X_C)^2}$$

$$\therefore Z = V/I = \sqrt{R^2 + (X_L - X_C)^2}$$

$$\Theta = \tan^{-1} (V_L - V_C) / V_R$$

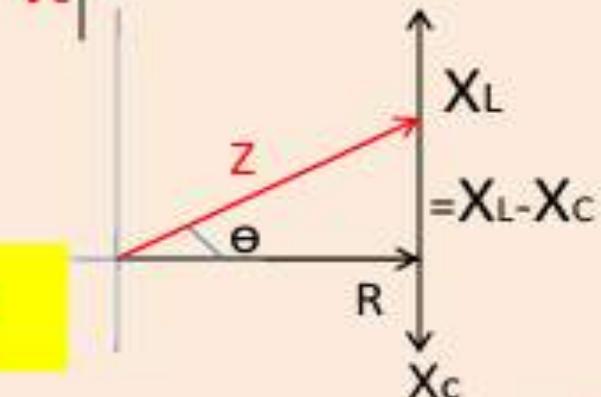
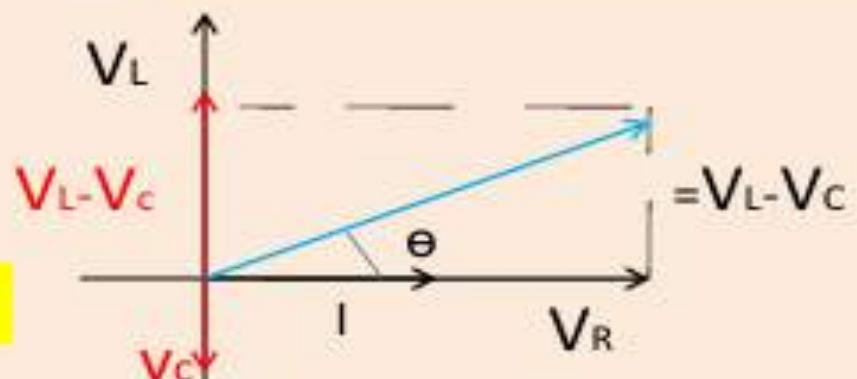
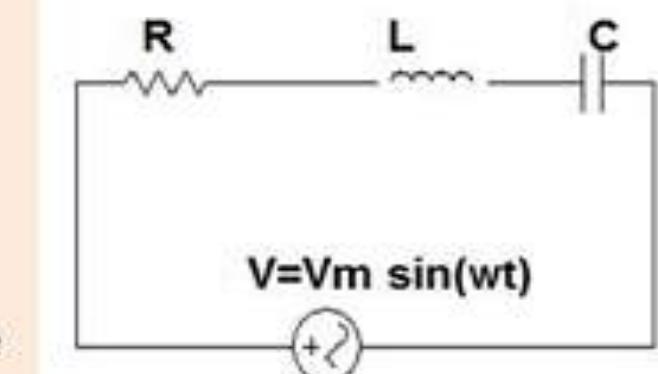
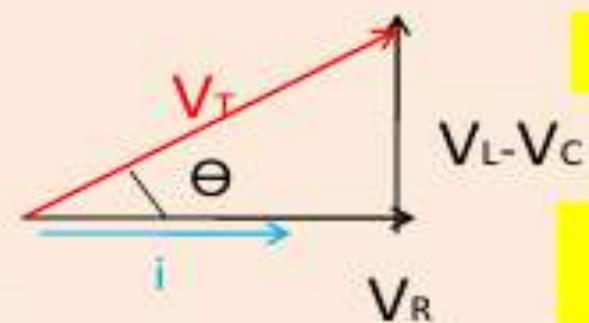
$$\Theta = \tan^{-1} (X_L - X_C) / R$$

Also :  $X_L > X_C$  :

