

**Ministry of high Education and Scientific Research  
Southern Technical University  
Technological institute of Basra  
Department of Electrical Techniques**



## **Learning package**

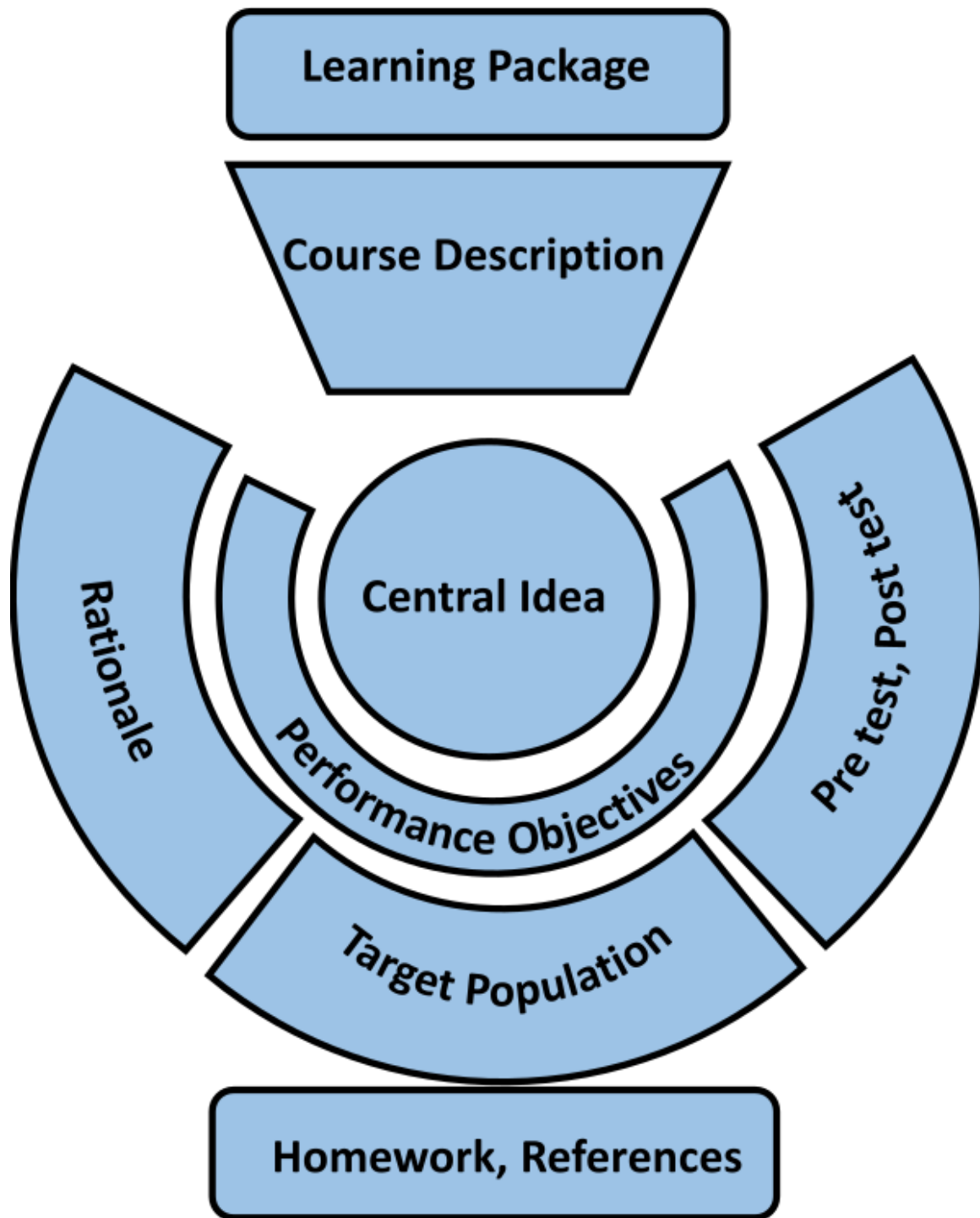
# **Power Electronics**

**For**

**Second year students**

**By**

**M.Sc. Humam Qahtan ALhassan  
Dep. Of Electrical Techniques  
2025**



Course Description

Course Name:	
Power Electronics Princeples	
Course Code:	
Semester / Year:	
Semester	
Description Preparation Date:	
14/ 05/ 2025	
Available Attendance Forms:	
Attendance only	
Number of Credit Hours (Total) / Number of Units (Total)	
60 hours/4 hour weekly/4 unit	
Course administrator's name (mention all, if more than one name)	
Name: Humam Qahtan	
Email: humam.alhasan@stu.edu.iq	
Course Objectives	
<ul style="list-style-type: none"> <li>❖ Differentiate between the general electronic circuits and power electronic devices.</li> <li>❖ Understand the main functions of power electronics: Power control and Power conversion.</li> <li>❖ Use the transistors for switching control.</li> <li>❖ Understand the various applications of UJT and op-amp circuits.</li> <li>❖ Learn the SCR structure, functions, circuits, and types.</li> <li>❖ Understand and differentiate between the different kinds of power conversion: AC-DC (rectifiers), DC-DC (choppers), DC-AC (invertors), AC-AC (convertors).</li> <li>❖ Connect the most important power electronic circuits in the Lab. and measure their parameters and characteristics.</li> </ul>	<ul style="list-style-type: none"> <li>• .....</li> <li>• .....</li> <li>• .....</li> </ul>

Teaching and Learning Strategies					
1. Cooperative Concept Planning Strategy.					
2. Brainstorming Teaching Strategy.					
3. Note-taking Sequence Strategy.					
Course Structure					
Weeks	Hours	Required Learning Outcomes	Unit or subject name	Learning method	Evaluation method
1	4hours	1- Differentiate between the general electronic circuits and power electronic devices. 2- Understand the main functions of power electronics: Power control and Power conversion. 3- Use the transistors for switching control. 4- Understand the various applications of UJT and op-amp circuits. 5-	Chapter 1: Power Electronic Devices Chapter 2: The Transistors Chapter 3: The Uni-Junction Transistor (UJT) Chapter 4: The Operational Amplifier (Op-Amp)	1.Conducting laboratory experiments to build and test digital circuits. This enhances theoretical understanding and develops practical skills.	Weekly, Monthly, Daily and Written Exams, and Final Term Exam.
2	4hours			2.Seeking feedback from instructors and peers to identify strengths and weaknesses	
3	4hours			3.Reviewing concepts periodical and applying them to new problems to reinforce memory and understanding.	
4	4hours			4.Using educational software an interactive applications to better understand concepts, s	
5	4hours			5.Encouraging self-research on r topics in electronics and explori	
6	4hours				
7	4hours				
8	4hours				
9	4hours				
10	4hours				
11	4hours				
12	4hours				
13	4hours				
14	4hours				
Course Evaluation					
Distribution as follows: 20 points for Midterm Theoretical Exams for the first semester, 20 points for Midterm Practical Exams for the first semester, 10 points for Daily Exams and Continuous Assessment, and 50 points for the Final Exam.					
Learning and Teaching Resources					

Required textbooks (curricular books, if any)	W.Shepherd,andL.Hulley, <b>PowerElectronicsandMotorControl</b> ,2ndedition,Camb ridgeUniversityPress,1996.
Main references (sources)	T.L. Floyd, <b>Electronic Devices</b> , 9th edition, Merrill Publishing Company, 1988.
Recommended books and references (scientific journals, reports...)	M.H.Rashid, <b>Power Electronics Handbook: Devices,CircuitsandApplications</b> ,2nd. AcademicPress:Elsevier,2007.
Electronic References, Websites	<a href="https://zlibrary-asia.se/">https://zlibrary-asia.se/</a>

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**In**  
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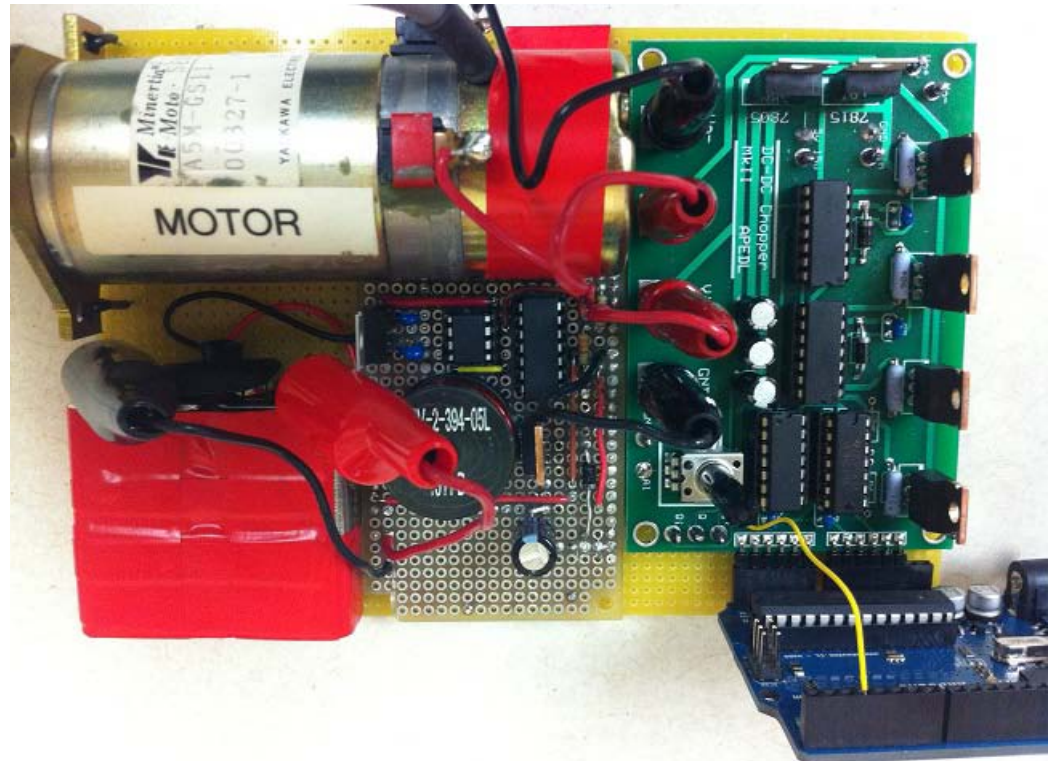
# **Chapter 1**

## **Power Electronic Devices**

# Introduction

## Power Electronic Devices:

Any device that can be used in the power processing circuits to convert or control the electric power.





# Classification of Power Electronic Devices

Uncontrolled device: diode  
(Uncontrollable device)

has only two terminals and can not be controlled by control signal.  
The on and off states of the device are determined by the power circuit.

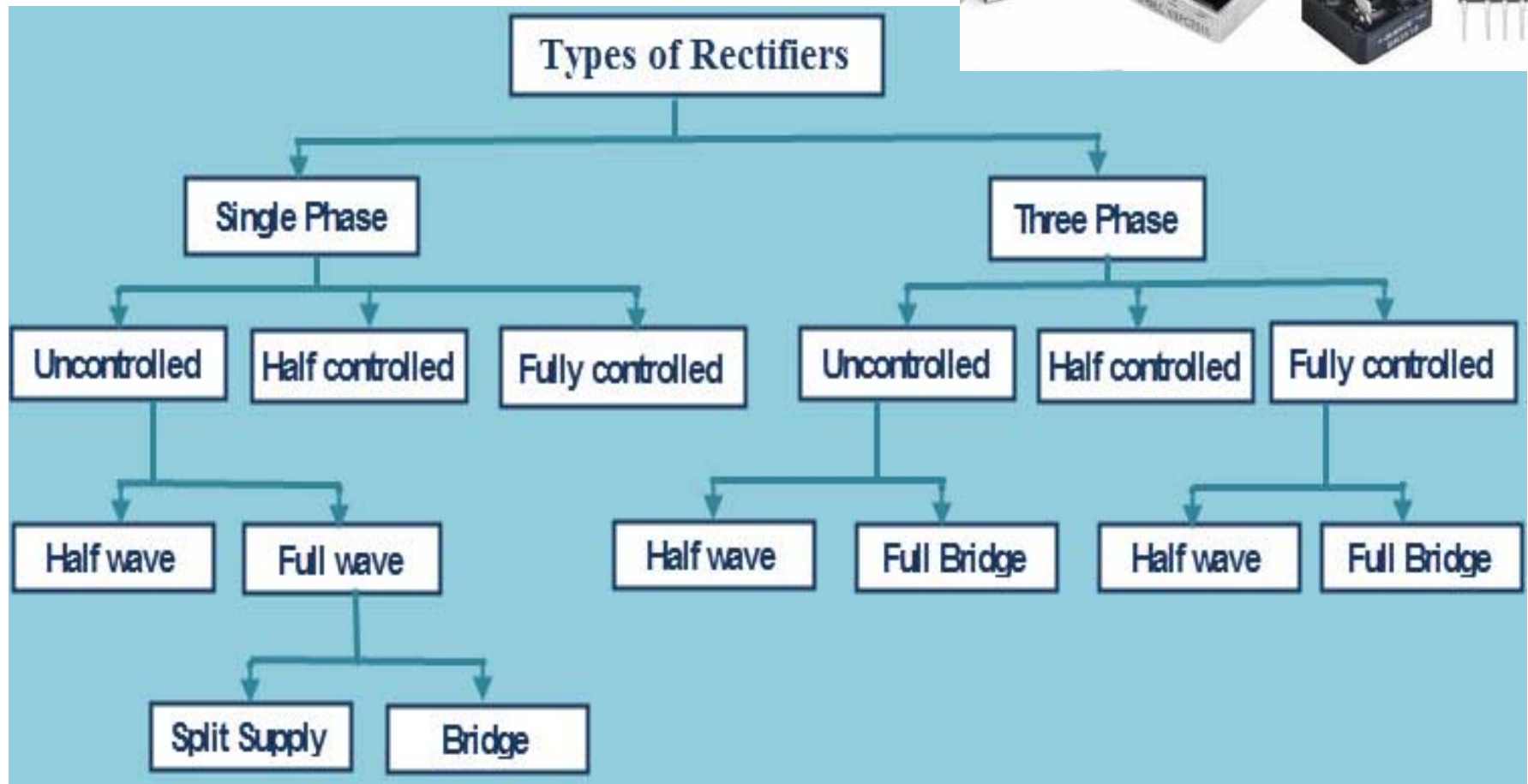
Half-controlled device: thyristor  
(Half-controllable device)

is turned-on by a control signal and turned-off by the power circuit

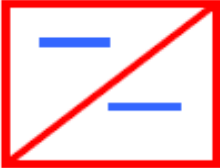
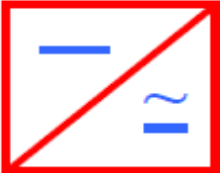
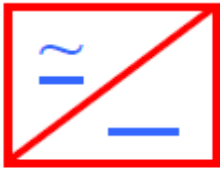
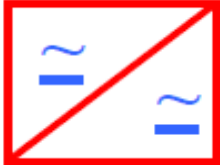
Fully-controlled device: Power MOSFET, IGBT, GTO, IGCT  
(Fully-controllable device)

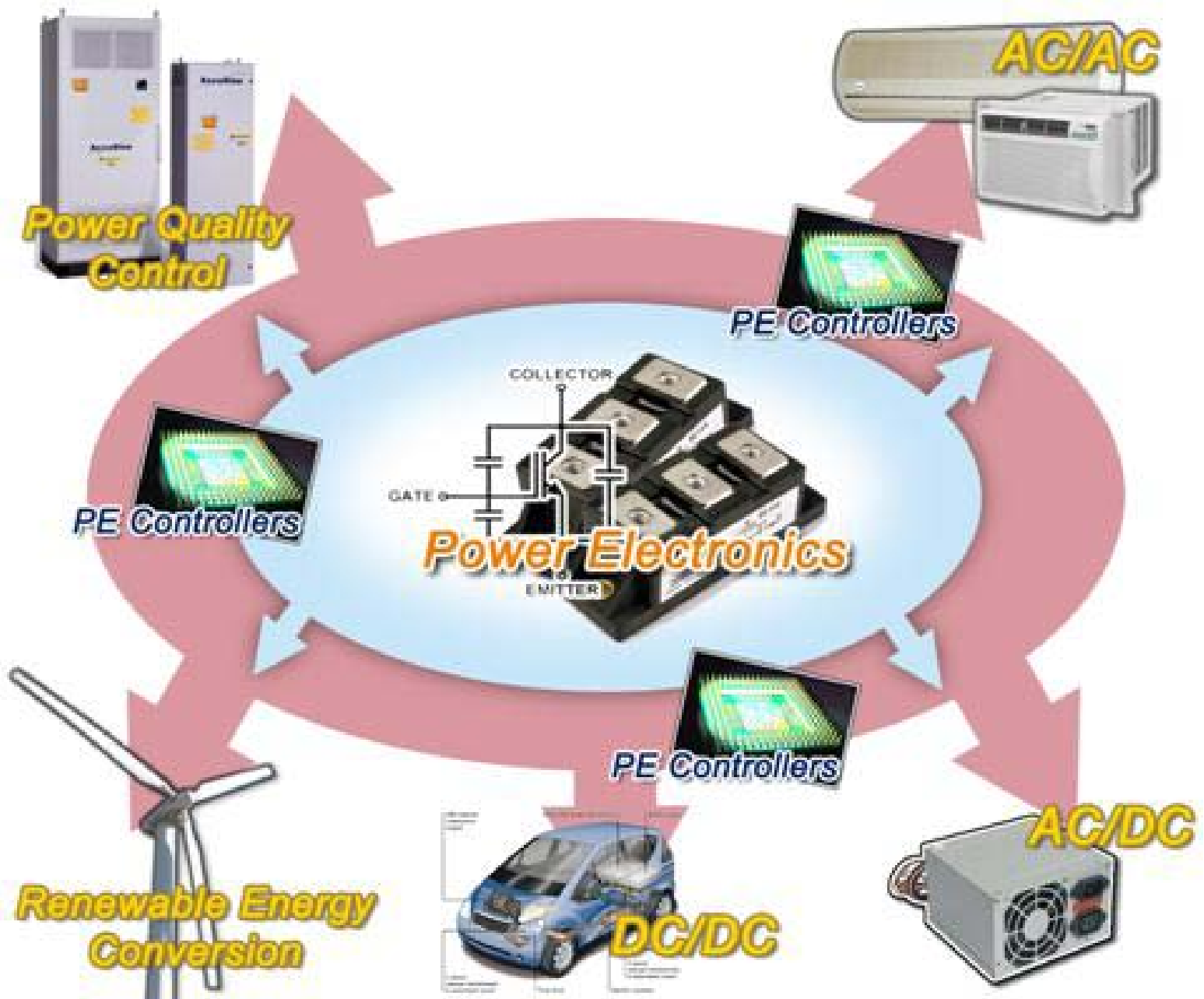
The on and off states of the device are controlled by control signals.

# Types of Rectifiers



# Power Conversion

CONVERSION FROM/TO	NAME	FUNCTION	SYMBOL
DC to DC	Chopper	Constant to variable DC or variable to constant DC	
DC to AC	Inverter	DC to AC of desired voltage and frequency	
AC to DC	Rectifier	AC to unipolar (DC) current	
AC to AC	AC controllers or AC Regulators	AC of desired frequency and/or magnitude from generally line AC	



# ***Diode Circuits (Uncontrolled Rectifiers)***

**Rectification:** The process of converting the alternating voltage to direct voltage.

## **Performance Parameters**

**Rectification Efficiency:**

$$\eta = P_{dc} / P_{ac}$$

**Form Factor:**

$$FF = V_{rms} / V_{dc}$$

**Ripple Factor:**

$$RF = \frac{V_{ac}}{V_{dc}} = \frac{\sqrt{V_{rms}^2 - V_{dc}^2}}{V_{dc}} = \sqrt{\frac{V_{rms}^2}{V_{dc}^2} - 1}$$
$$RF = \sqrt{FF^2 - 1}$$

## Three Phase Half-Wave Uncontrolled Rectifier ( $f_o = 3f_i$ )

$$V_{dc} = \frac{3\sqrt{3} V_m}{2\pi} = 0.827V_m$$

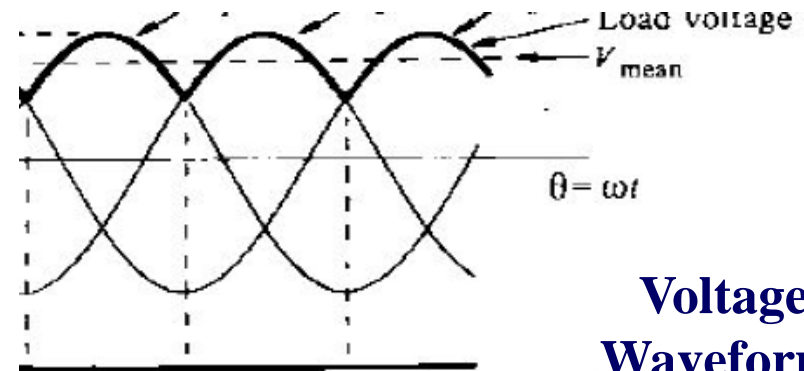
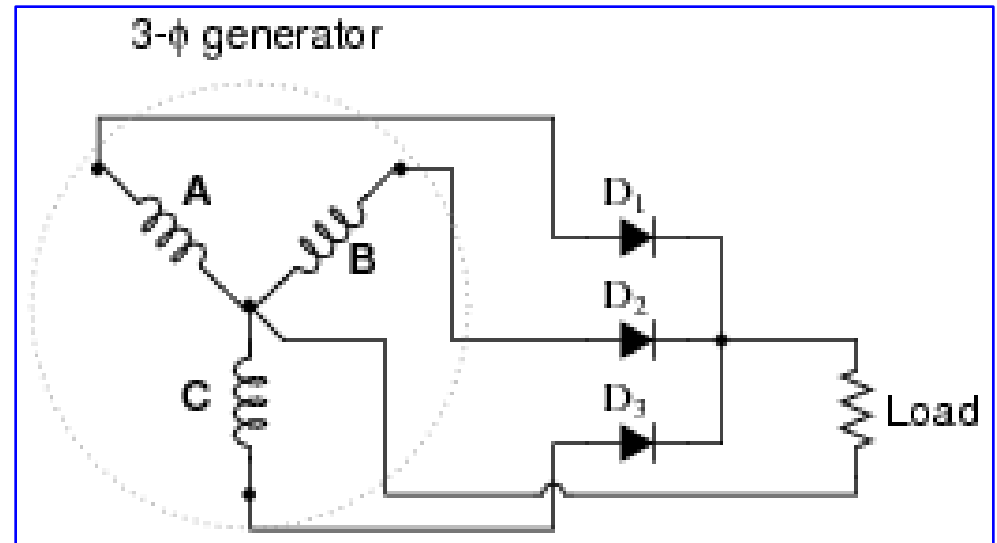
$$I_{dc} = \frac{3\sqrt{3} V_m}{2\pi R} = \frac{0.827V_m}{R}$$

$$V_{rms} = \sqrt{\frac{1}{2} + \frac{3\sqrt{3}}{8\pi}} V_m = 0.8407 V_m$$

$$I_{rms} = \frac{0.8407 V_m}{R}$$

$$I_r = I_s = \frac{0.8407 V_m}{R \sqrt{3}} = 0.4854 \frac{V_m}{R}$$

$$\text{Diode PIV} = \sqrt{2}V_{LL} = \sqrt{3} V_m$$



**Voltage Waveforms**

### Example 1

The rectifier shown above is operated from 460V/50 Hz supply at the secondary side and the load resistance is  $R = 20\Omega$ . If the source inductance is negligible, determine: (a) Rectification efficiency, (b) Form factor (c) Ripple factor (d) Peak inverse voltage (PIV) of each diode.

#### Solution:

$$V_s = \frac{460}{\sqrt{3}} = 265.58 \text{ Volt} \quad ; \quad V_m = 265.58 \times \sqrt{2} = 375.59 \text{ Volt}$$

$$V_{dc} = \frac{3\sqrt{3} V_m}{2\pi} = 0.827 V_m \quad ; \quad I_{dc} = \frac{3\sqrt{3} V_m}{2\pi R} = \frac{0.827 V_m}{R}$$

$$V_{rms} = 0.8407 V_m \quad ; \quad I_{rms} = \frac{0.8407 V_m}{R}$$

$$\Rightarrow \eta = \frac{P_{dc}}{P_{ac}} = \frac{V_{dc} I_{dc}}{V_{rms} I_{rms}} = 96.767 \%$$

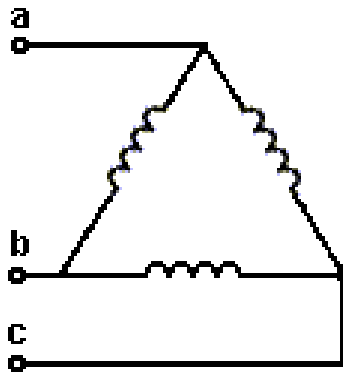
$$\Rightarrow FF = \frac{V_{rms}}{V_{dc}} = 101.657 \%$$

$$\Rightarrow RF = \frac{V_{ac}}{V_{dc}} = \frac{\sqrt{V_{rms}^2 - V_{dc}^2}}{V_{dc}} = \sqrt{\frac{V_{rms}^2}{V_{dc}^2} - 1} = \sqrt{FF^2 - 1} = 18.28 \%$$

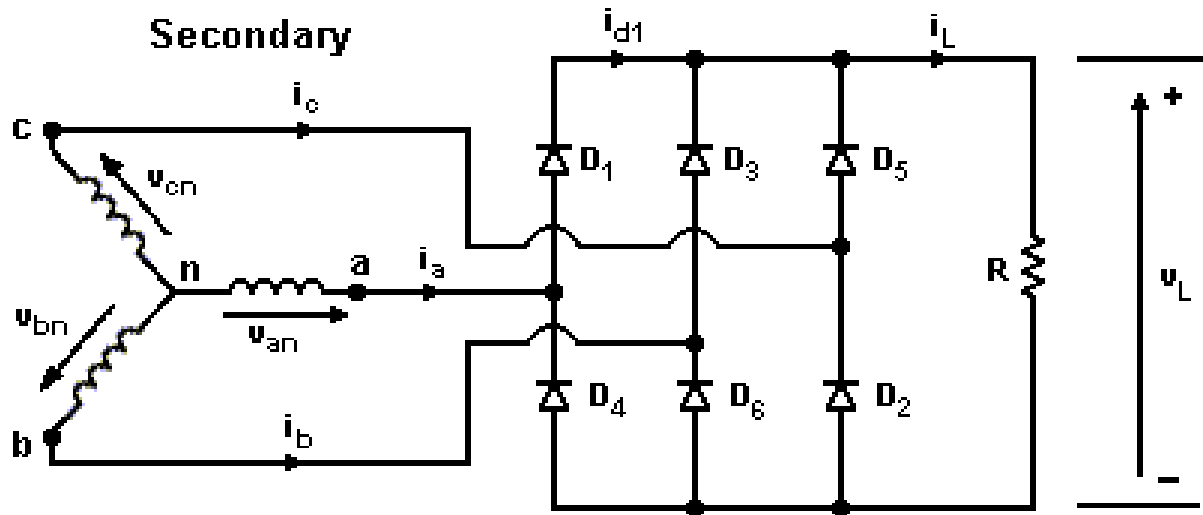
$$\Rightarrow PIV = \sqrt{3} V_m = 650.54 \text{ Volt}$$

# Three Phase Uncontrolled Bridge Rectifier ( $f_o = 6f_i$ )

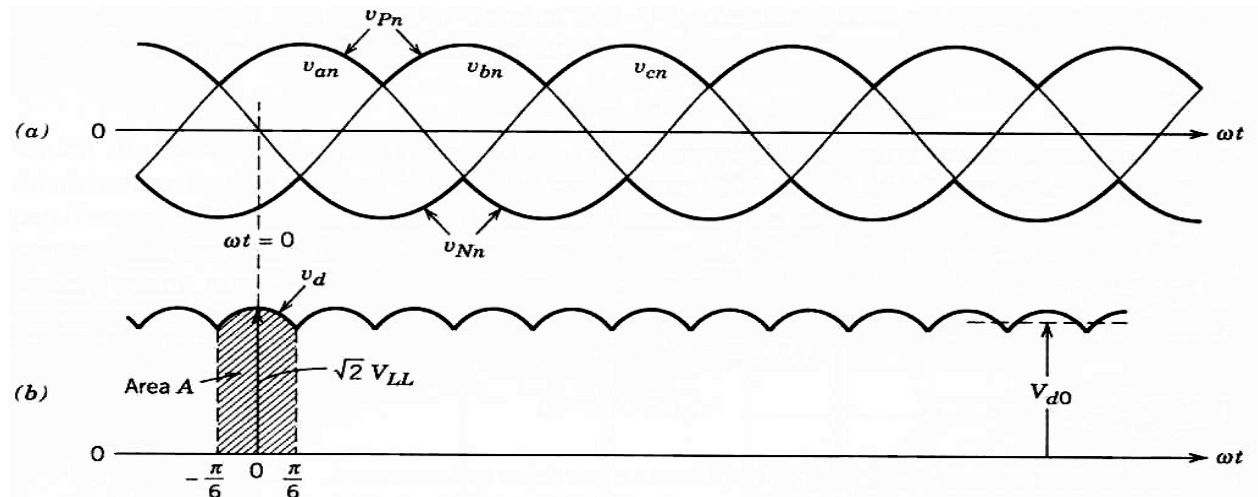
Primary



Secondary



Voltage  
Waveforms





## ***Three Phase Uncontrolled Bridge Rectifier ( $f_o = 6f_i$ )***

$$V_{dc} = \frac{3\sqrt{3} V_m}{\pi} = \frac{3\sqrt{2} V_{LL}}{\pi} = 1.654V_m = 1.3505V_{LL}$$

$$I_{dc} = \frac{V_{dc}}{R} = \frac{1.654V_m}{R} = \frac{1.3505V_{LL}}{R}$$

$$V_{rms} = \sqrt{\frac{3}{2} + \frac{9\sqrt{3}}{4\pi}} V_m = 1.6554 V_m = 1.3516V_{LL}$$

$$I_{rms} = \frac{1.6554 V_m}{R}$$

$$I_r = \frac{1.6554 V_m}{R\sqrt{3}} = 0.9667 \frac{V_m}{R}$$

$$I_s = 0.9667\sqrt{2} \frac{V_m}{R}$$

$$\text{Diode PIV} = \sqrt{2}V_{LL} = \sqrt{3} V_m$$

Where:

$V_s = 0.707 V_m$  is the rms voltage of transformer secondary;

$I_s = 0.7804 I_m$  is the rms current of one line transformer secondary;

$I_m$  = peak secondary line current.

**Example 2** 3 $\phi$  Bridge rectifier is operated from 460V/50 Hz supply and the load resistance is  $R = 20\Omega$ . If the source inductance is negligible, determine (a) The efficiency, (b) Form factor (c) Ripple factor (d) Peak inverse voltage (PIV) of each diode .

**Solution:**

$$V_s = \frac{460}{\sqrt{3}} = 265.58 \text{ Volt} \quad ; \quad V_m = 265.58 \times \sqrt{2} = 375.5 \text{ Volt}$$

$$V_{dc} = \frac{3\sqrt{3} V_m}{\pi} = 1.654 V_m = 621.2 \text{ Volt} \quad ; \quad I_{dc} = \frac{1.654 V_m}{R} = 31.0613 \text{ A}$$

$$V_{rms} = 1.6554 V_m = 621.75 \text{ Volt} \quad ; \quad I_{rms} = \frac{1.6554 V_m}{R} = 31.08 \text{ A}$$

$$\Rightarrow \eta = \frac{P_{dc}}{P_{ac}} = \frac{V_{dc} I_{dc}}{V_{rms} I_{rms}} = 99.83 \%$$

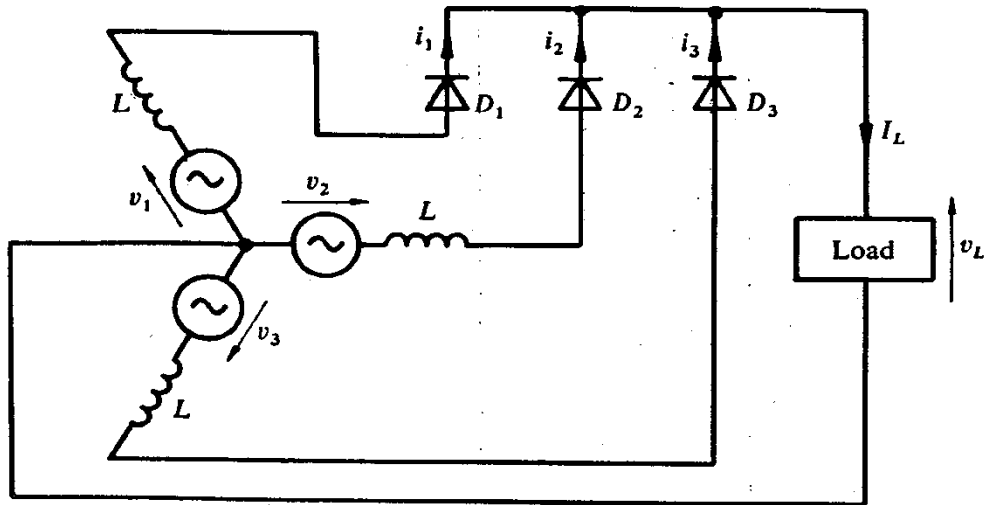
$$\Rightarrow FF = \frac{V_{rms}}{V_{dc}} = 100.08 \%$$

$$\Rightarrow RF = \frac{V_{ac}}{V_{dc}} = \frac{\sqrt{V_{rms}^2 - V_{dc}^2}}{V_{dc}} = \sqrt{\frac{V_{rms}^2}{V_{dc}^2} - 1} = \sqrt{FF^2 - 1} = 4 \%$$

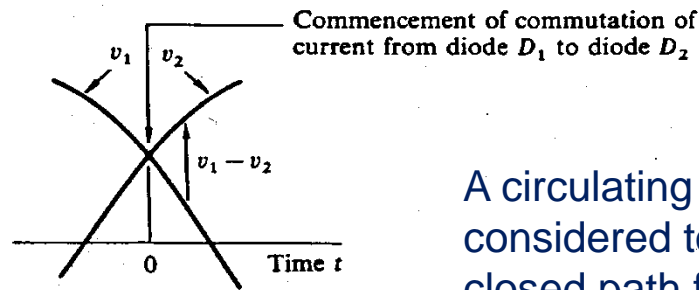
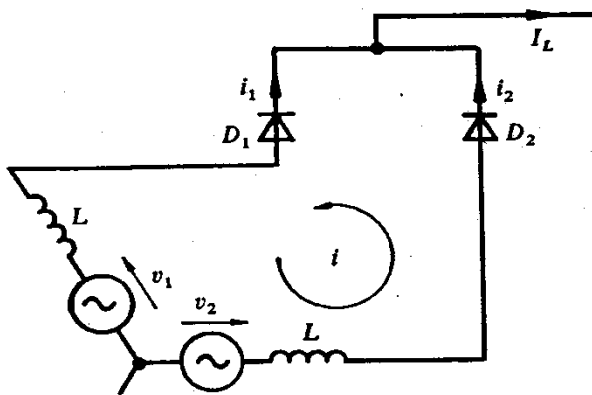
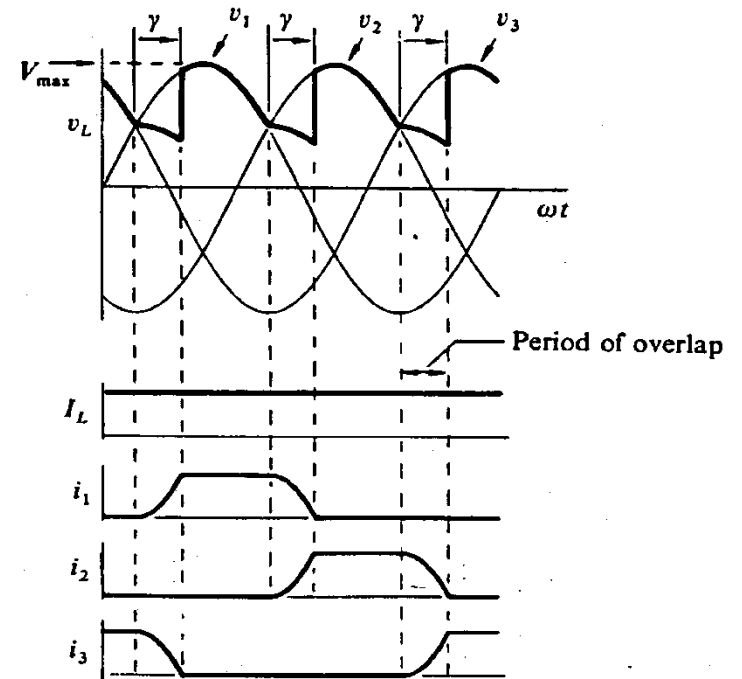
$$\Rightarrow PIV = \sqrt{3} V_m = 650.54 \text{ Volt}$$

# Overlap Phenomenon

- ❑ Overlap is the phenomenon due to the effect of source inductance on the AC side.
- ❑ Commutation current is delayed due to the source inductance which is normally the leakage reactance of a transformer (as  $X \gg R$  for a transformer, the source resistance is usually neglected).
- ❑ The waveforms with the commutation period, denoted by  $[\gamma]$  during which both the outgoing diode and incoming diode are conducting. This period is also known as “overlap” period.
- ❑ During the overlap period, the load current is the addition of the two diode currents, the assumption being made that the load is inductive enough to give a constant load current.
- ❑ The load voltage is the mean of the two conducting phases during overlap period.
- ❑ The effect of overlap is to reduce the mean output voltage.



(a)



A circulating current  $i$  can be considered to flow in the closed path formed by the 2 conducting diodes  $D_1$  and  $D_2$ .

The average output voltage due to overlap:

$$V_{dc} = \frac{1}{2\pi/3} \left[ \int_{\frac{\pi}{6} + \gamma}^{\frac{5\pi}{6}} V_m \sin \theta d\theta + \int_0^{\gamma} V_m \sin \frac{\pi}{6} \cos \phi d\phi \right] = \frac{3\sqrt{3}}{4\pi} V_m (1 + \cos \gamma)$$

$$V_{dc} = \frac{3\sqrt{3}}{4\pi} V_m (1 + \cos \gamma)$$

**OR**

$V_{dc} = V_{dc}$  without overlap - reduction of  $V_{dc}$  due to overlap.

$$V_{dc} \text{ without overlap} = \frac{1}{2\pi/3} \int_{\pi/6}^{5\pi/6} V_m \sin \omega t d\omega t = \frac{3\sqrt{3} V_m}{2\pi}$$

### Example 3

A three-phase half-wave rectifier circuit is supplied from a [120/208] V, 3phase, 60 Hz source. Determine: 1) the average DC output voltage of the rectifier, 2) the conduction angle  $\theta_C$ , 3) output frequency  $f_o$ .

#### Solution:

$$V_{ph} = \frac{208}{\sqrt{3}} = 120.2 \text{ Volt} ; V_{peak} = V_m = \sqrt{2} V_{ph} = 170 \text{ Volt}$$

$$1) V_{dc} = 3 \sqrt{3} \times \frac{V_m}{2\pi} = 140.3 \text{ Volt} ; 2) \theta_C = \omega t_C = 2\pi f_i \times \left( \frac{1}{3f_i} \right) = \frac{2\pi}{3} = 120^\circ$$

$$3) f_o = 3f_i = 3 \times 60 = 180\text{Hz}$$

### Example 4

3 $\phi$  – Half-Wave rectifier with  $\Delta$ -Y transformer is connected to 100 $\Omega$  resistive load. For 220V secondary line to line voltage and 50Hz supply frequency. Calculate: 1) The dc load power, 2) The conduction time of each diode, 3) If the input transformer has leakage reactance which causes an overlap angle of 20°, calculate  $V_{dc}$ .

#### Solution:

$$1) V_{dc} = 0.827 V_m = 0.827 \times \sqrt{2} V_{ph} = 0.827 \times \sqrt{2} \frac{220}{\sqrt{3}} = 149 \text{ Volt}$$

$$\Rightarrow P_{dc} = \frac{V_{dc}^2}{R} = \frac{(149)^2}{100} = 222 \text{ W}$$

$$2) \theta_C = \omega t_C \Rightarrow t_C = \frac{\theta_C}{\omega} = \frac{2\pi/3}{2\pi f_i} = 6.67 \text{ m sec OR } t_C = \frac{1}{f_o} = \frac{1}{3f_i}$$

$$3) \text{ Due to overlap: } V_{dc} = 3\sqrt{3} \frac{V_m}{4\pi} (1 + \cos 20) = 144.1 \text{ Volt}$$

# Problems and Solutions

## Question 1

A three-phase half-wave rectifier circuit is supplied from a [220/380] V, 3phase, 60 Hz source. Determine : 1) The average DC output voltage of the rectifier, 2) The conduction time of each diode, 3) If there is an overlap phenomenon of  $30^\circ$ , find  $V_{dc}$  and the reduction of  $V_{dc}$  due to overlap.