1/ the cct. is inductive

2/  $\Theta$  is positive

3/  $V_T$  lead  $V_R$  by  $\Theta$



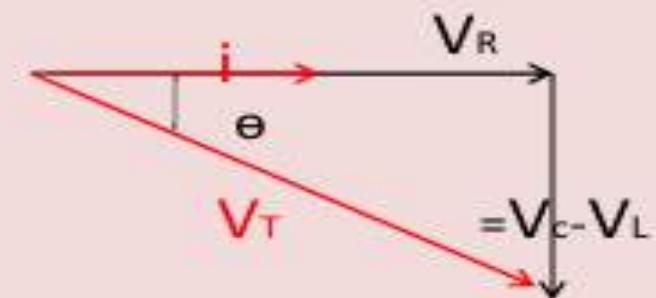
2/ If  $X_C > X_L \therefore V_C > V_L$

When  $X_L < X_C$

1/ The cct. Is capacitive

2/  $\theta$  is negative

3/  $i_T$  leads  $V_T$  by  $\theta$



3/ If  $X_L = X_C \therefore V_L = V_C$

When  $X_L = X_C$

1/ We have **resonance case**

Resonance series frequency

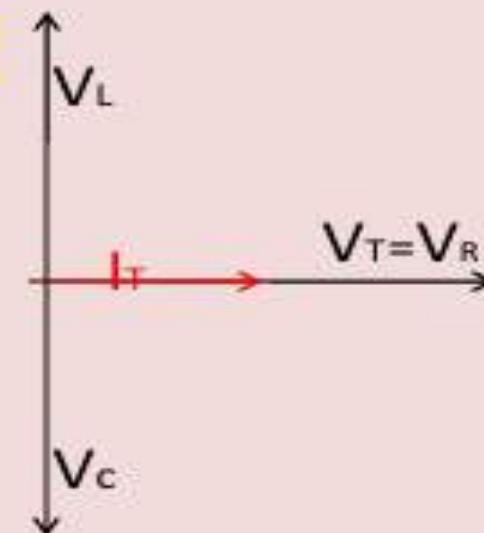
$$X_L = X_C \therefore 2\pi f_o L = (1/2\pi f_o C)$$

$$\therefore f_o^2 = (1/4\pi^2 L C)$$

$$f_r = f_o = 1/(2\pi\sqrt{L C}) \text{ Hz}$$

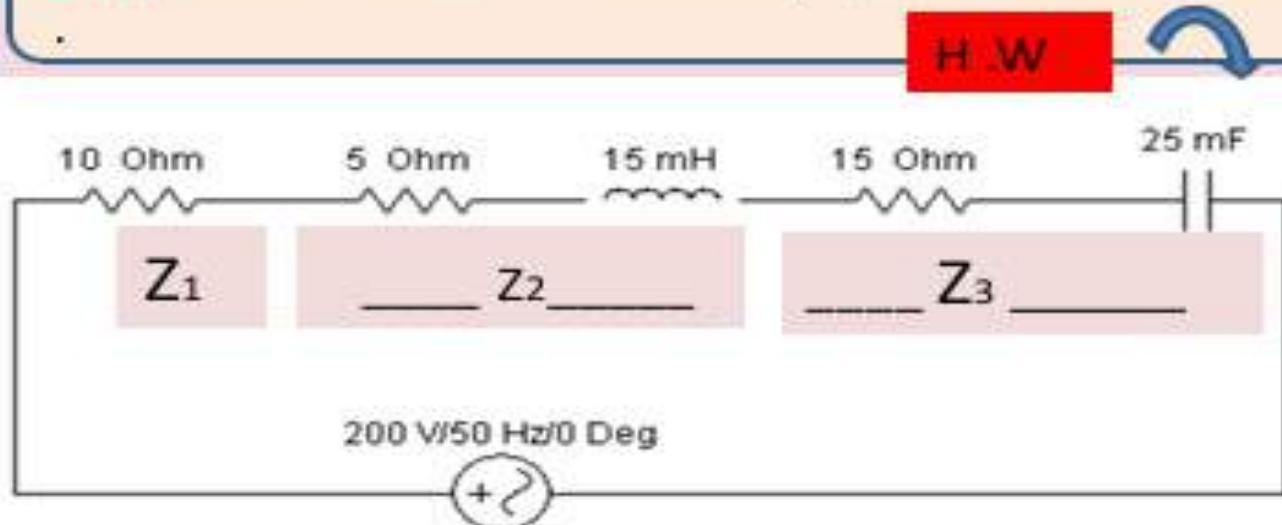
The energy stored in the coil(w,e)

$$W = (1/2) L I_m^2 \text{ joule}$$



## Post test

Ex(a) : For the cct. Shown Find ( $Z_T$ ,  $I$ ,  $\Theta$  ,  $V_{Z_1}$ ,  $V_{Z_2}$  ,  $V_{Z_3}$ )then draw the phaser diagram