### Solution:

$$V_m = 380 \times \frac{\sqrt{2}}{\sqrt{3}} = 311 \text{ Volt}$$

$$1) V_{dc} = 0.827V_m = 0.827 \times 311 = 212 \text{ Volt}$$

$$2) \theta_c = \omega t_c \Rightarrow t_c = \frac{\theta_c}{\omega} = \frac{1}{f_o} = \frac{1}{3f_i} = \frac{1}{3 \times 60} = 5.56 \text{ msec}$$

$$3) \text{ For an overlap angle of } 30^\circ \Rightarrow V_{dc} = 3\sqrt{3} \frac{V_m}{4\pi} (1 + \cos \gamma)$$

$$\therefore V_{dc} = 3\sqrt{3} \frac{311}{4\pi} (1 + \cos 30^\circ) = 198.2 \text{ Volt}$$

$$\therefore \text{ the reduction in } V_{dc} = V_{dc} \text{ without overlap} - V_{dc} \text{ with overlap}$$

$$V_{dc} = 212 - 198.2 = 13.8 \text{ Volt}$$

## Question 2

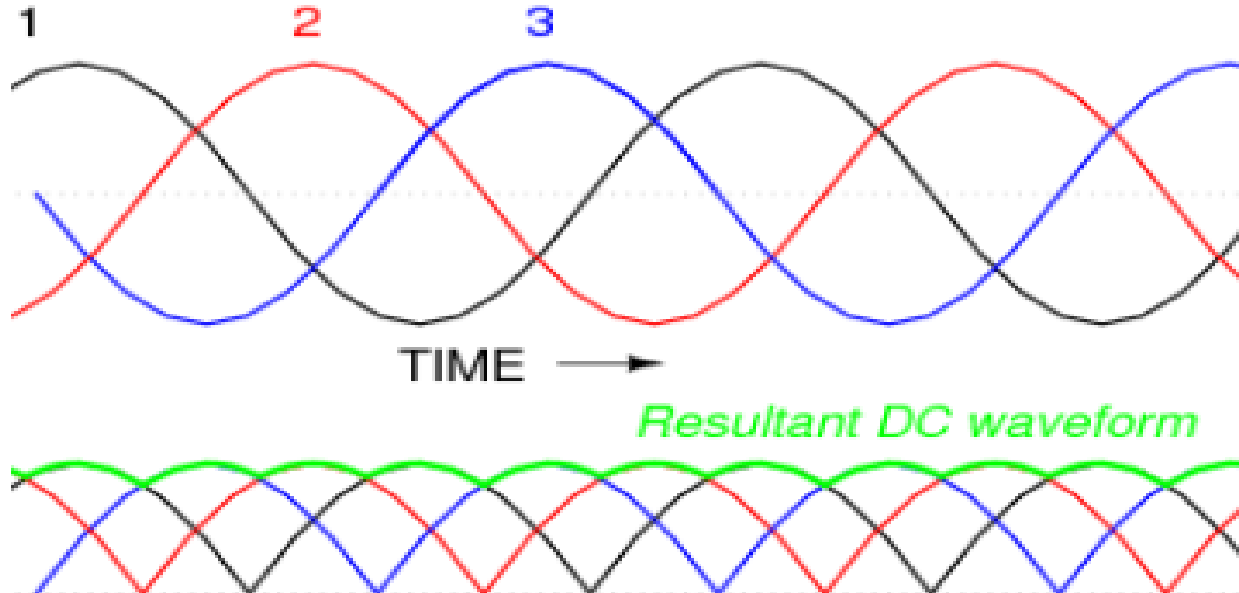
A three-phase Bridge rectifier is supplied from a [220/120] V, 3phase, 60 Hz source. 1) Determine the average DC output voltage of the rectifier, 2) Sketch the load voltage and supply current waveforms.

### Solution:

$$V_m = 120 \times \frac{\sqrt{2}}{\sqrt{3}} = 97.97 \text{ Volt}$$

$$1) V_{dc} = 1.654 V_m = 1.654 \times 97.97 = 162 \text{ Volt}$$

2) Load voltage and supply waveforms as below:





### Question 3

3 $\phi$ -Bridge rectifier with  $\Delta$ -Y transformer and [1200w, 3 $\Omega$ ] resistive load. Find :  
1) The secondary line voltage, 2) The Form Factor, and 3) The efficiency of rectification.

#### Solution:

$$1) P_{dc} = \frac{V_{dc}^2}{R} \Rightarrow V_{dc} = 3 \times \sqrt{1200} = 60 \text{ Volt}$$

$$V_{dc} = 1.654V_m \Rightarrow V_m = \frac{60}{1.654} = 36.27 \text{ Volt}$$

$$V_{line} = \frac{\sqrt{3} V_m}{\sqrt{2}} = 44.26 \text{ Volt}$$

$$2) V_{rms} = 1.6554V_m = 60.041 \text{ Volt}$$

$$FF = \frac{V_{rms}}{V_{dc}} = \frac{1.6554V_m}{1.654V_m} = 100.8\%$$

$$3) I_{dc} = \frac{V_{dc}}{R} = \frac{60}{3} = 20 \text{ A}$$

$$I_{rms} = \frac{V_{rms}}{R} = \frac{60.041}{3} = 20.014 \text{ A}$$

$$\eta = \frac{P_{dc}}{P_{ac}} = \frac{V_{dc} I_{dc}}{V_{rms} I_{rms}} = \frac{1200}{60.041 \times 20.014} = 99.86 \%$$

**Question 4** 3 $\phi$  – Half-Wave rectifier with  $\Delta$ -Y transformer and [250w, 5A] resistive load. Find the value of the secondary line voltage.

**Solution:**

$$P_{dc} = V_{dc} \times I_{dc} = 250\text{W} \Rightarrow V_{dc} = 250 / 5 = 50\text{V} = 0.827V_m$$

$$\Rightarrow V_m = 60.5\text{V} ; V_{ph} = V_m / \sqrt{2} = 42.79\text{V} ; V_{line} = \sqrt{3}V_{ph} = 74\text{V}$$

**Question 5** 3 $\phi$  – Bridge rectifier with  $\Delta$ -Y transformer is connected to 100 $\Omega$  resistive load. For 220V secondary line to line voltage and 50Hz supply frequency, calculate: 1) The dc load power, 2) The conduction time.

**Solution:**

$$V_{dc} = 1.654V_m = 1.654 \times \sqrt{2} \times 220 / \sqrt{3} = 297\text{V} \Rightarrow P_{dc} = V_{dc}^2 / R = (297)^2 / 100 = 883\text{W}$$

$$t_c = \theta_c / \omega = 1 / f_o = 1 / 6f_i = 1 / (6 \times 50) = 3.33\text{msec}$$

**Question 6** 3 $\phi$  – Bridge rectifier with  $\Delta$ -Y transformer and [250w, 5A] resistive load. Find the value of secondary line voltage  $V_{ab}$ .

**Solution:**

$$P_{dc} = V_{dc} \times I_{dc} = 250\text{W} \Rightarrow V_{dc} = 250 / 5 = 50\text{V} = 1.654V_m$$

$$\Rightarrow V_m = 52.3\text{V} ; V_{ph} = V_m / \sqrt{2} = 36.98\text{V} ; V_{line} = \sqrt{3}V_{ph} = 64\text{V}$$

**Question 7** Choose the correct or best alternative in the following:

- 1) Power electronics is the application of.....for the control and conversion of electric power.  
A. Conductors                      B. Transformer      C. Inductive load                      **D.** solid-state electronics
- 2) Most power semiconductor devices are only used in .....  
**A.**commutation mode    B. Rectification mode    C. Amplification mode    D. Non of the above
- 3) The three phase half-wave rectifier with resistive has an average value = .....  
A.  $0.87 V_{ph}$                       **B.**  $1.17 V_{ph}$                       C.  $1.41 V_{ph}$                       D.  $1.99 V_{ph}$
- 4) When voltage applied to a diode is more than PIV, it is likely to result in.....  
A. More distortion on output side      B. Poor regulation      C. Conduction in both direction  
**D.** Breakdown at the junction.
- 5) The ripple factor of a full-wave rectifier compared to half wave rectifier is .....  
A. half that of half -wave rectifier      **B.** less than half that of half-wave rectifier  
C. equal to that of half -wave rectifier      D. none of the above.
- 6) Switched mode power supplies are preferred over the continuous types, because they are.....and.....  
A. suitable for use in both ac and dc      **B.** more efficient      **C.** suitable for low-power circuits.  
D. suitable for high-power circuits.
- 12) Electric current is the flow of .....  
A. Neutrons                      B. Photons                      **C.** Electrons                      D. none of the above

## **Question 8**      **Fill in the blanks with the appropriate words**

- 1) In a rectifier, electrical power flows from the.....side to the.....side.
- 2) Uncontrolled rectifiers employ.....whereas controlled rectifiers employ.....
- 3) For any waveform “Form factor” is always.....than or equal to unity.
- 4) Three phase half-wave uncontrolled rectifier uses..... diodes .
- 5) Three phase half-wave uncontrolled rectifier requires..... phase..... wire power supply .

**Answers:**

- 1) ac, dc
- 2) diodes, thyristors
- 3) greater
- 4) three
- 5) three , four

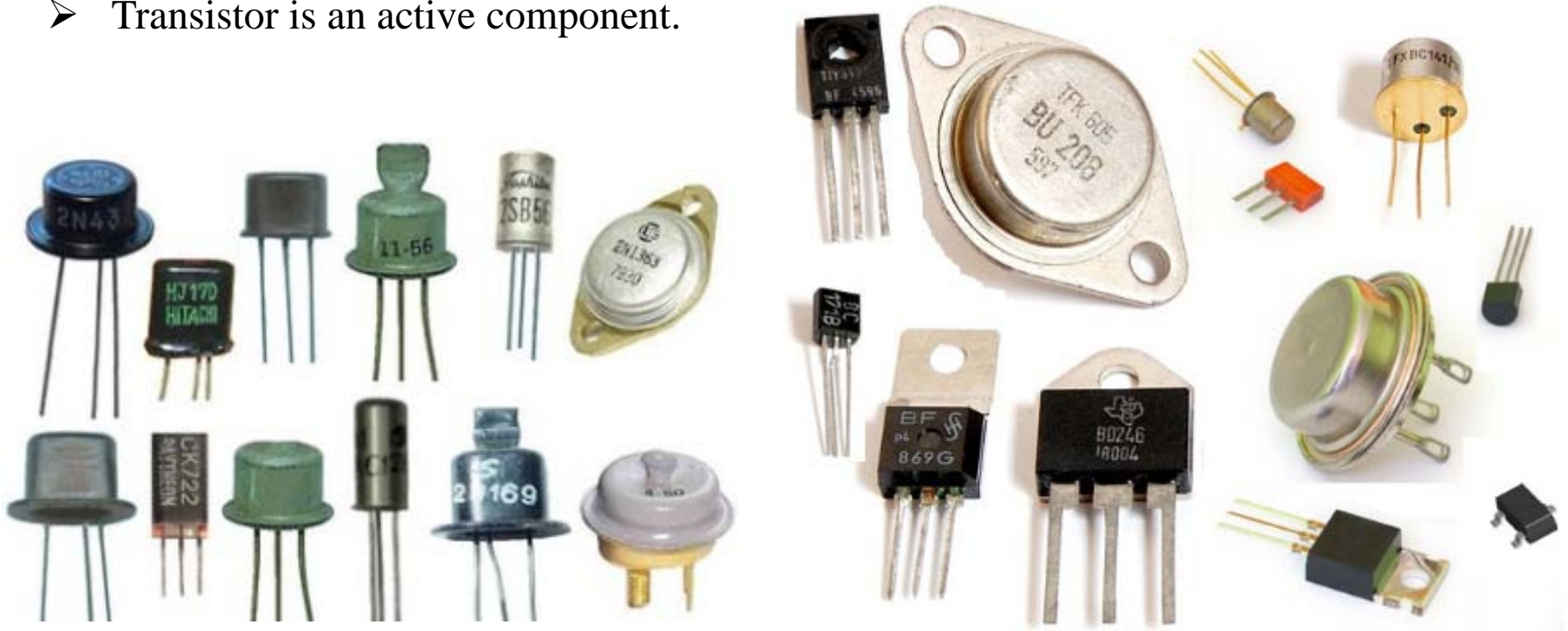
# **Chapter 2**

## **The Transistors**

# The Transistor

**Transistor:** It is a three-terminal, solid-state semiconductor device used to control the electric current or voltage between two of the terminals by applying an electric current or voltage to the third terminal.

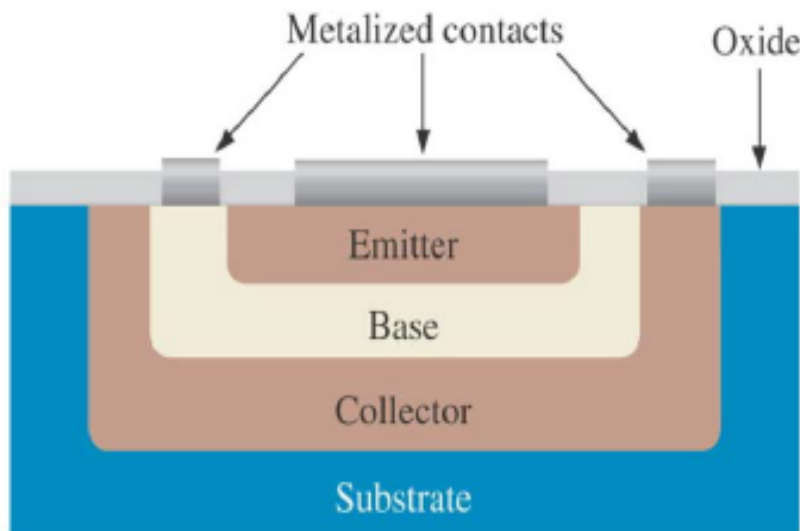
- Transistor is an active component.



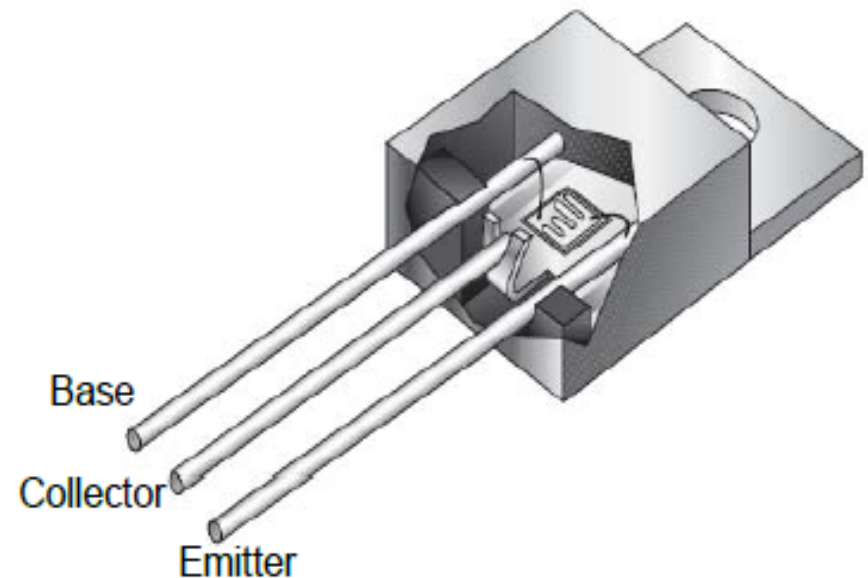
## Examples of Different Transistors Packages

# Bipolar Junction Transistor (BJT)

- It is constructed with *three* doped semiconductor regions separated by two PN junctions.
- The three regions are called **emitter**, **base**, and **collector**.
- The base is lightly doped and very narrow compared with the heavily doped emitter and moderately doped collector.
- It is used as an electrical signal amplifier or an electronic switch.
- Bipolar: refers to the use of both holes and electrons as current carriers.



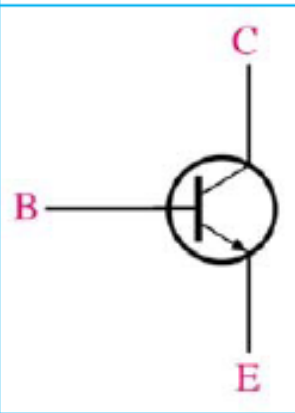
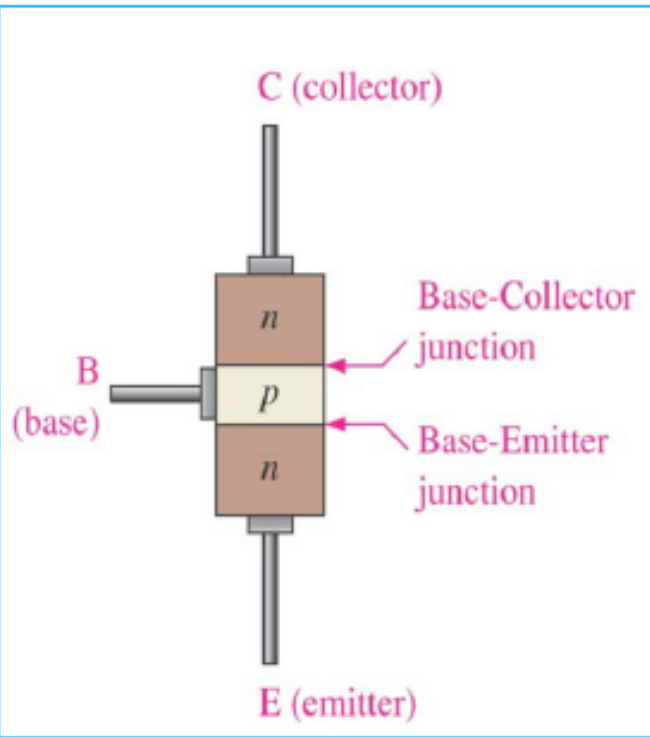
**Basic BJT construction**



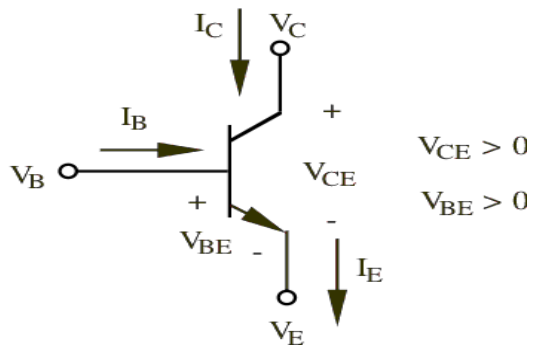
**BJT package Example**

# Types of BJTs

**npn**



*npn Symbol*



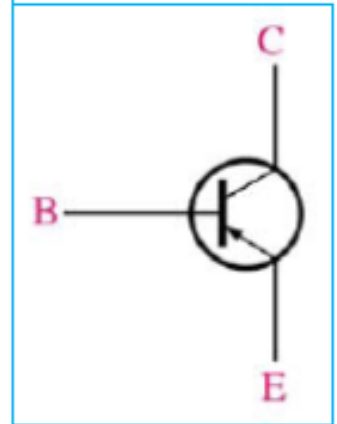
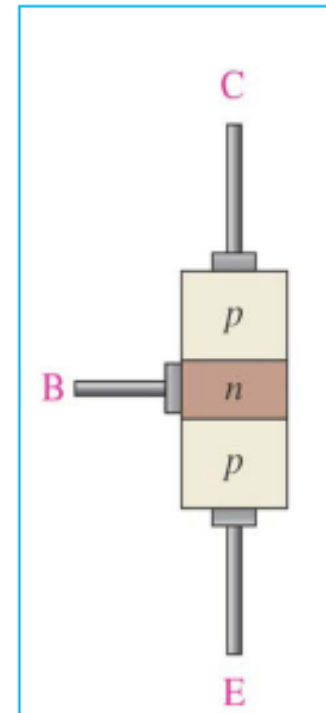
$$V_{BE} \approx 0.7 \text{ V}$$

$$I_E = I_C + I_B$$

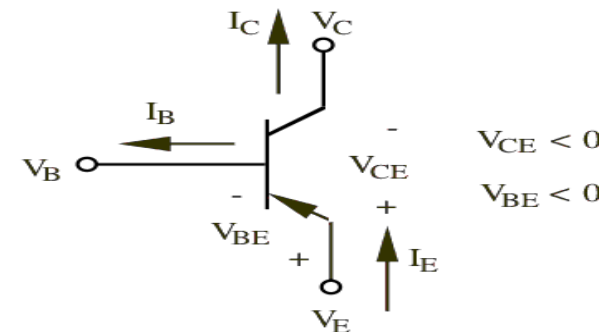
$$V_{BE} = V_B - V_E$$

$$V_{CE} = V_C - V_E$$

**pnp**

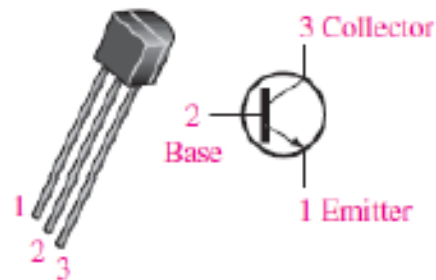


*pnp Symbol*

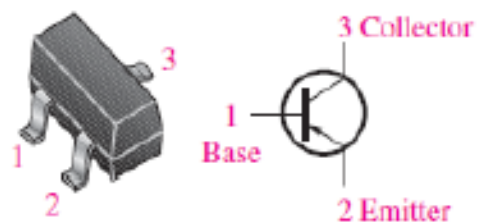




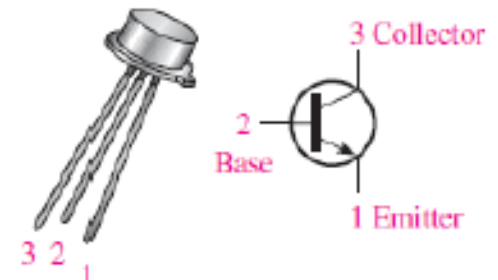
## Examples of BJTs



(a) TO-92

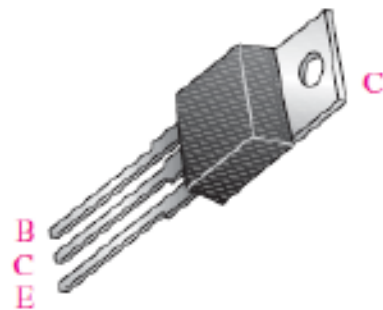


(b) SOT-23

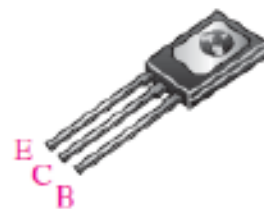


(c) TO-18. Emitter is closest to tab.

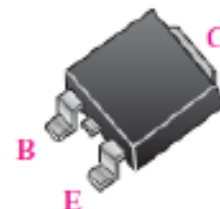
## General-purpose/small-signal transistors



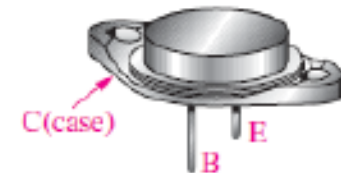
(a) TO-220



(b) TO-225



(c) D-Pack



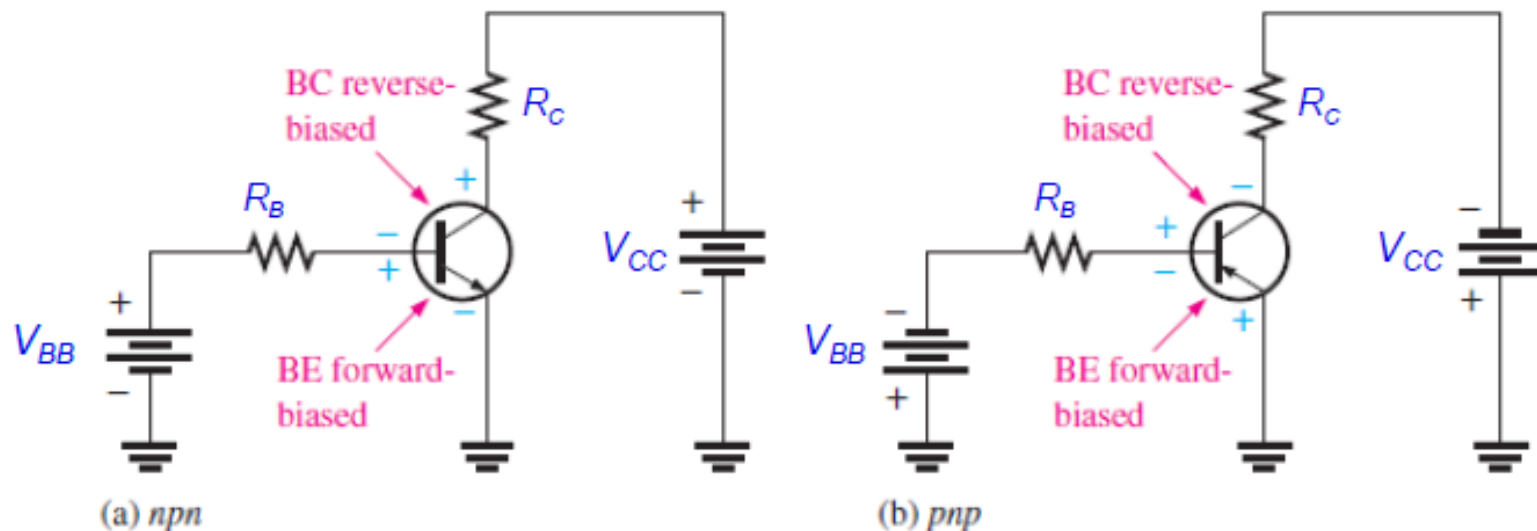
(d) TO-3

## Power transistors

## Common Emitter BJT Circuit

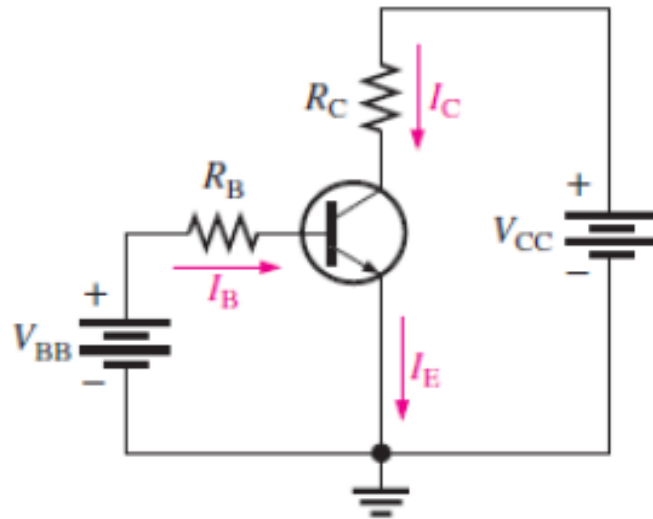
- In order for a **BJT** to operate properly as an amplifier, the two **pn** junctions must be correctly biased with external **dc** voltages.
- The operation of **pnp** is similar to the **npn** except that the roles of electrons and holes, bias voltage polarities, and current directions are all reversed.

### Forward-Reverse Bias for BJT Operation as an amplifier

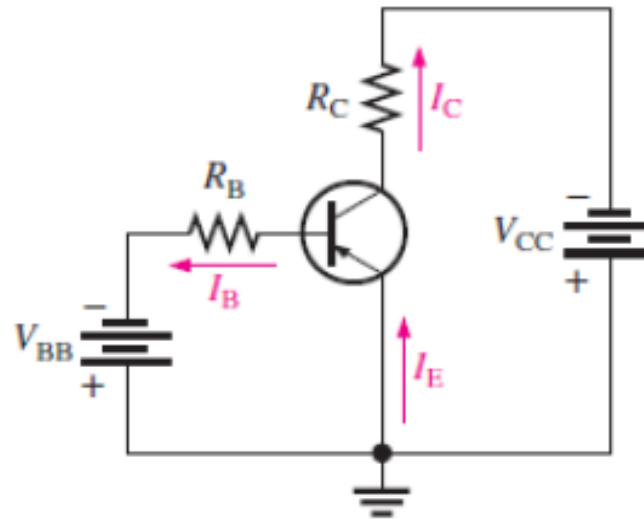


- The BE junction in both cases is forward-biased .
- The BC junction in both cases is reversed-biased.

## BJT Currents



(a) *nnp*



(b) *pnp*

For Conventional current direction (holes current) we have:

$$I_E = I_B + I_C$$

$I_B$  is very small due to light doping

$$I_E \simeq I_C$$

*Collector current is much greater than base current and hence the current gain*

## BJT Parameters

### DC Beta ( $\beta_{DC}$ ) and DC Alpha ( $\alpha_{DC}$ )

- The dc current gain of a transistor ( $\beta_{DC}$ ) is the ratio of dc collector current ( $I_C$ ) to the dc base current ( $I_B$ ).

$$\beta_{DC} = \frac{I_C}{I_B}$$

*Typical values of  $\beta_{DC}$   
from less than 20 to 200 or higher.*

- In data sheets, the hybrid  $h$ -parameters are used for transistors where  $h_{FE} = \beta_{DC}$ .
- $\alpha_{DC}$  is the ratio of dc collector current ( $I_C$ ) to the dc emitter current ( $I_E$ ).

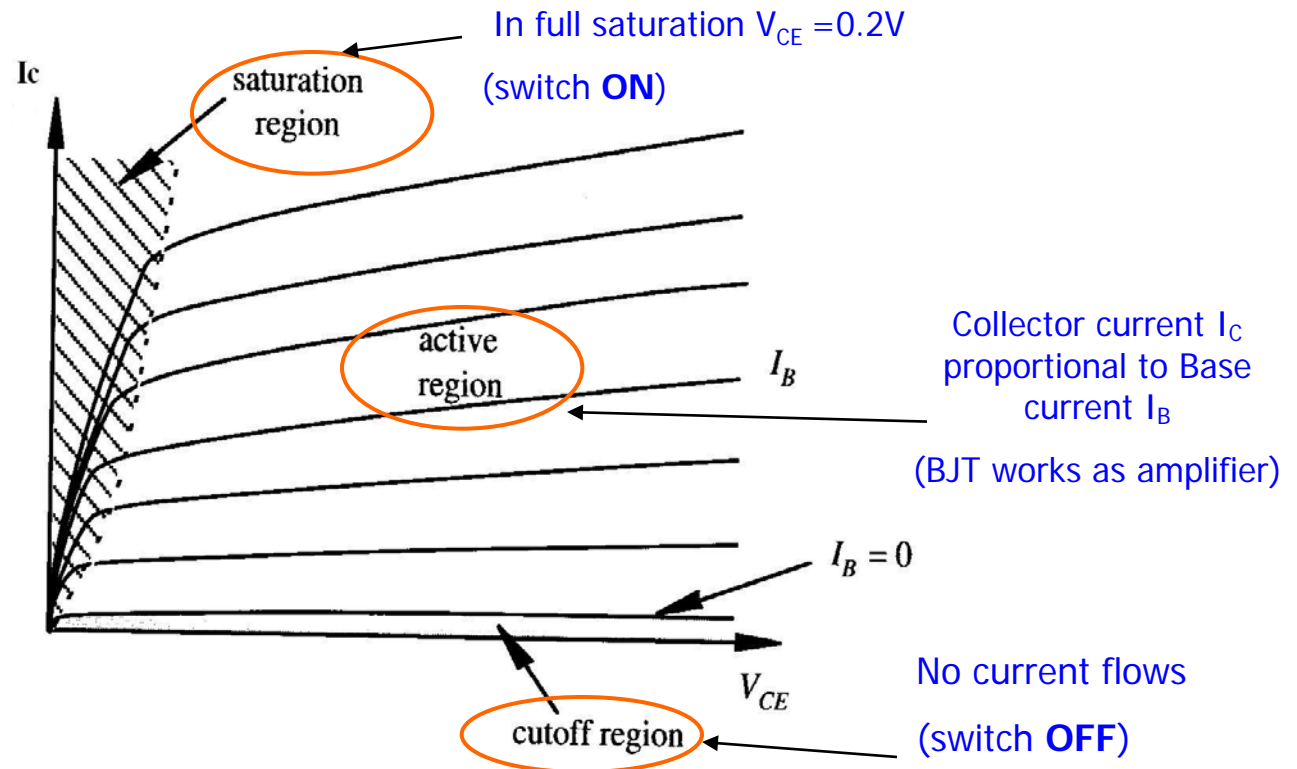
$$\alpha_{DC} = \frac{I_C}{I_E}$$

*Typical values of  $\alpha_{DC}$   
from 0.95 to 0.99 or less than 1.*

## BJT Operation

- ❑ Emitter is grounded and input voltage is applied to Base.
- ❑ Base-Emitter starts to conduct when  $V_{BE}$  is about 0.7V,  $I_C$  flows with  $I_C = \beta_{DC} I_B$
- ❑ As  $I_B$  further increases,  $V_{BE}$  slowly increases to 0.7V,  $I_C$  rises exponentially.
- ❑ As  $I_C$  rises, voltage drop across  $R_C$  increases and  $V_{CE}$  drops toward ground (transistor in saturation, no more linear relation between  $I_C$  and  $I_B$ )

### Common Emitter Characteristics



## ***BJT Operation***

- ❑ Electrons diffuse from **E**mitter to **B**ase (from  $n$  to  $p$ ) With  $V_C > V_B > V_E$
- ❑ Depletion layer on the Base-Collector junction  $\rightarrow$  no flow of electron allowed.
- ❑ The Base is thin and Emitter region is heavily doped  $\rightarrow$  electrons have enough momentum to cross Base into Collector.
- ❑ Small base current  $I_B$  controls large current  $I_C$  through  $\beta_{DC}$  which functioning as a current gain of the amplifier.
- ❑  $\beta_{DC}$  is temperature and voltage dependent.

## Example 1

- (a) For a given BJT:  $I_B = 50 \mu\text{A}$  and  $I_C = 3.65 \text{ mA}$ . Find the dc current gain ( $\beta_{DC}$ ),  $I_E$ , and  $\alpha_{DC}$ .  
(b) In a certain BJT:  $I_B = 50 \mu\text{A}$  and  $\beta_{DC} = 200$ . Find  $I_C$ ,  $I_E$ , and  $\alpha_{DC}$ . (HOME WORK)

### SOLUTION

$$\beta_{DC} = \frac{I_C}{I_B} = \frac{3.65 \text{ mA}}{50 \mu\text{A}} = \frac{3.65 \times 10^{-3}}{50 \times 10^{-6}} = 73$$

$$I_E = I_B + I_C = 50 \times 10^{-6} + 3.65 \times 10^{-3} = 3.7 \times 10^{-3} = 3.7 \text{ mA}$$

$$\alpha_{DC} = \frac{I_C}{I_E} = \frac{3.65 \text{ mA}}{3.7 \text{ mA}} = \frac{3.65 \times 10^{-3}}{3.7 \times 10^{-3}} = 0.986$$

## DC Analysis of BJT Circuit

$$V_{R_B} = V_{BB} - V_{BE}$$

Also, by Ohm's law,

$$V_{R_B} = I_B R_B$$

Substituting for  $V_{R_B}$  yields

$$I_B R_B = V_{BB} - V_{BE}$$

Solving for  $I_B$ ,

$$I_B = \frac{V_{BB} - V_{BE}}{R_B}$$

The voltage at the collector with respect to the grounded emitter is

$$V_{CE} = V_{CC} - V_{R_C}$$

Since the drop across  $R_C$  is

$$V_{R_C} = I_C R_C$$

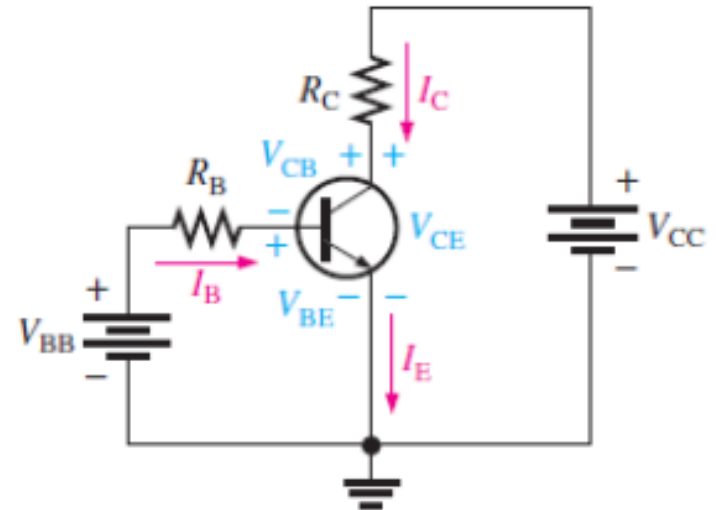
the voltage at the collector with respect to the emitter can be written as

$$V_{CE} = V_{CC} - I_C R_C$$

where  $I_C = \beta_{DC} I_B$ .

The voltage across the reverse-biased collector-base junction is

$$V_{CB} = V_{CE} - V_{BE}$$



DC Bias Circuit of *npn* Transistors



## Example 2

- 1) For the given npn BJT circuit if  $\beta_{DC} = 150$ , find:  $I_B$ ,  $I_C$ ,  $I_E$ ,  $V_{BE}$ ,  $V_{CE}$ , and  $V_{CB}$ .
- 2) Repeat the problem if  $\beta_{DC} = 90$ ,  $R_B = 22 \text{ k}\Omega$ ,  $R_C = 220 \Omega$ ,  $V_{BB} = 6 \text{ V}$ ,  $V_{CC} = 9 \text{ V}$ . (HOME WORK)

### SOLUTION

$$V_{BE} \cong 0.7 \text{ V}$$

$$I_B = \frac{V_{BB} - V_{BE}}{R_B} = \frac{5 \text{ V} - 0.7 \text{ V}}{10 \text{ k}\Omega} = 430 \mu\text{A}$$

$$I_C = \beta_{DC} I_B = (150)(430 \mu\text{A}) = 64.5 \text{ mA}$$

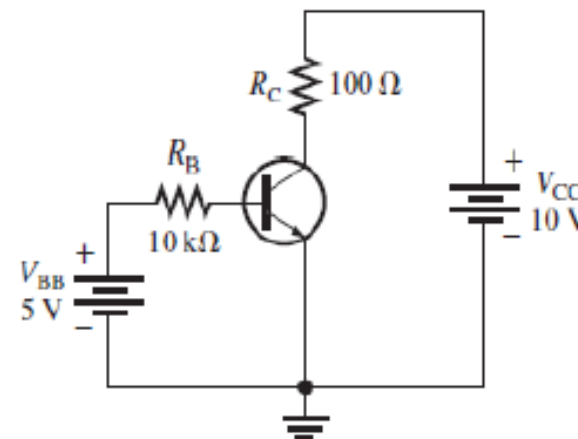
$$I_E = I_C + I_B = 64.5 \text{ mA} + 430 \mu\text{A} = 64.9 \text{ mA}$$

Solve for  $V_{CE}$  and  $V_{CB}$ .

$$V_{CE} = V_{CC} - I_C R_C = 10 \text{ V} - (64.5 \text{ mA})(100 \Omega) = 10 \text{ V} - 6.45 \text{ V} = 3.55 \text{ V}$$

$$V_{CB} = V_{CE} - V_{BE} = 3.55 \text{ V} - 0.7 \text{ V} = 2.85 \text{ V}$$

Since the collector is at a higher voltage than the base, the collector-base junction is reverse-biased.



# BJT As Switch

## OFF State

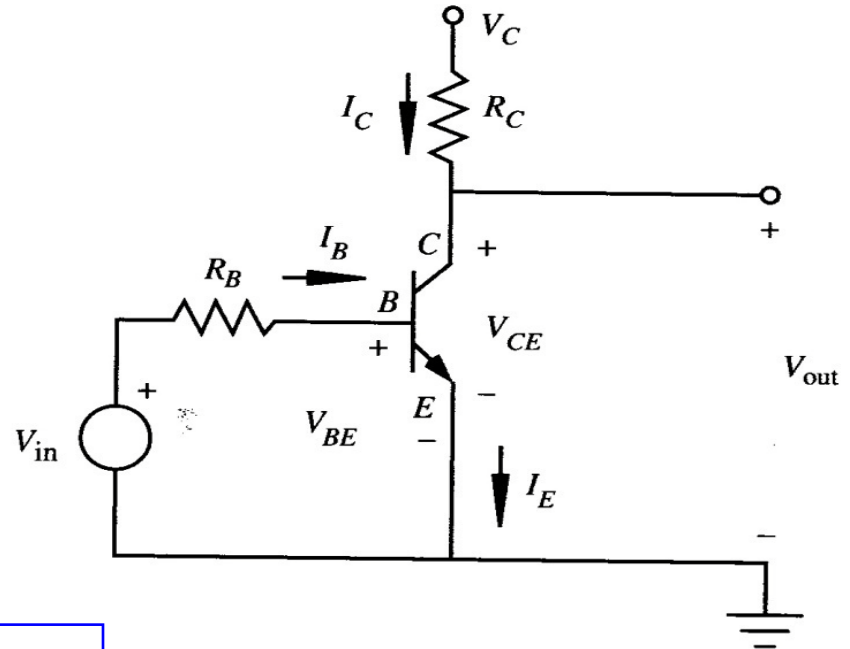
When  $V_{in} < 0.7V$

- BE junction not forward biased
- **Cutoff** state of transistor
- $I_C = I_E = 0$
- $V_{out} = V_{CE} = V_C$
- $V_{out} = \text{High}$

## ON State

When  $V_{in} > 0.7$

- BE junction forward biased ( $V_{BE} = 0.7V$ )
- $I_B = (V_{in} - V_{BE}) / R_B$
- **Saturation** region
- $V_{CE}$  small ( $\sim 0.2 V$  for saturated BJT)
- $V_{out} = \text{Low}$



## Example 3

**Practical LED Switch:** For the given 2N3904 npn BJT circuit assuming the LED requires 20-40 mA to provide a bright display and has 2 voltage drop when forward biased. Find that the circuit works properly with ON and OFF states.