H.W

$$Z_T = 31.6 \Omega,$$
$$I = 6.329 A$$

$$\Theta = 18.43^\circ$$

solution

$$V_{Z_1} = 63.29 V$$

$$V_{Z_2} = 99.998 V$$

$$V_{Z_3} = 184.49 V$$

Ex(b): For the cct. Shown Find:  $I$ ,  $\Theta$  ,  $V_R$ ,  $V_C$  ,  $V_L$  and draw the phaser diagram.

H.W



solution

$$I = 14 A$$

$$\Theta = 45.55^\circ$$

$$V_R = 140 V$$

$$V_C = 297 V$$

$$V_L = 439.81 V$$

الأسبوع العاشر

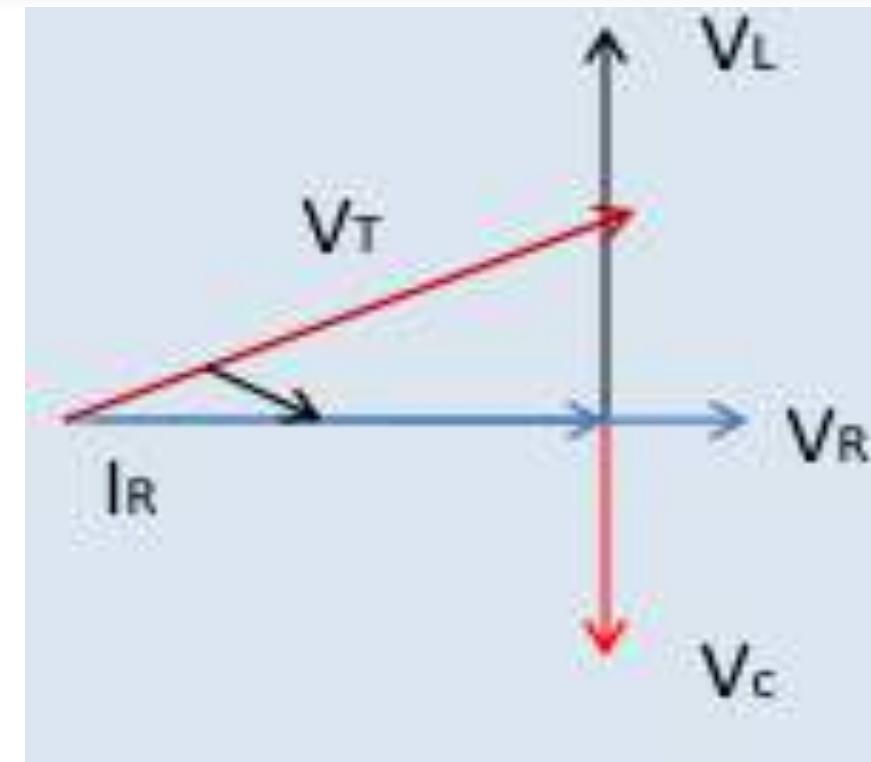
Effect of alternating current at  
parallel circuits

## :Aim of lecture

Aim of lecture : To make the student should be able to decipher complex electrical networks linking parallel and current knowledge of the relationship Balvoltaip in this case, and how to find a phase angle and the reluctance of the circle and permittivity

# pretest

Drawing the phase diagram for the cct contain  
(L,C)in series .If  $x_L > x_C$



## R-L in parallel

## في حالات التوازي

$$I_R = V/R, \quad I_L = V/X_L, \quad I_T = \sqrt{I_R^2 + I_L^2}$$

$$I_T = \sqrt{(V/R)^2 + (V/X_L)^2} = \sqrt{V^2 / R^2 + V^2 / X_L^2}$$

$$I_T = V \sqrt{1/R^2 + 1/X_L^2} = I/V = Y = \sqrt{1/R^2 + 1/X_L^2} \text{ (Moh)},$$