### Solution

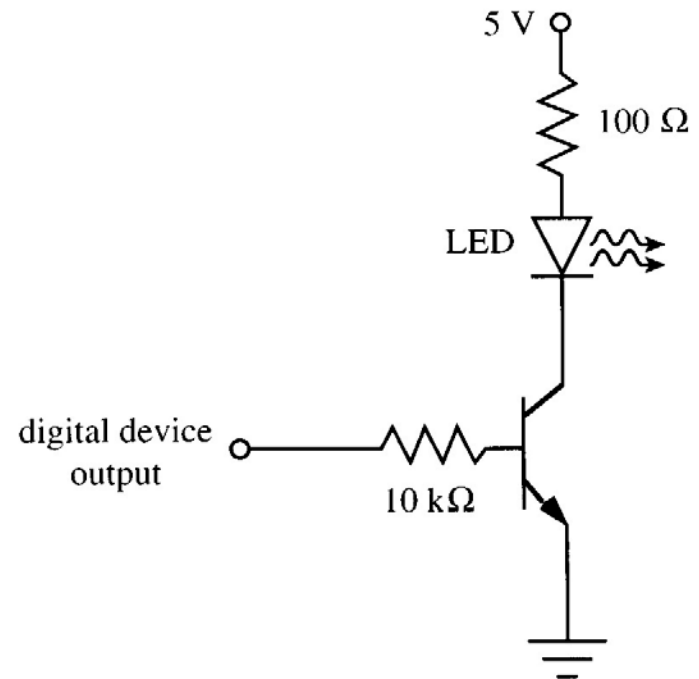
- When digital output is 0V, transistor is **OFF**.
- When digital output is 5V, the transistor is in **saturation (ON)**, with base current:

$$I_B = (5V - 0.7V) / 10K\Omega = 0.43 \text{ mA}$$

Collector current (LED current) is limited by collector resistor as:

$$I_C = (5V - 2V - 0.2V) / 100\Omega = 28 \text{ mA}$$

*Hence: LED is lighted properly*



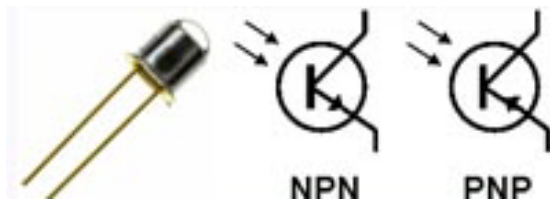
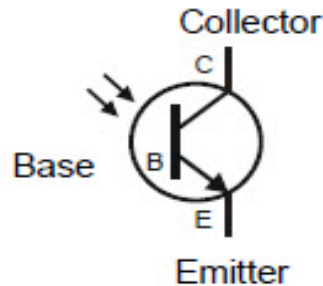
# Phototransistors

- **Phototransistors** are solid-state light detectors that possess internal gain.
- They are photodiode-amplifier combinations (2 or 3 terminals) integrated within a single silicon chip to overcome the major fault of photodiodes (unity gain).
- They can be used to provide either an analog or digital output signal.

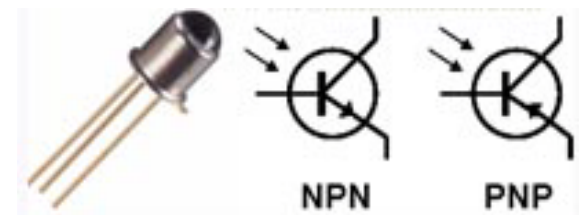
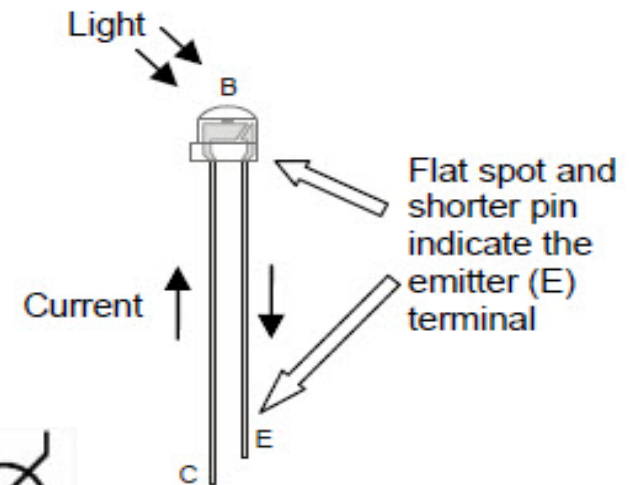


## NPN Phototransistors

0.25", small area, high speed  
0.04", medium area, high sensitivity  
0.05", large area, high sensitivity



## Two and Three Terminal Phototransistors



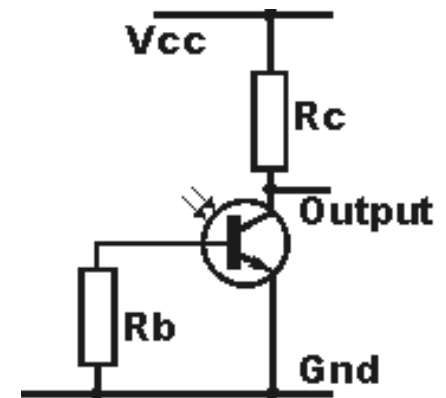
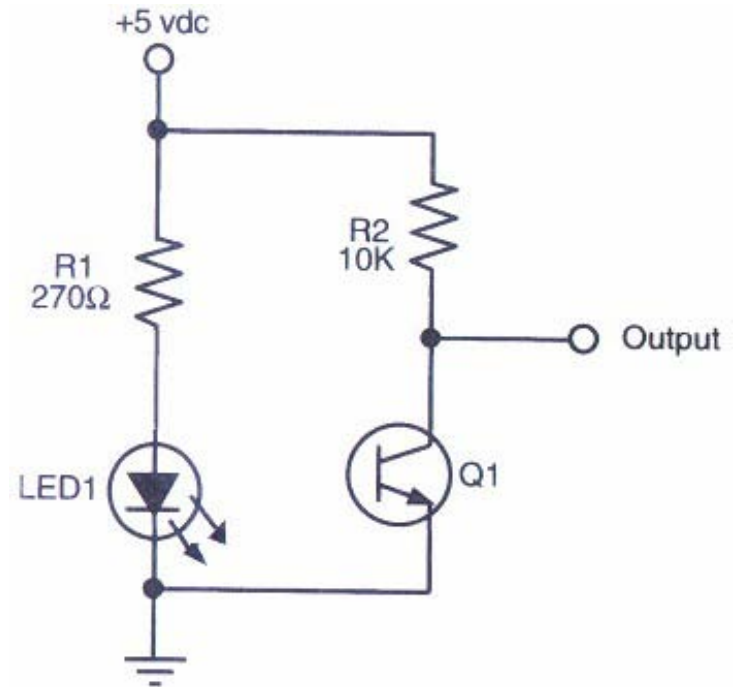
# Features and Applications of Phototransistors

## Features

- Low-cost visible and near-IR region.
- Available with gains from 100 to over 1500.
- Moderately fast response times.
- Available in a wide range of packages.
- Same general electrical characteristics as BJTs.

## Applications

- Computer/business equipment: write-protect control and margin controls in printers.
- Industrial: security systems and safety shields.
- Consumers: coin counters, lottery card readers, audio/visual equipments, games, and camera shutter control.



**Circuit Diagrams for  
Phototransistor Connections**

# Problems and Solutions

## Question 1

Using ideal BJT switch of  $\beta_{DC} = 200$ ,  $V_{CC} = 10V$  and  $I_B = 20\mu A$ .

- 1) Find the value of base resistor  $R_B$  required to switch the load "ON" when the input terminal voltage exceeds 2.5V and  $V_{BE} = 0.7V$ .
- 2) Calculate  $R_C$  for point (1).
- 3) Find the minimum base current  $I_B$  required to turn the transistor "Fully-ON" (saturated) for a load that requires 200 mA when the input voltage is increased to 5.0V. Also calculate the new value of  $R_B$ .

## Solution:

$$1) R_B = \frac{V_{in} - V_{BE}}{I_B} = \frac{2.5 - 0.7}{20 \times 10^{-6}} = 90 \text{ k}\Omega$$

2) For ideal BJT at saturation  $V_{CE} = 0$  Volt

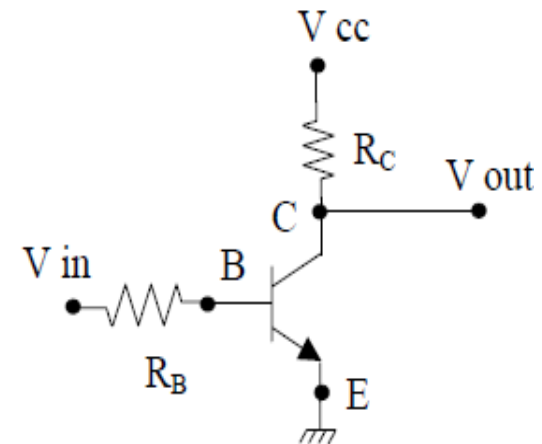
$$I_C = \beta_{DC} I_B = 200 \times 20 \times 10^{-6} = 4 \text{ mA}$$

$$R_C = \frac{V_{CC} - V_{CE}}{I_C} = \frac{10 - 0}{4 \times 10^{-3}} = 2.5 \text{ k}\Omega$$

3) At ON state, the load current is equal to  $I_C$

$$I_B = \frac{I_C}{\beta_{DC}} = \frac{200 \text{ mA}}{200} = 1 \text{ mA}$$

$$R_B = \frac{V_{in} - V_{BE}}{I_B} = \frac{5 - 0.7}{1 \times 10^{-3}} = 4.3 \text{ k}\Omega$$



**Question 2** The BJT in the given circuit has:  $50 \leq \beta_{DC} \leq 150$ ,  $V_{CC} = 12V$ ,  $V_{BE} = 0.7V$ , and  $V_{CE} = 0.2V$ . Find  $R_B$  that saturates the BJT with the so called Over Driven Factor (ODF) of at least 10.

**Solution:**

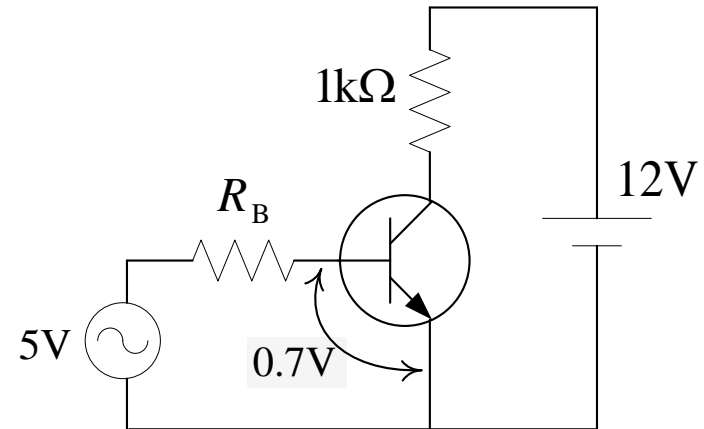
$$I_{Csat} = \frac{V_{CC} - V_{CE}}{R_C} = \frac{12 - 0.2}{1 \times 10^3} = 11.8 \text{ mA}$$

$$I_B = \frac{I_{Csat}}{\beta_{DC \min}} = \frac{11.8 \times 10^{-3}}{50} = 0.236 \text{ mA}$$

For OFD of at least 10, we have:

$$I'_B = 10 \times I_B = 10 \times 0.236 \times 10^{-3} = 2.36 \text{ mA}$$

$$R_B = \frac{V_{in} - V_{BE}}{I'_B} = \frac{5 - 0.7}{2.36 \times 10^{-3}} = 1.82 \text{ k}\Omega$$



**Question 3** Find for the given npn BJT circuit:  $I_B$  ,  $I_C$  ,  $I_E$  ,  $V_{CB}$  ,  $\beta_{DC}$  ,  $\alpha_{DC}$

**Solution:**

We have  $V_{BE} = 0.7 \text{ V}$  and from the circuit  $V_{CE} = 8 \text{ V}$

$$I_B = \frac{V_{BB} - V_{BE}}{R_B} = \frac{4 - 0.7}{4.7 \times 10^3} = 0.7 \text{ mA}$$

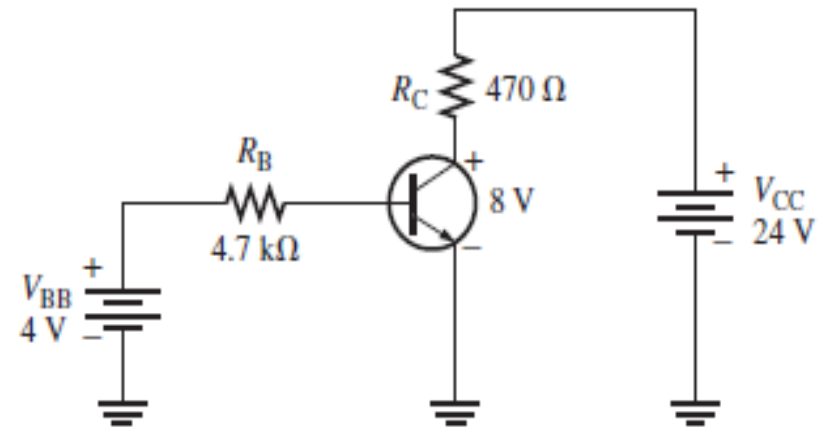
$$I_C = \frac{V_{CC} - V_{CE}}{R_C} = \frac{24 - 8}{470} = 34 \text{ mA}$$

$$I_E = I_B + I_C = 0.7 \text{ mA} + 34 \text{ mA} = 34.7 \text{ mA}$$

$$V_{CB} = V_{CE} - V_{BE} = 8 - 0.7 = 7.3 \text{ V}$$

$$\beta_{DC} = \frac{I_C}{I_B} = \frac{34 \text{ mA}}{0.7 \text{ mA}} = 48.57$$

$$\alpha_{DC} = \frac{I_C}{I_E} = \frac{34 \text{ mA}}{34.7 \text{ mA}} = 0.9798$$





**Question 4** For the given BJT switch circuit:  $\beta_{DC} = 100$ ,  $V_{CC} = 5V$ ,  $V_{BE} = 0.7V$ ,  $V_{CE} = 0V$ ,  $V_{LED} = 2V$  and  $I_{LED} = 15mA$ . Assuming the minimum average voltage of microcontroller I/O port  $V_{port}$  with logical “1” is about 4.2V.

- 1) Find the value of  $R_B$  and  $R_C$ .
- 2) Calculate the power dissipation on  $R_B$  and  $R_C$ .

**Solution:**

$$1) I_C = 5 \times I_{LED} = 5 \times 15 \times 10^{-3} = 75 \text{ mA}$$

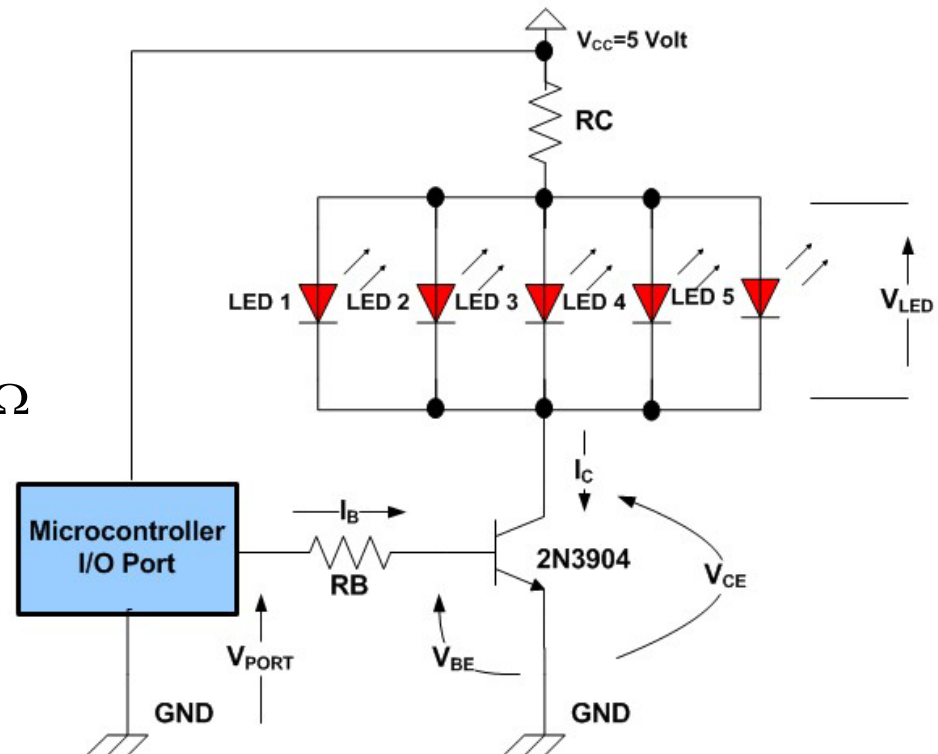
$$I_B = \frac{I_C}{\beta_{DC}} = \frac{75 \text{ mA}}{100} = 0.75 \text{ mA}$$

$$R_B = \frac{V_{port} - V_{BE}}{I_B} = \frac{4.2 - 0.7}{0.75 \times 10^{-3}} = 4.6 \text{ k}\Omega$$

$$R_C = \frac{V_{CC} - V_{LED} - V_{CE}}{I_C} = \frac{5 - 2 - 0}{75 \times 10^{-3}} = 40 \Omega$$

$$2) \text{ Power dissipation on } R_B = I_B^2 R_B \\ = (0.75 \times 10^{-3})^2 \times 4.6 \times 10^3 = 2.58 \text{ mW}$$

$$\text{Power dissipation on } R_C = I_C^2 R_C \\ = (75 \times 10^{-3})^2 \times 40 = 0.225 \text{ W}$$



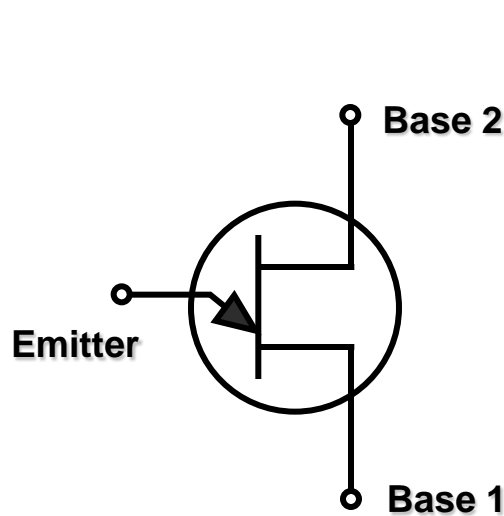


# **Chapter 3**

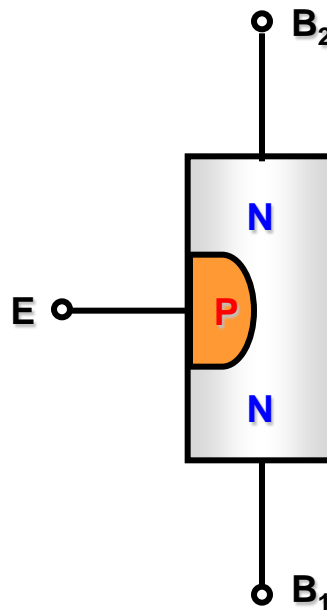
## **The Uni-Junction Transistor ( UJT )**

# The Uni-Junction Transistor UJT

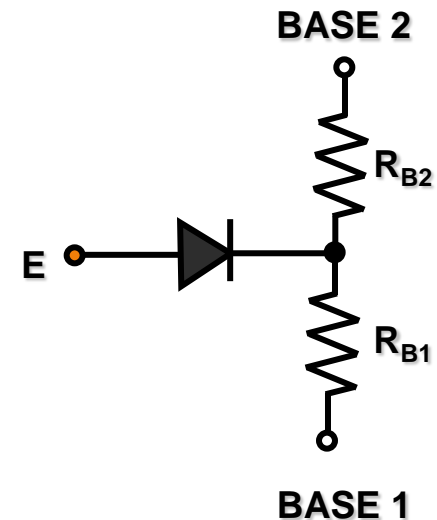
UJT is a semiconductor device having only one PN junction and three terminals, Base1, Base2, and Emitter.



**Symbol**



**Structure**



**Equivalent Circuit**

The Inter-Base Resistor:  $R_{BB} = R_{B1} + R_{B2}$

# Equivalent Circuit Of UJT

❑ The  $V_{BB}$  source is generally fixed and provides constant voltage from  $B_2$  to  $B_1$ .

❑ The UJT is normally operated with both  $B_2$  and  $E$  is positive biased relative to  $B_1$ .

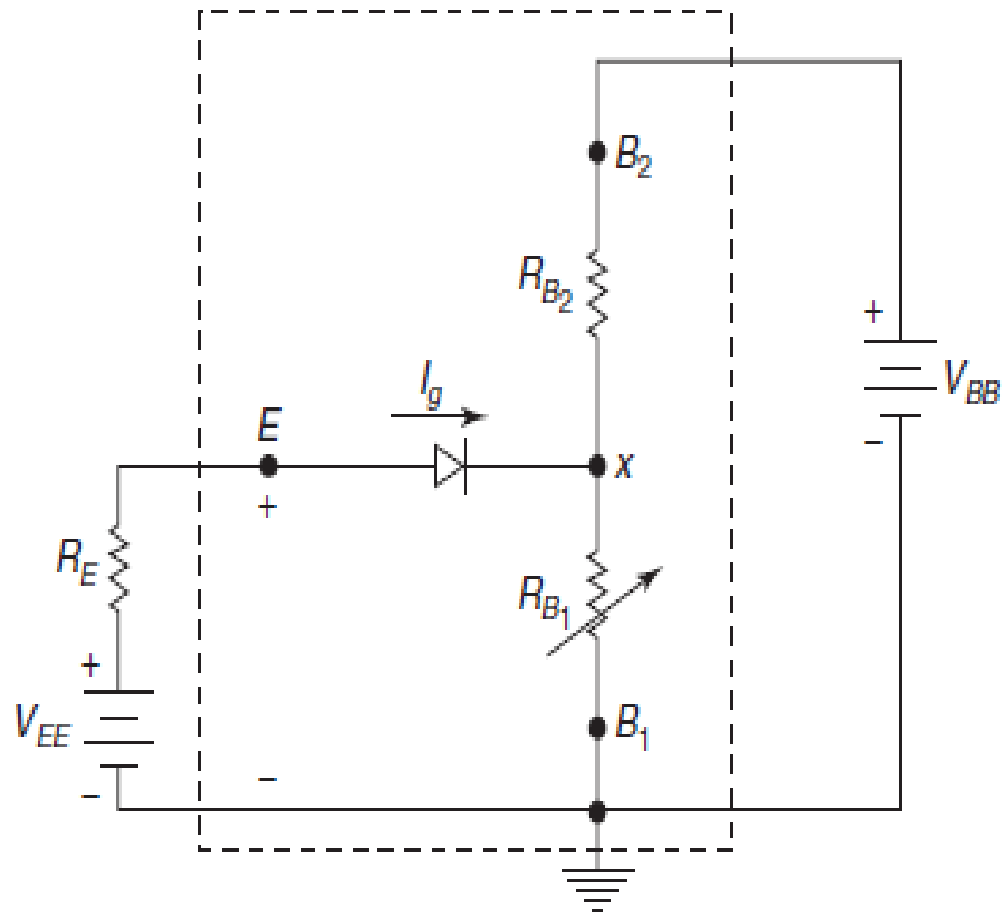
❑  $B_1$  is always the UJT reference terminal and all voltages are measured relative to  $B_1$ .

❑  $V_{EE}$  is a variable voltage source.

❑  $\eta$  is the **Intrinsic standoff ratio**:

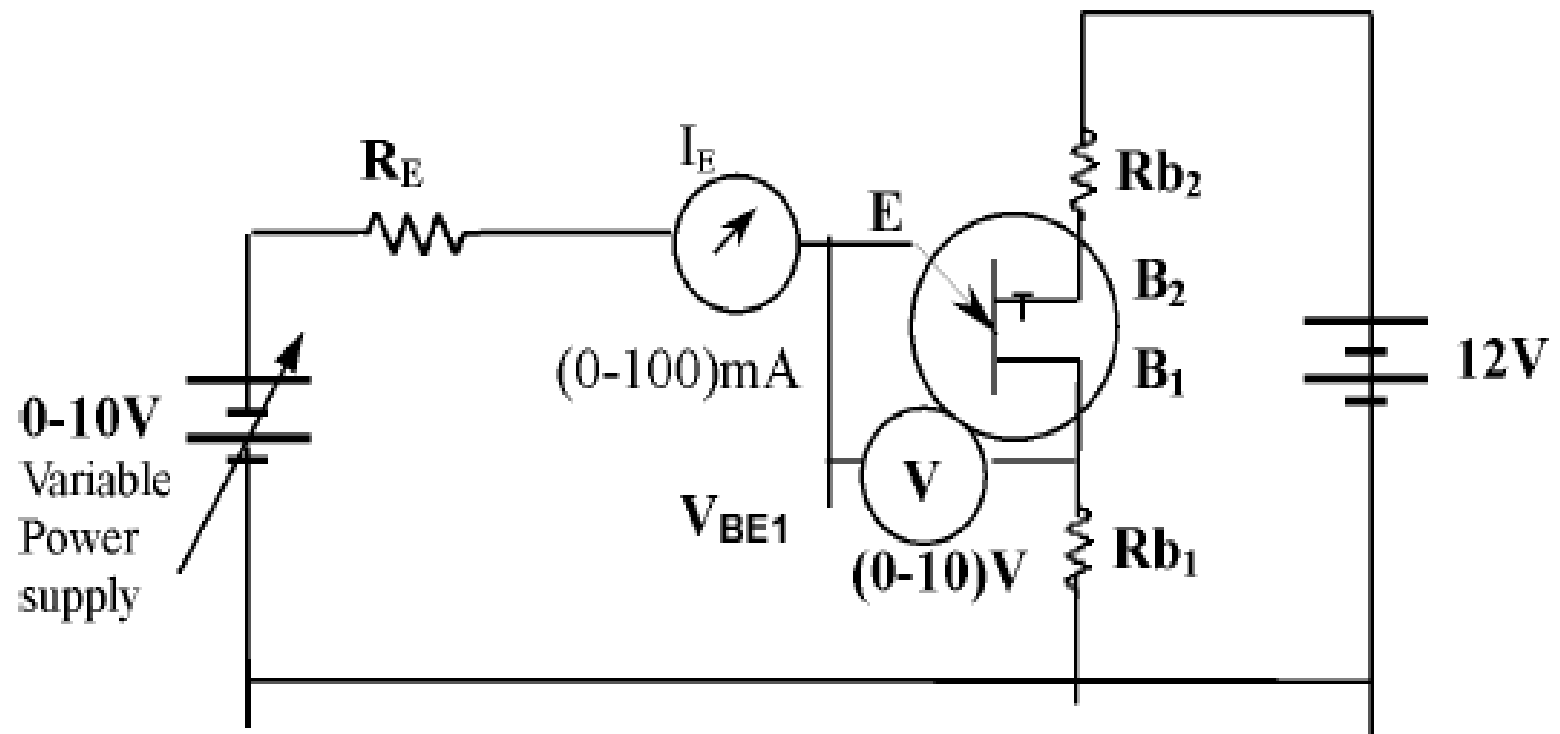
$$\eta = \frac{R_{B1}}{R_{B1} + R_{B2}} = \frac{R_{B1}}{R_{BB}}$$

$$R_{BB} = R_{B1} + R_{B2}$$



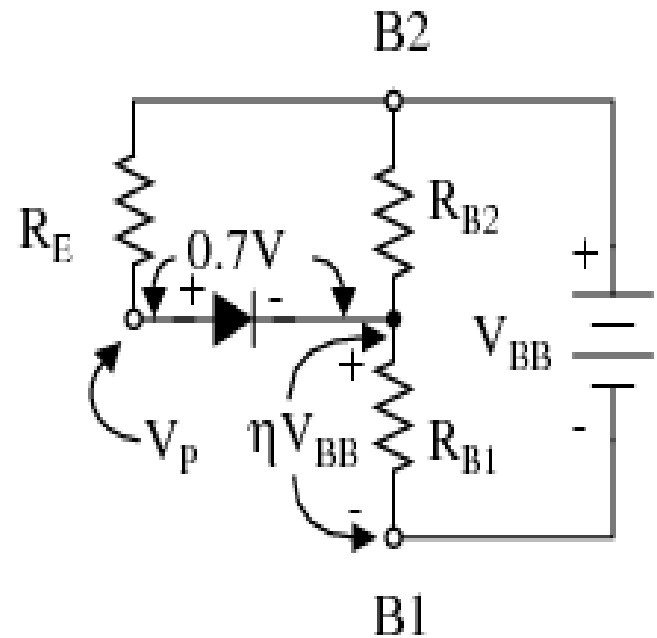
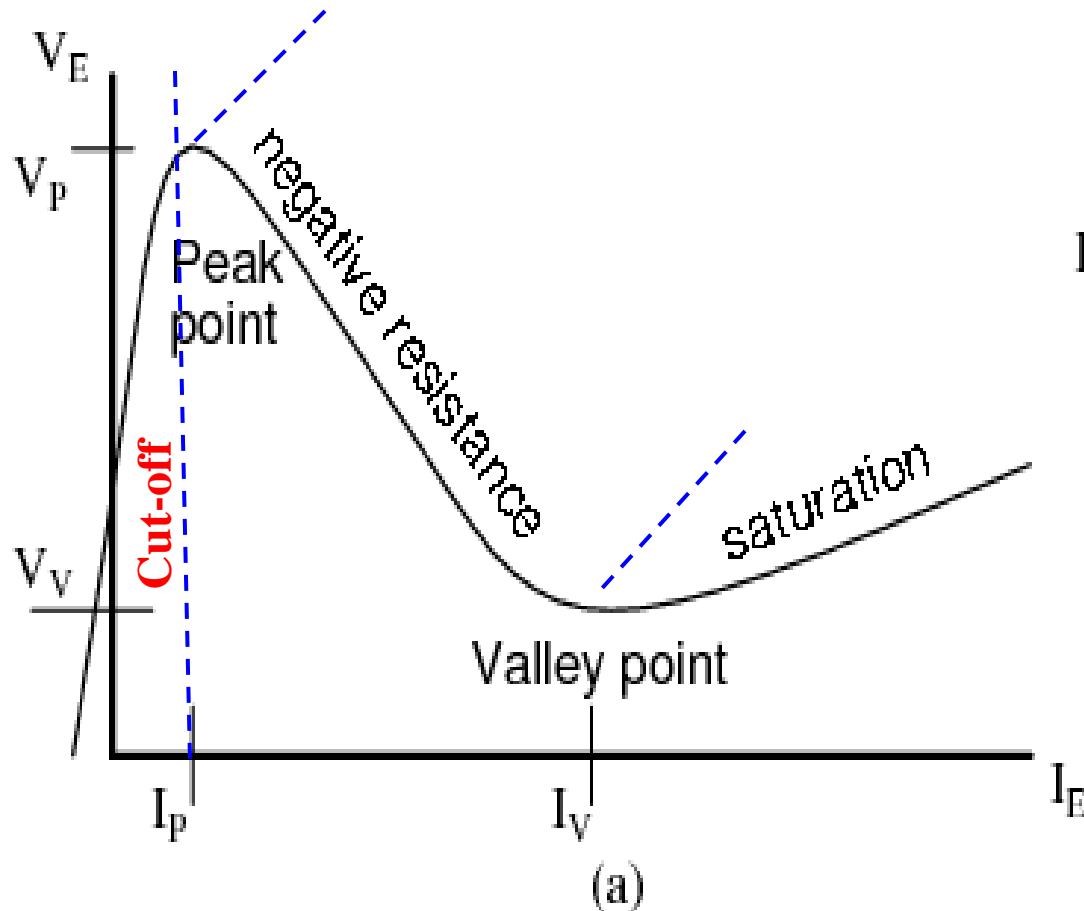
# Input Forward Characteristics Of UJT

## CIRCUIT DIAGRAM:



Standard values :  $R_E = 1K\Omega$ ,  $R_{b2} = 2.2K\Omega$ ,  $R_{b1} = 220\Omega$ ,  $T = 2N2646$

# Characteristic Curve



$$V_P = 0.7 + \eta V_{BB}$$

$$V_V \approx 0.10(V_{BB})$$

(b)

# UJT Relaxation Oscillator

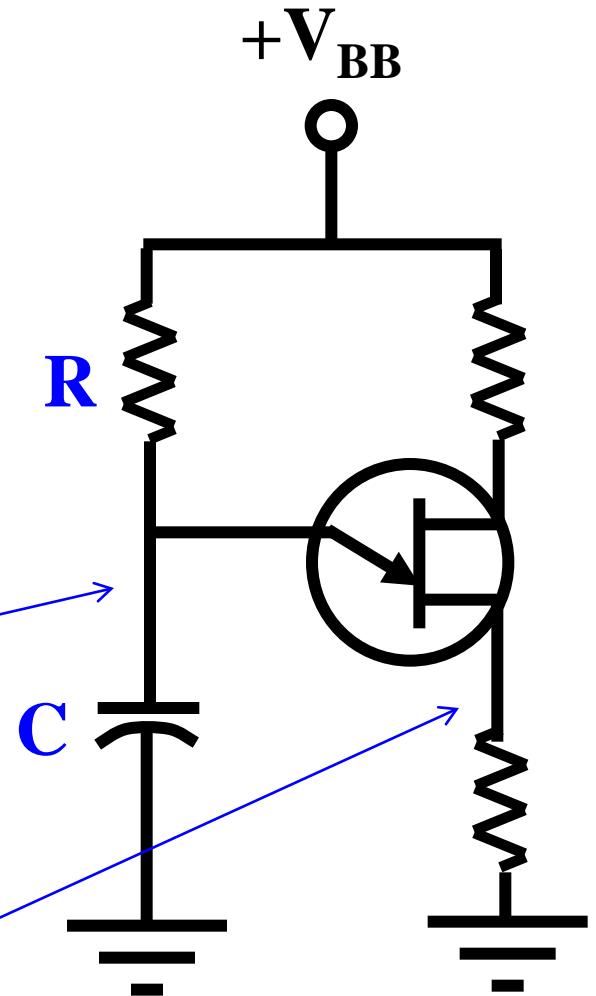
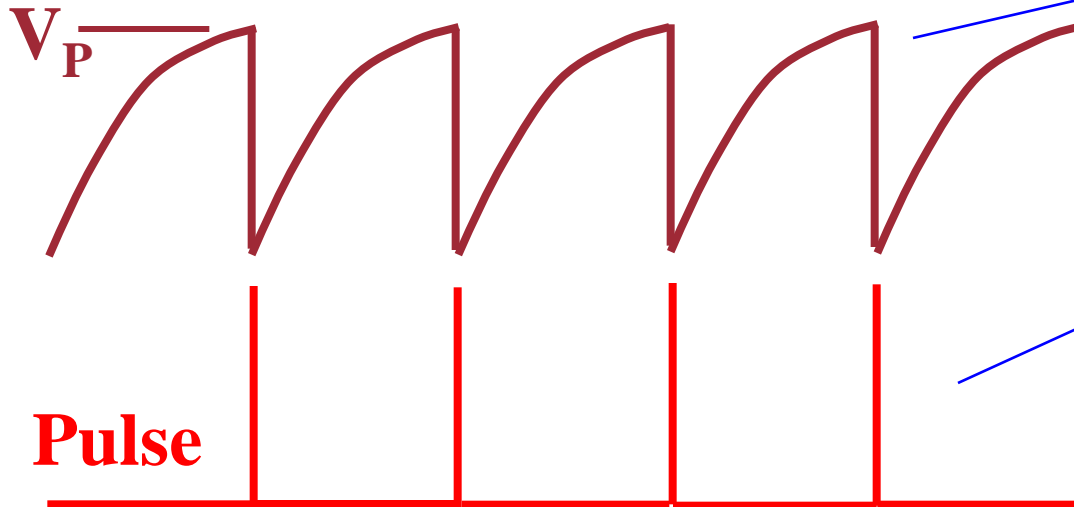
It provides two waveforms.

$$f \cong \frac{1}{RC \ln \left( \frac{1}{1-\eta} \right)}$$

$$\eta = \frac{R_{B1}}{R_{B1} + R_{B2}}$$

$$\tau = RC$$

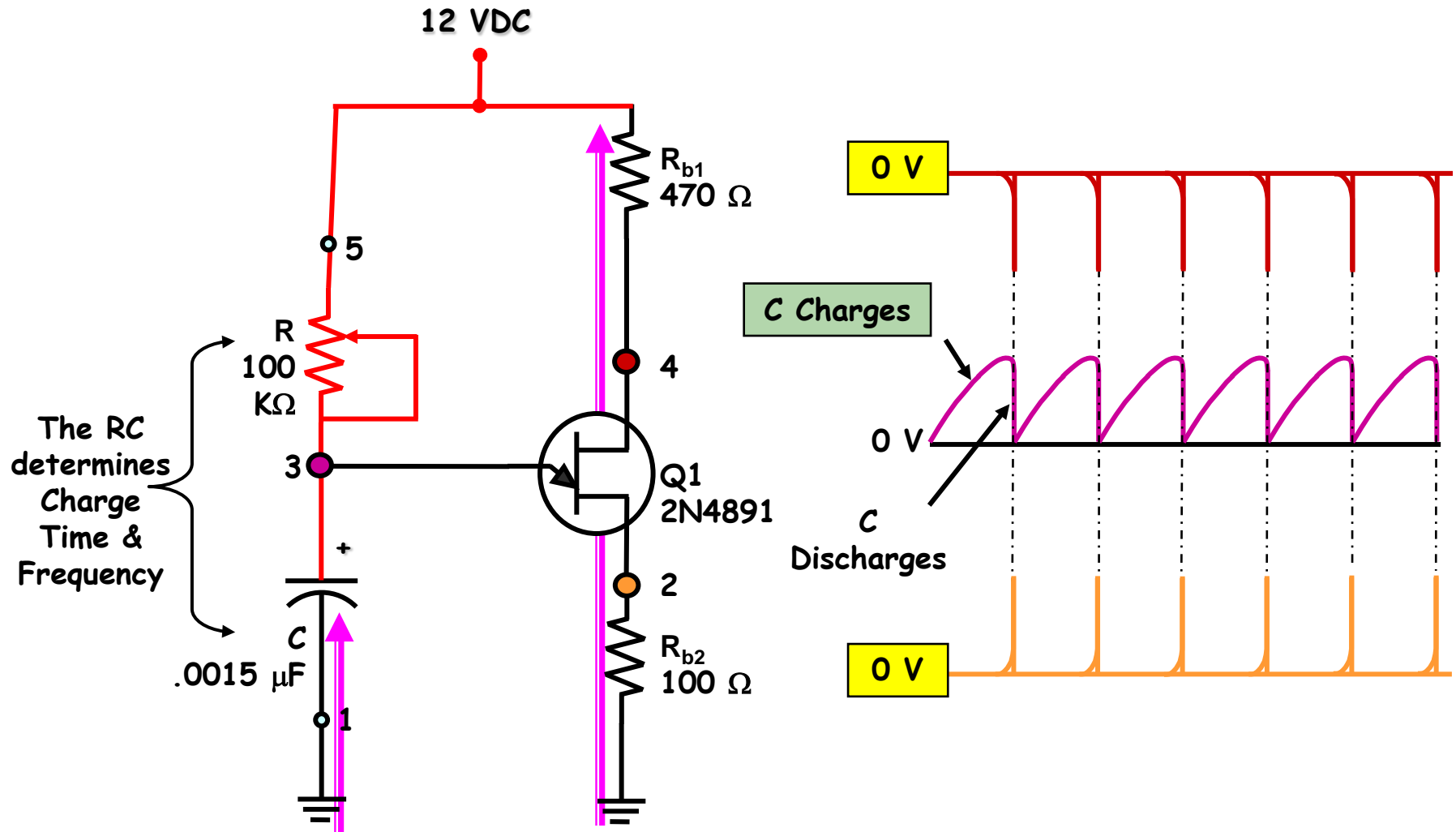
**Exponential sawtooth**





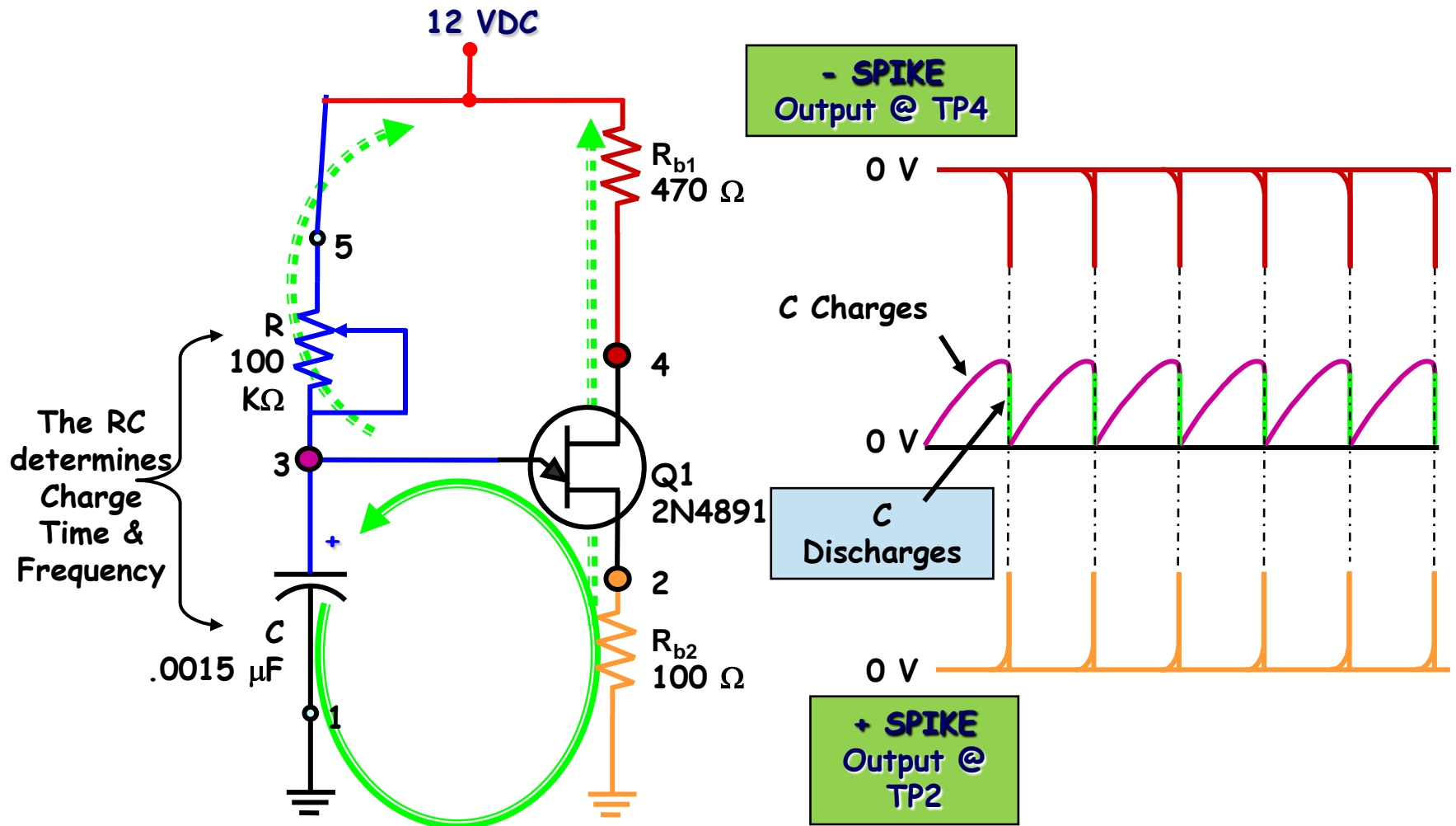
# Operation of UJT Relaxation Oscillator:

*C* charging



# Operation of UJT Relaxation Oscillator:

*C* discharging



Output; + & - Spikes and Sawtooth at TP3

## Theory of operation as an oscillator

- For satisfactory operation, two conditions for the turn-on and turn-off of the UJT must be met as:

$$\frac{V_{BB} - V_V}{I_V} < R < \frac{V_{BB} - V_P}{I_P}$$

- The time period and, therefore, frequency of oscillation can be derived as below.