$1/\Omega$ , (Siemens) , (admittance of the cct.) ,  $Y = 1/Z$ ,  $Z = 1/Y$

$$\Theta = \tan^{-1} (-I_L / I_R)$$

**EX(1): for the cct. Shown find  $Y_T$ ,  $Z_T$ ,  $I_R$ ,  $I_L$ ,  $I_T$ ,  $\Theta$**

**Drawing the phaser diagram.**

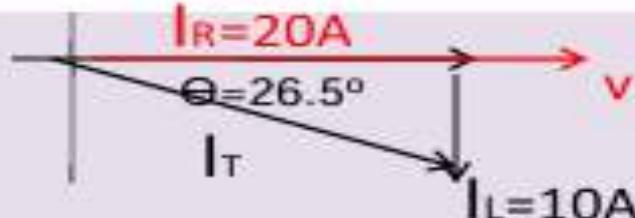
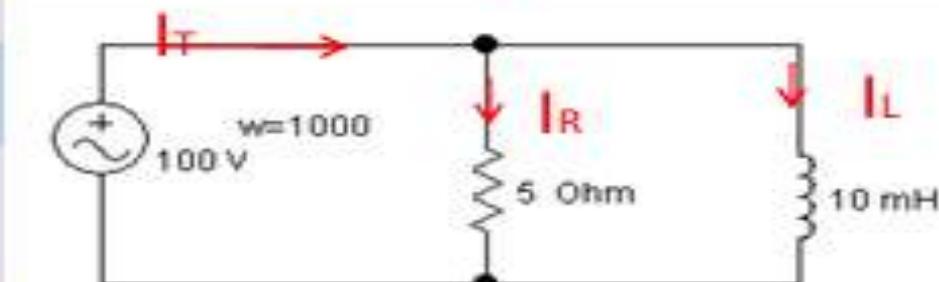
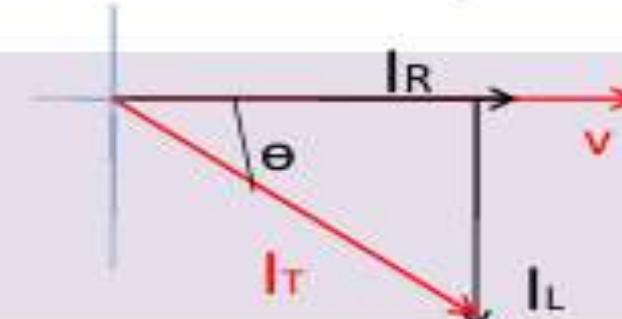
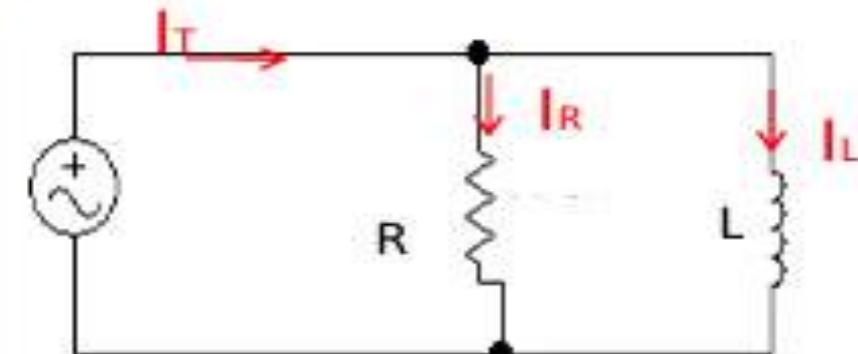
$$I_R = V/R = 100/5 = 20A, \quad I_L = V/X_L = 100/(1000 * 0.01)) = 10A$$