*The voltage across the capacitor during charging is given as:*

$$V_C = V_{BB} \left( 1 - e^{-t/RC} \right)$$

$$\begin{aligned} V_P &= V_D + \eta V_{BB} \\ &= V_C = V_{BB} \left( 1 - e^{-t/RC} \right) \end{aligned}$$

$$V_{swing} = V_P - V_V$$

$$\begin{aligned} T &= \frac{1}{f} = RC \ln \left( \frac{1}{1 - \eta} \right) \\ &= 2.3RC \log_{10} \left( \frac{1}{1 - \eta} \right) \end{aligned}$$

**Example 1** Design a 1kHz relaxation oscillator using UJT with the following specifications:  
 $V_{BB} = 10V$ ,  $\eta = 0.56 \sim 0.75$ ,  $I_P = 5\mu A$ , and  $I_V = 4mA$ .

**Solution:**

The value of  $R$  can be found using the following condition:

$$\frac{V_{BB} - V_V}{I_V} < R < \frac{V_{BB} - V_P}{I_P}$$

$$\therefore R_{\max} = \frac{V_{BB} - V_P}{I_P} \quad \text{and} \quad R_{\min} = \frac{V_{BB} - V_V}{I_V}$$

$$V_P = 0.7 + \eta V_{BB}$$

$$V_V \simeq 0.1 V_{BB} = 1V$$

For the given UJT, the average value of  $\eta$  can be found as:  $\eta = \frac{0.56 + 0.75}{2} = 0.655$

$$\Rightarrow V_P = 0.7 + 0.655 \times 10 = 7.25V$$

$$\Rightarrow R_{\max} = \frac{10 - 7.25}{5 \times 10^{-6}} = 550k\Omega \quad \Rightarrow R_{\min} = \frac{10 - 1}{4 \times 10^{-3}} = 2.25k\Omega$$

Suitable value of  $R$  can be selected between  $2.25k\Omega$  and  $550k\Omega$  as:  $R = 10k\Omega$

$$f = \frac{1}{RC \ln\left(\frac{1}{1-\eta}\right)} \quad \Rightarrow C = \frac{1}{1 \times 10^3 \times 10 \times 10^3 \times \ln\left(\frac{1}{1-0.655}\right)} \approx 94nF$$

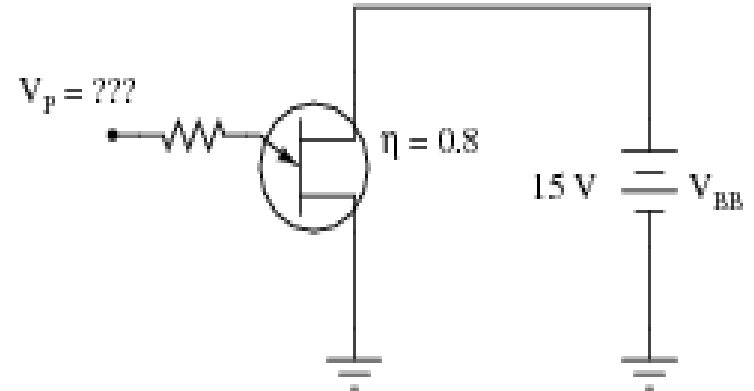
**Example 2**

A given UJT with an intrinsic standoff ratio ( $\eta = 0.8$ ) is powered by a 15 volt DC source. Calculate the emitter voltage ( $V_P$ ) needed to “trigger” this UJT into its conductive state.

Solution:

$$V_P = V_D + \eta V_{BB} = 0.7 + \eta V_{BB}$$

$$\Rightarrow V_P = 0.7 + 0.8 \times 15 = 12.7 \text{ V}$$

**Example 3**

A given UJT relaxation oscillator has the following:  $V_{BB} = 30\text{V}$ ,  $V_D = 0.6\text{V}$ ,  $R = 100\text{k}\Omega$ , and  $\eta = 0.6$ . What is the value of  $C$  that gives 1kHz output frequency? Calculate the maximum value of capacitor voltage  $V_C$ .

Solution:

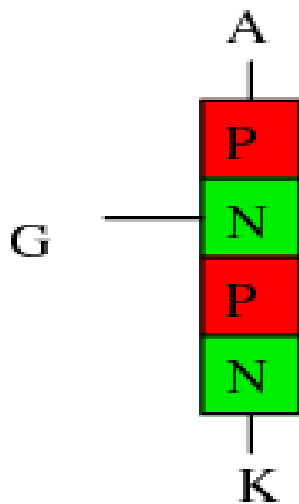
$$V_P = V_D + \eta V_{BB} \Rightarrow V_P = 0.6 + 0.6 \times 30 = 18.6 \text{ V}$$

$$f = \frac{1}{RC \ln\left(\frac{1}{1-\eta}\right)} \Rightarrow C = \frac{1}{1 \times 10^3 \times 100 \times 10^3 \times \ln\left(\frac{1}{1-0.6}\right)} = 1.09 \times 10^{-6} \text{ F} = 1.09 \mu\text{F}$$

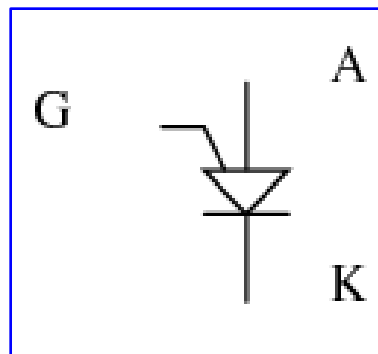
$$(V_C)_{\max} = V_P \Rightarrow (V_C)_{\max} = 18.6 \text{ V}$$

# Programmable Unijunction Transistor (PUT):

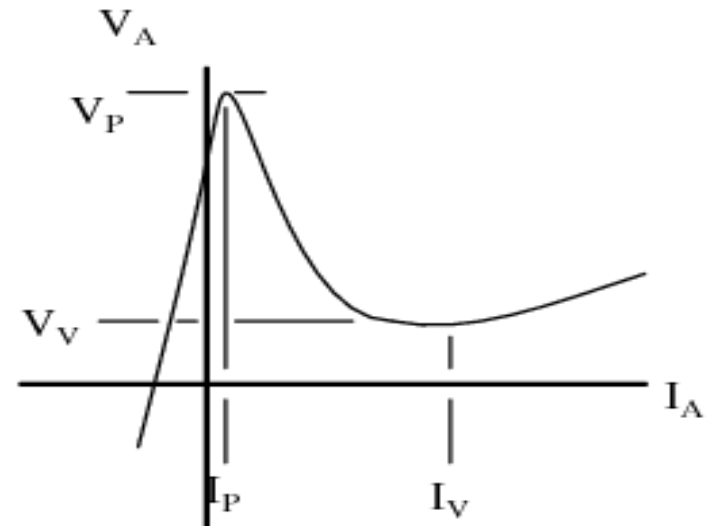
- ❑ Although UJT is expensive if obtained, the PUT is inexpensive and in production.
- ❑ PUT serves similar to the UJT, But it has three terminals as the thyristor.
- ❑ The PUT shares the four-layer structure typical of thyristors as shown.
- ❑ The gate, an N-type layer near the anode, is known as an “anode gate”.
- ❑ The gate lead on the schematic symbol is attached to the anode end of the symbol.



**PUT Configuration**

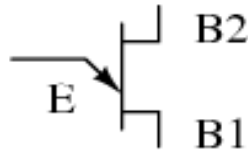


**Symbol**

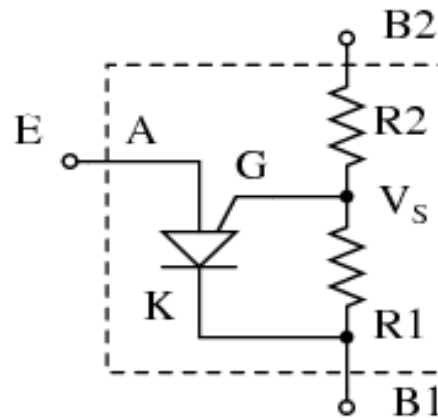


**Input forward characteristics**

## PUT Equivalent Circuit



Unijunction



PUT equivalent

$$R_{BB0} = R1 + R2$$

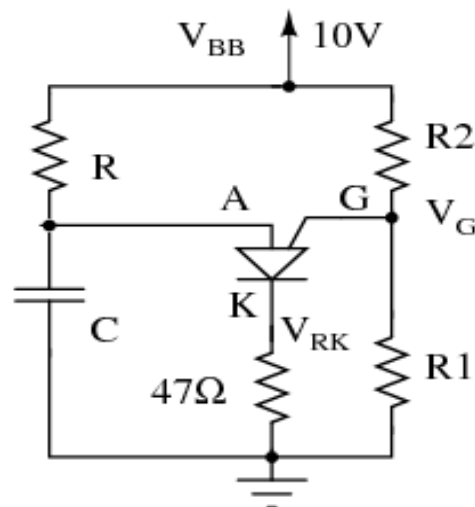
$$\eta = \frac{R1}{R1 + R2}$$

$$V_S = \eta V_{BB}$$

$$V_P = V_T + V_S$$

$$R_G = \frac{R1 \cdot R2}{R1 + R2}$$

## PUT Relaxation Oscillator



# Problems and Solutions

**Question 1** For a given UJT of 180 mw power and inter-base resistor  $R_{BB} = 4k\Omega$ , find the estimated value of maximum source voltage  $V_{BB}$ .

Solution:

$$\text{UJT Power} = \frac{V_{BB}^2}{R_{BB}}$$

$$\Rightarrow V_{BB}^2 = 180 \times 10^{-3} \times 4 \times 10^3 = 720$$

$$\therefore V_{BB} = \sqrt{720} = 26.8 \text{ Volt}$$

---

**Question 2** For a given UJT,  $V_{BB} = 10$  volts,  $\eta_{min} = 0.6$ , and  $\eta_{max} = 0.8$ , find the possible values of  $V_P$ .

Solution:

$$V_P = V_D + \eta V_{BB} = 0.7 + \eta V_{BB}$$

$$\Rightarrow (V_P)_{min} = 0.7 + \eta_{min} V_{BB} = 0.7 + 0.6 \times 10 = 6.7 \text{ Volt}$$

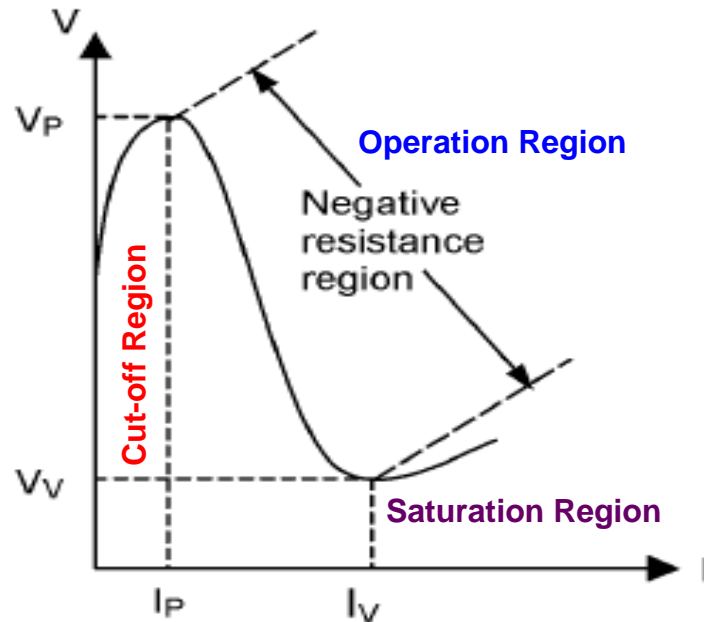
$$\Rightarrow (V_P)_{max} = 0.7 + \eta_{max} V_{BB} = 0.7 + 0.8 \times 10 = 8.7 \text{ Volt}$$



### Question 3

Sketch the input forward characteristics curve of UJT and indicate the regions of operation.

Solution:



Input forward characteristics curve of UJT

---

### Question 4

Why a UJT oscillator called relaxation oscillator?

Solution:

Because the charging time constant  $RC$  is much greater than the discharging time. So the capacitor relax in charging state, and hence the name of relaxation oscillator.

## Question 5

For the given relaxation oscillator: 1) find the output frequency if  $\eta = 0.65$ , 2) the maximum value of  $V_C$ , and 3) the value of  $V_C$  at half value of periodic time  $T$ .

### Solution:

1)

$$f = \frac{1}{RC \ln\left(\frac{1}{1-\eta}\right)}$$

$$\therefore f = \frac{1}{68 \times 10^3 \times 0.01 \times 10^{-6} \times \ln\left(\frac{1}{1-0.65}\right)} = 1.4 \text{ kHz}$$

2)

$$V_P = V_D + \eta V_{BB} = 0.7 + \eta V_{BB}$$

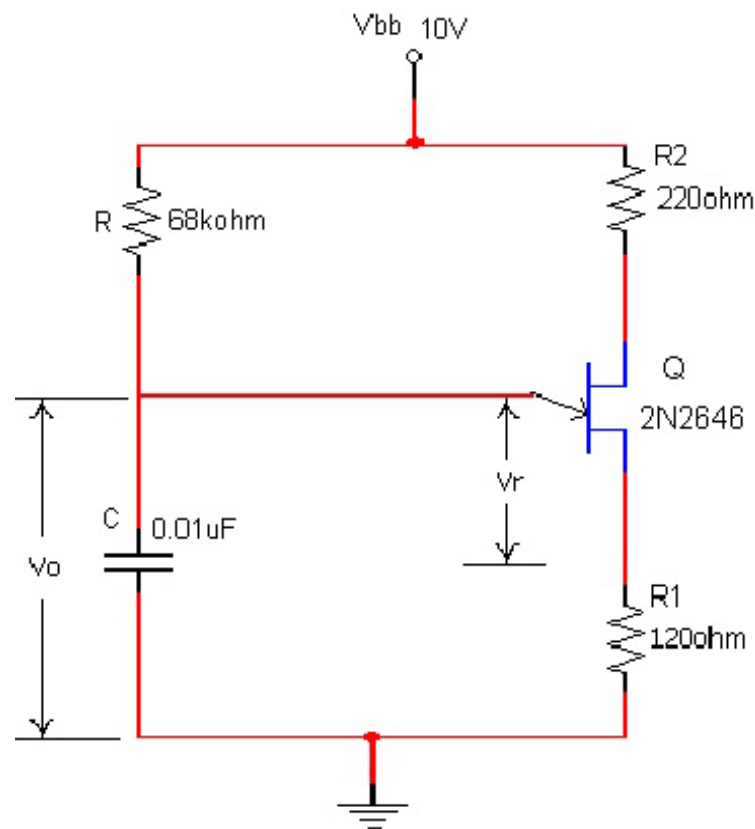
$$\Rightarrow V_P = 0.7 + 0.65 \times 10 = 7.2 \text{ V}$$

$$(V_C)_{\max} = V_P \Rightarrow (V_C)_{\max} = 7.2 \text{ V}$$

3)

$$V_C = V_{BB} \left(1 - e^{-t/RC}\right)$$

$$\text{at } t = \frac{T}{2} = \frac{1}{2f} = \frac{1}{2 \times 1.4 \times 10^3} = 0.357 \text{ m sec} \Rightarrow V_C = 10 \left(1 - e^{\frac{-0.357 \times 10^{-3}}{(68 \times 10^3 \times 0.01 \times 10^{-6})}}\right) = 4 \text{ V}$$



**Question 6** A given UJT relaxation oscillator has the following:  $V_{BB} = 20\text{V}$ ,  $I_V = 10\text{mA}$ ,  $I_P = 40\text{ }\mu\text{A}$ ,  $C = 1\text{ }\mu\text{F}$ , and  $\eta = 0.65$ . Find the value of maximum and minimum frequencies.

**Solution:**

$$V_P = 0.7 + \eta V_{BB} \Rightarrow V_P = 0.7 + 0.65 \times 20 = 13.7\text{V}$$

$$V_V \simeq 0.1 V_{BB} = 2\text{V}$$

$$f = \frac{1}{RC \ln\left(\frac{1}{1-\eta}\right)} \Rightarrow f_{\max} = \frac{1}{R_{\min} C \ln\left(\frac{1}{1-\eta}\right)} \quad \text{and} \quad f_{\min} = \frac{1}{R_{\max} C \ln\left(\frac{1}{1-\eta}\right)}$$

$$\therefore R_{\max} = \frac{V_{BB} - V_P}{I_P} \quad \text{and} \quad R_{\min} = \frac{V_{BB} - V_V}{I_V}$$

$$\Rightarrow R_{\max} = \frac{20 - 13.7}{40 \times 10^{-6}} = 157.5\text{k}\Omega \quad \Rightarrow R_{\min} = \frac{20 - 2}{10 \times 10^{-3}} = 1.8\text{k}\Omega$$

$$\therefore f_{\max} = \frac{1}{1.8 \times 10^3 \times 1 \times 10^{-6} \times \ln\left(\frac{1}{1-0.65}\right)} = 529\text{Hz}$$

$$\therefore f_{\min} = \frac{1}{157.5 \times 10^3 \times 1 \times 10^{-6} \times \ln\left(\frac{1}{1-0.65}\right)} = 6\text{Hz}$$

**Question 7** For the given UJT relaxation oscillator, calculate the maximum and minimum frequencies if  $\eta = 0.6$

**Solution:**

$$V_P = 0.7 + \eta V_{BB} \Rightarrow V_P = 0.7 + 0.6 \times 12 = 7.9 \text{ V}$$

$$V_V \simeq 0.1 V_{BB} = 1.2 \text{ V}$$

$$R_{\max} = R_1 + R_2 = 118 \text{ k}\Omega$$

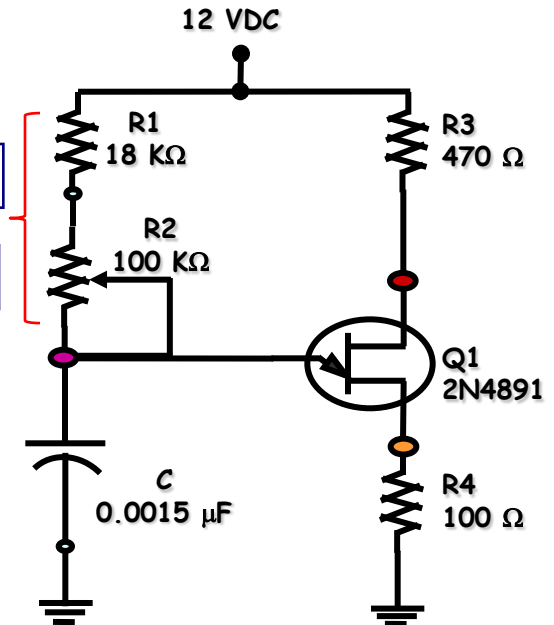
$$R_{\min} = R_1 + 0 = 18 \text{ k}\Omega$$

$$f = \frac{1}{RC \ln\left(\frac{1}{1-\eta}\right)}$$

$$\Rightarrow f_{\max} = \frac{1}{R_{\min} C \ln\left(\frac{1}{1-\eta}\right)}$$

$$= \frac{1}{18 \times 10^3 \times 0.0015 \times 10^{-6} \times \ln\left(\frac{1}{1-0.6}\right)} = 40 \text{ kHz}$$

$$\Rightarrow f_{\min} = \frac{1}{R_{\max} C \ln\left(\frac{1}{1-\eta}\right)} = \frac{1}{118 \times 10^3 \times 0.0015 \times 10^{-6} \times \ln\left(\frac{1}{1-0.6}\right)} = 6.16 \text{ kHz}$$



**Question 8** For the given UJT relaxation oscillator with  $V_{BB} = 30\text{V}$  and  $\eta = 0.6$ , calculate the output frequency and the voltage swing.