$$I_T = \sqrt{I_R^2 + I_L^2} = \sqrt{20^2 + 10^2} = 22A$$

$$\Theta = \tan^{-1} -I_L / I_R = \tan^{-1} (-10/20) = -26.5$$

$$Z_T = V/I_T = 100/22 = 4.545\Omega$$

$$Y_T = 1/Z_T = 0.22 \text{ moh}$$



## R-C in Parallel

$$I_R = V/R, I_C = V/X_C$$

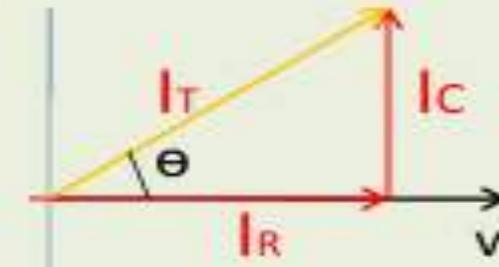
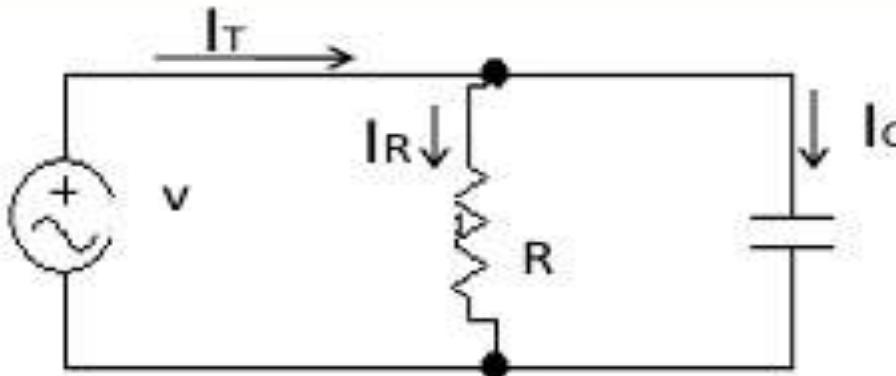
$$I_T = \sqrt{I_R^2 + I_C^2}$$

$$= \sqrt{(V/R)^2 + (V/X_C)^2}$$

$$I = \sqrt{\frac{1}{R^2} + \frac{1}{X_C^2}}$$

$$I/V = Y = \sqrt{\frac{1}{R^2} + \frac{1}{X_C^2}}$$

$$\Theta = \tan^{-1} (I_C / I_R)$$



**EX(2)** : for the cct. Shown find  $Y_T, Z_T, I_R, I_C, I_T, \Theta$   
Drawing the phaser diagram.

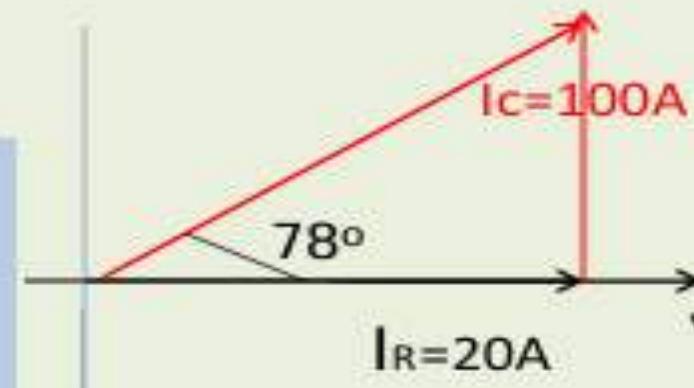
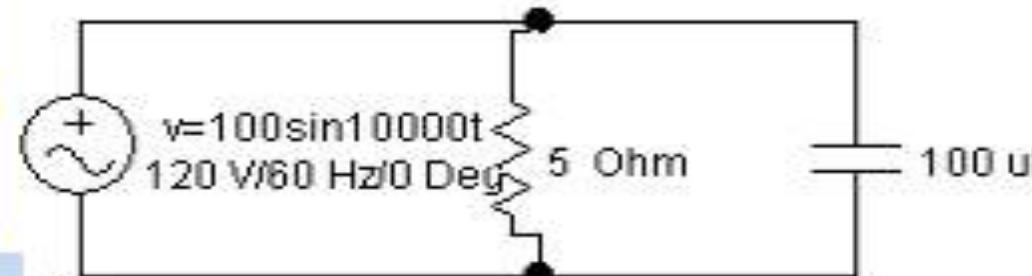
**Solution** :  $X_C = 1/\omega C = 1/(10000 \times 100 \times 10^{-6}) = 1\Omega$

$$Y = \sqrt{1/R^2 + 1/X_C^2} = \sqrt{1/52 + 1/12} = 1.01 \text{ mohm},$$

$$Z = 1/Y = 0.98 \Omega, \text{ or } Z = V/I = 100/101 = 0.98 \Omega, I_R = V/R = 100/5 = 20A$$

$$I_C = V/X_C = 100/1 = 100A, I_T = \sqrt{I_R^2 + I_C^2} = \sqrt{20^2 + 100^2} = 101A$$

$$\Theta = \tan^{-1} I_C/I_R = \tan^{-1} 5 = 78^\circ$$



## The general Parallel case

**1** If  $X_L > X_C \quad \therefore I_C > I_L \quad \therefore I_T = \sqrt{I_R^2 + (I_C - I_L)^2}$

$$Z_T = 1 / \sqrt{(1/R)^2 + (1/X_C - 1/X_L)^2} \quad \text{OR} \quad Z = V/I_T$$

$$\Theta = \tan^{-1} (I_C - I_L) / I_R$$

**2** If  $X_C > X_L \quad \therefore I_L > I_C \quad \therefore I_T = \sqrt{I_R^2 + (I_C - I_L)^2}$

$$Z_T = 1 / \sqrt{(1/R)^2 + (1/X_L - 1/X_C)^2} \quad \text{OR} \quad Z = V/I_T$$

$$\Theta = \tan^{-1} (I_C - I_L) / I_R$$

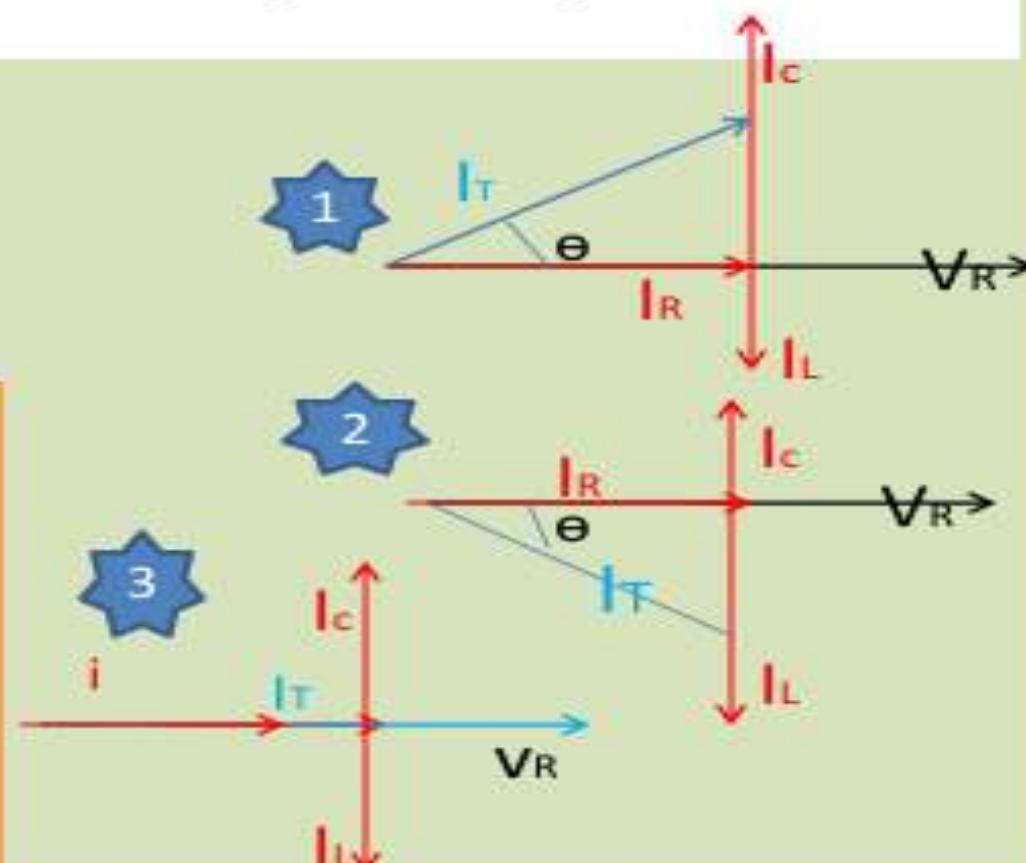
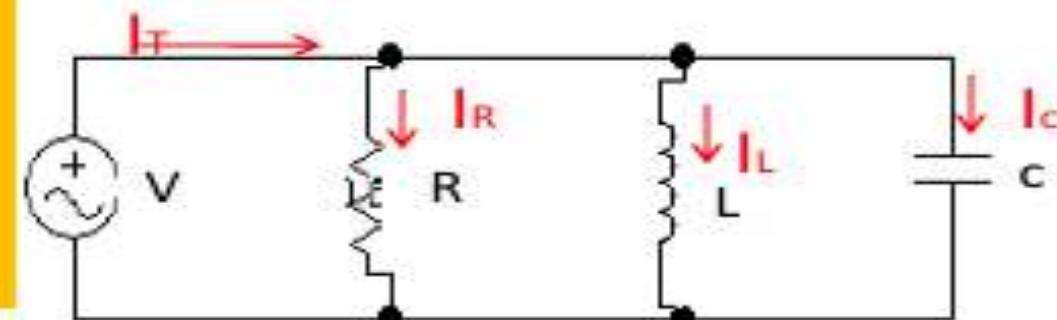
**3**

If  $X_C = X_L$  (Resonance Parallel case)  $\therefore I_C = I_L \quad \therefore I_T = I_R$

$$Z_T = 1 / \sqrt{(1/R)^2} \quad \therefore Z_T = R \quad , \quad V_T = I_T \cdot Z_T \quad , \quad \Theta = 0$$

$$f_r = 1 / 2\pi \sqrt{L \cdot C} \text{ HZ}$$

$f_r$ : (Resonance Parallel frequency)



### Example(3):

For the parallel cct. Shown in figer find : 1/ The total current 2/ phase angle  
3/ Impedance of the cct. 4/ phase diagram .

solution



$$I_R = V/R = 120/100 = 1.2 \text{ A} , X_C = 1/(2\pi f C) = 1/(2\pi \times 60 \times 25 \times 10^{-6})$$

$$\therefore X_C = 100 \Omega , I_C = V/X_C = 120/100 = 1.2 \text{ A} , X_L = 2\pi f L = 2\pi \times 60 \times 0.5$$

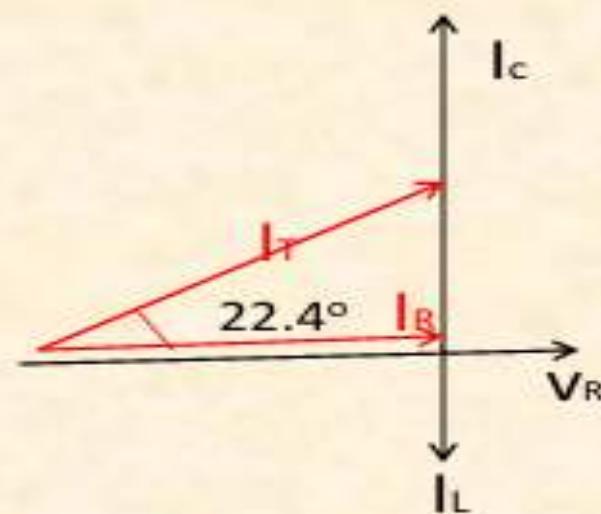
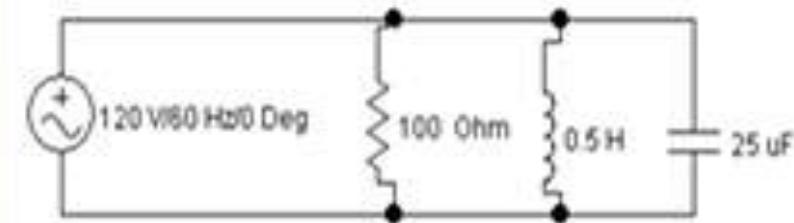
$$\therefore X_L = 188.4 \Omega , I_L = V/X_L = 120/188.4 = 0.63 \text{ A}$$

$$I_C - I_L = 1.2 - 0.63 = 0.57 \text{ A} \quad \therefore I_T = \sqrt{I_R^2 + (I_C - I_L)^2}$$

$$\therefore I_T = \sqrt{(1.2)^2 + (0.57)^2} \quad \therefore I_T = 1.3 \text{ A} ,$$

$$\theta = \tan^{-1} |I_C - I_L| / |I_R| = \tan^{-1} 0.57/1.2 = 22.4^\circ$$

$$Z = V/I_T = 120/1.3 = 92 \Omega$$



## Posttest

Ex: For the cct. Shown in figer find 1) the source current  $I_T$ .  
2) Active and reactive power and apparent power

### Solution

$$X_L = 2\pi f L = 2\pi \times 60 \times 0.5 = 188 \Omega$$

$$X_C = \frac{1}{2\pi f C} = \frac{1}{2\pi \times 60 \times 20 \times 10^{-6}} = 132.6 \Omega$$

$$Z_L = \sqrt{(100^2 + 188^2)} = 213 \Omega, \theta = \tan^{-1} 188/100 = 62^\circ$$

$$Z_L = 213 < 62^\circ \Omega, Z_C = 132.6 < -90^\circ$$

$$I_L = V/Z_L = 250/213 < 62^\circ = 1.17 < -62^\circ A$$

$$I_C = V/Z_C = 250/132.6 < -90^\circ = 1.88 < 90^\circ A, I_T = I_L + I_C$$

$$\therefore I_T = 1.88 < 90^\circ + 1.17 < -62^\circ$$

$$\therefore I \cos \theta = 1.17 \cos -62^\circ + 1.88 \cos 90^\circ = 0.423 A$$

$$I \sin \theta = 1.17 \sin -62^\circ + 1.88 \sin 90^\circ = 0.79 A$$

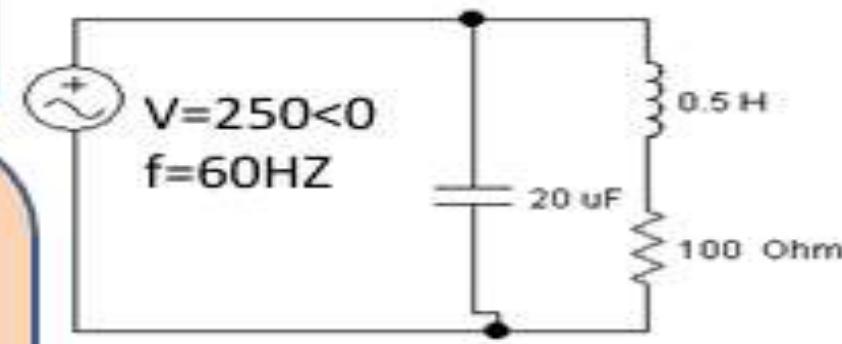
$$\therefore I_T = \sqrt{(0.423)^2 + (0.79)^2} = 0.896 A$$

$$\theta = \tan^{-1} 0.79 / 0.423 = 61.8^\circ \quad \therefore I = 0.896 < 61.8^\circ A$$

$$P = I \cdot V \cos \theta = 250 \times 0.896 \times \cos 61.8^\circ = 105.73 \text{ watt}$$

$$Q = I \cdot V \sin \theta = 250 \times 0.896 \times \sin 61.8^\circ = 197.4 \text{ var}$$

$$S = V \cdot I = 250 \times 0.896 = 224 \text{ V.A}$$



(Active power )

(Reactive power )

(Apparent power)

## References:

- 1- electrical technology (Edward Hughes)
- 2- Electrical technology (B.L THERAJA)
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(Fitzgerald Mc-Graw-Hill)
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# Thank you