**Solution:**

$$V_P = 0.7 + \eta V_{BB}$$

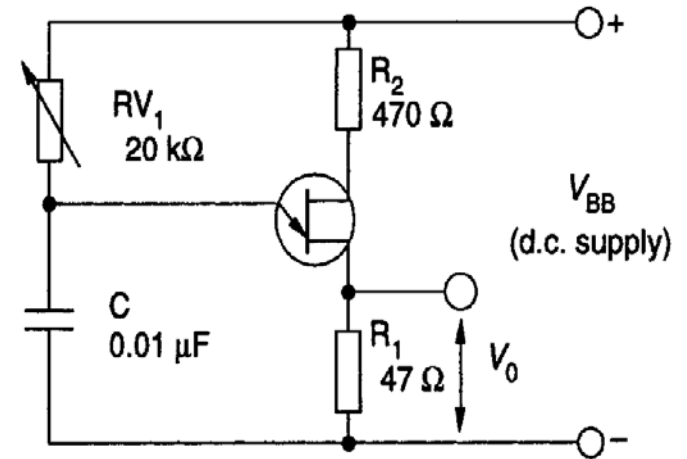
$$\Rightarrow V_P = 0.7 + 0.6 \times 30 = 18.7\text{V}$$

$$V_V \simeq 0.1 V_{BB} = 3\text{V}$$

$$f = \frac{1}{RC \ln\left(\frac{1}{1-\eta}\right)}$$

$$\Rightarrow f = \frac{1}{20 \times 10^3 \times 0.01 \times 10^{-6} \times \ln\left(\frac{1}{1-0.6}\right)} = 545\text{kHz}$$

$$V_{\text{swing}} = V_P - V_V \Rightarrow V_{\text{swing}} = 18.7 - 3 = 15.7\text{V}$$



## Question 9      Fill in the following blanks with suitable words.

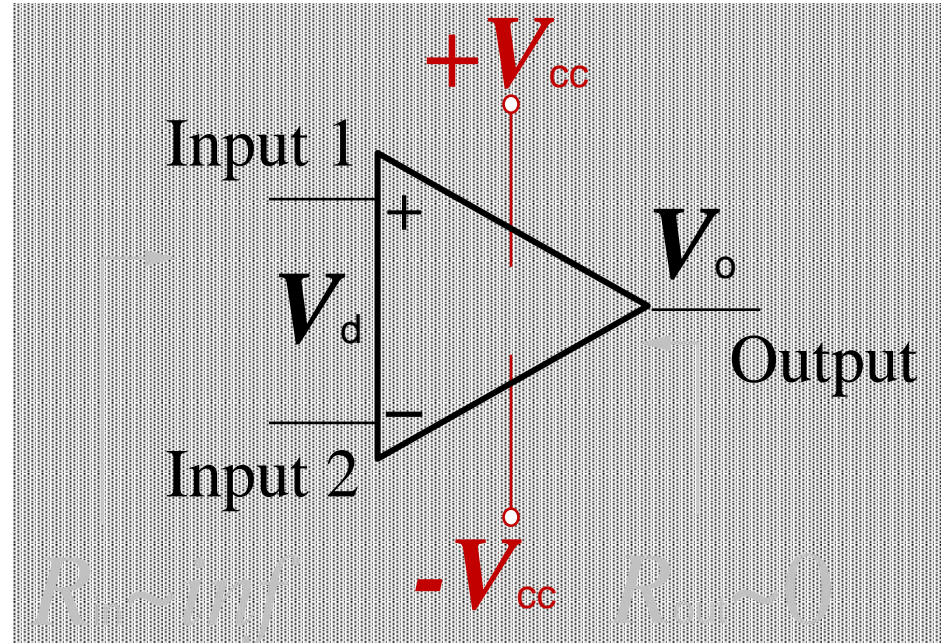
- 1) UJT is also called Double Base Diode.
- 2) Intrinsic standoff ratio is the coefficient of UJT that has typical values lie between 0.5 and 0.8.
- 3) UJT interbase resistance of  $N$  block of several thousands of Ohms when positive voltage is applied to B1 at reverse biased condition of the pn junction.
- 4) The condition of operation of UJT is:  $V_E = 0.7 + \eta V_{BB}$ .
- 5) The UJT has three operating regions as, cut-off region, negative resistance region, and saturation region.
- 6) The oscillation condition of UJT oscillator is:  $\frac{V_{BB} - V_V}{I_V} < R < \frac{V_{BB} - V_P}{I_P}$
- 7) Capacitor voltage during charging time of UJT oscillator can be expressed as:  $V_C = V_{BB} (1 - e^{-t/RC})$
- 8) The negative resistance region in the characteristic of the UJT makes it useful for constructing voltage oscillators.

# **Chapter 4**

## **The Operational Amplifier (Op-Amp)**

# The Operational Amplifier (Op-Amp )

- Very high differential gain  $G_d$ .
- High input impedance  $R_{in}$ .
- Low output impedance  $R_{out}$ .
- Provide voltage changes (amplitude and polarity).
- Used in oscillator, filter and instrumentation.
- Accumulate a very high gain by multiple stages.

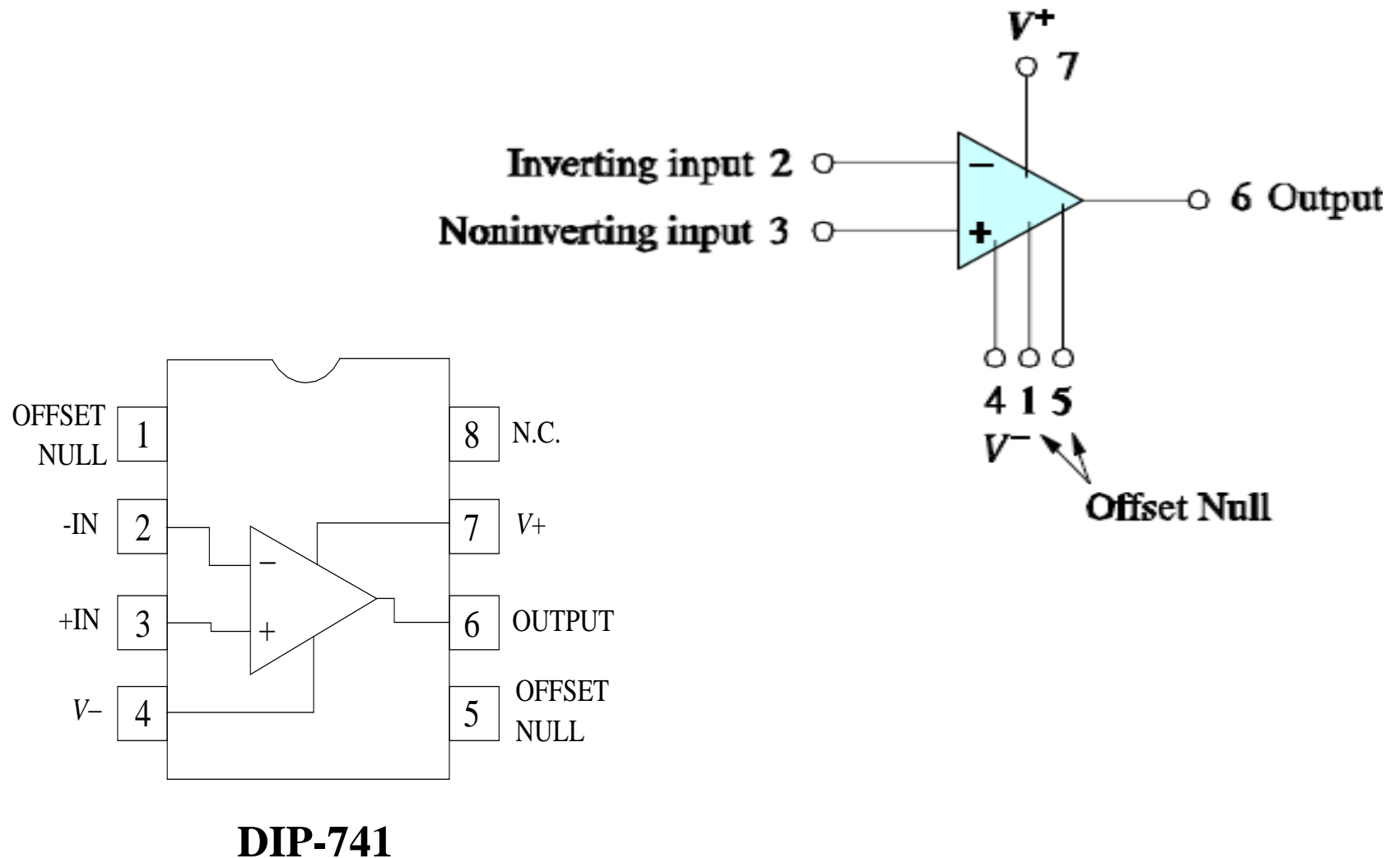


$$V_o = G_d V_d$$

$G_d$  : differential gain normally very large about  $10^5$



# ***The Op-Amp Symbol***



# Op-Amp Properties

## (1) Infinite Open Loop gain

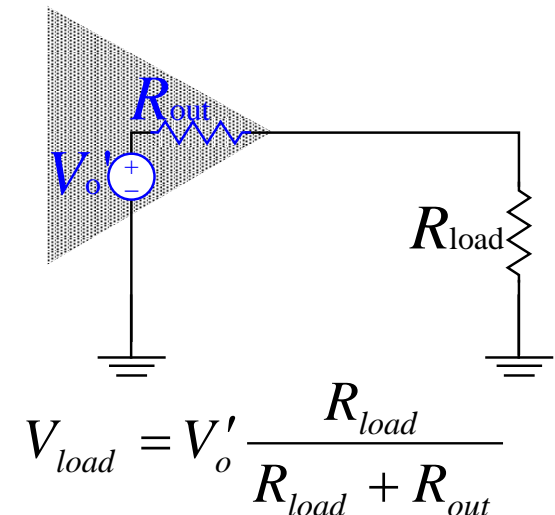
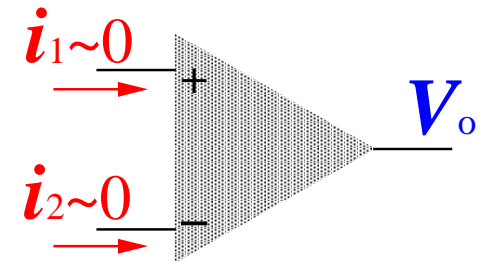
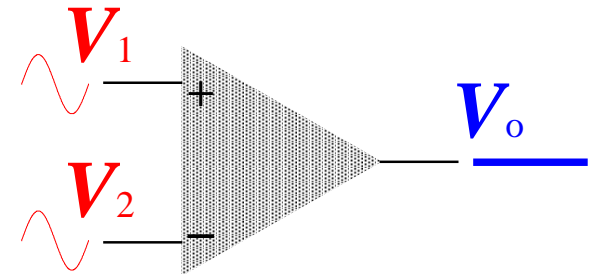
- The gain without feedback equal to  $G_d$ .
- Zero common-mode gain.
- Practically,  $G_d = 20,000$  to  $200,000$

## (2) Infinite Input impedance

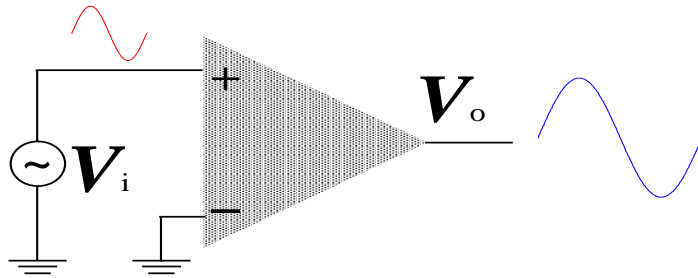
- Input current  $i_1, i_2 \sim 0A$
- $T\Omega$  in high-grade op-amp
- mA input current in low-grade op-amp

## (3) Zero Output Impedance

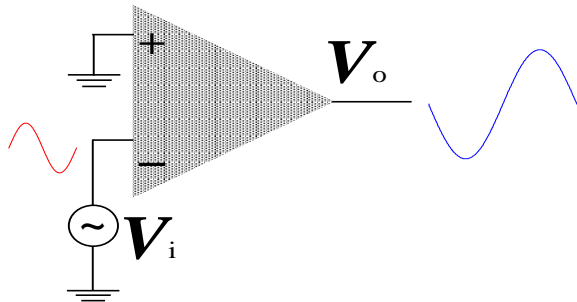
- act as perfect internal voltage source
- No internal resistance
- Output impedance in series with load
- Reducing output voltage to the load
- Practically,  $R_{out} \sim 20-100 \Omega$



## Single-Ended Input

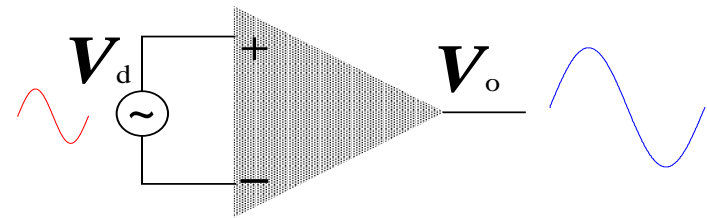
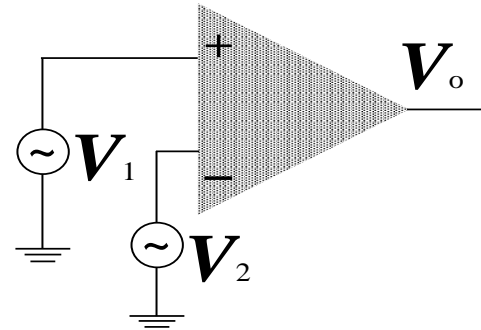


- + terminal : Source
- - terminal : Ground
- $0^\circ$  phase change



- + terminal : Ground
- - terminal : Source
- $180^\circ$  phase change

## Double-Ended Input

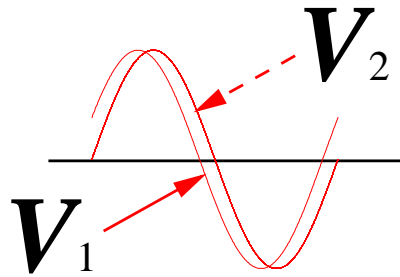


$$V_d = V_+ - V_-$$

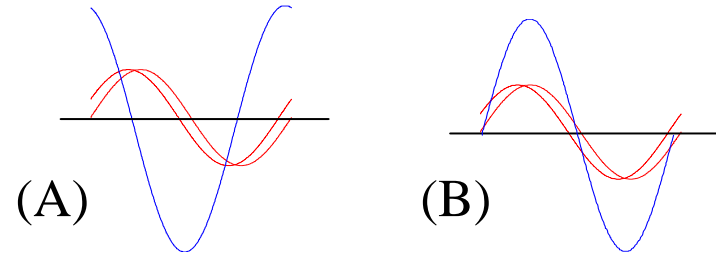
- Differential input  $V_d$ .
- $0^\circ$  phase shift change between  $V_o$  and  $V_d$

### Question:

Which of the following (A or B) is the output voltage  $V_o$  if the input voltages is given as:



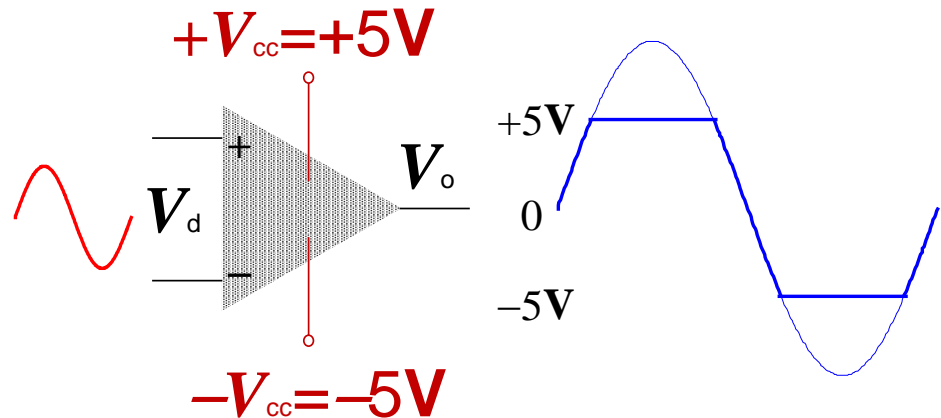
Input voltage



Output voltage (A or B) ?

### **Op-Amp Distortion**

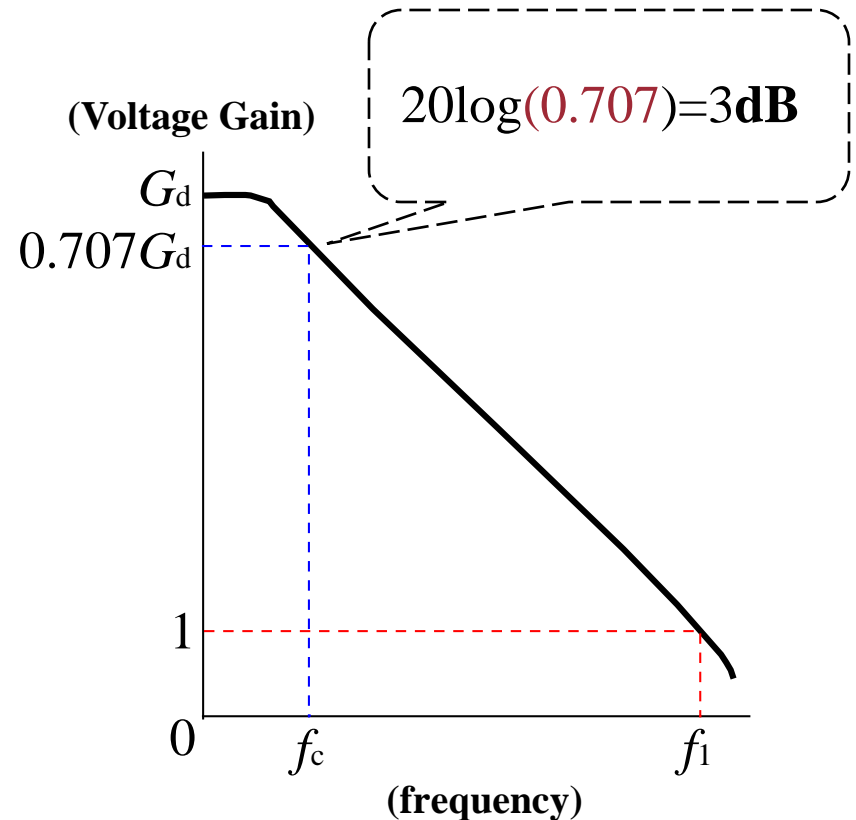
The output voltage never excess the DC biasing voltage of the Op-Amp.



# Frequency-Gain Relation

- Ideally, signals are amplified from DC to the highest AC frequency
- Practically, bandwidth is limited
- 741 family op-amp have a limit bandwidth of few KHz.
- Unity Gain frequency  $f_1$ : the gain at unity
- Cutoff frequency  $f_c$ : the gain drop by 3dB from dc gain  $G_d$
- Gain Bandwidth (GB) product is represented as:

$$\text{GB Product : } f_1 = G_d f_c$$



**Example 1:** Determine the cutoff frequency of an op-amp having a unit gain frequency  $f_1 = 10$  MHz and voltage differential gain  $G_d = 20\text{V/mV}$ .

**Solution:**

Since  $f_1 = 10$  MHz

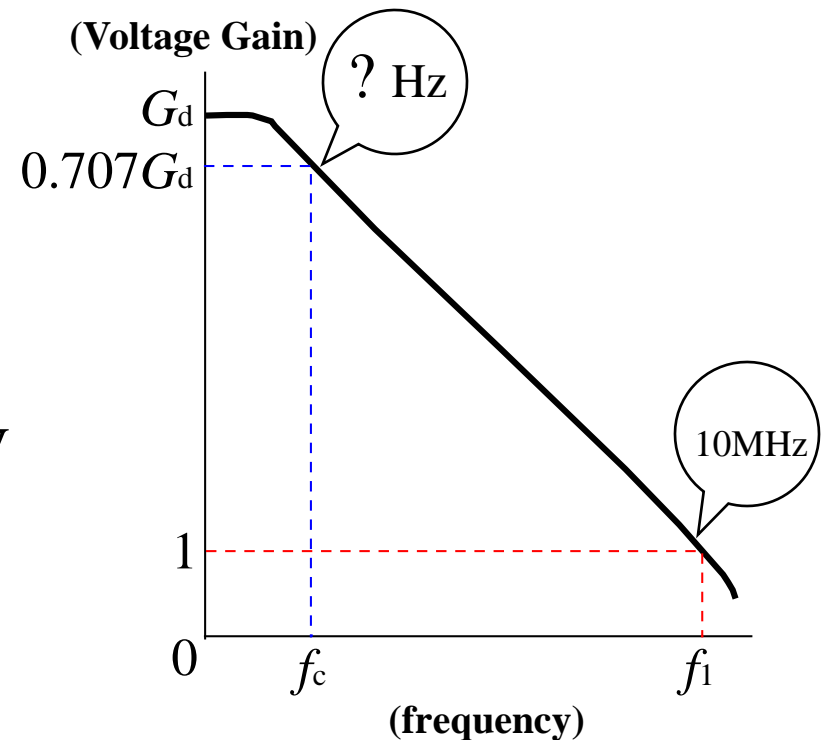
By using GB production equation

$$f_1 = G_d f_c$$

$$f_c = f_1 / G_d = 10 \text{ MHz} / 20 \text{ V/mV}$$

$$= 10 \times 10^6 / 20 \times 10^3$$

$$= 500 \text{ Hz}$$



# *Ideal Op-Amp Applications*

## **Analysis Method :**

Two ideal Op-Amp Properties:

- (1) The voltage between  $V_+$  and  $V_-$  is zero  $V_+ = V_-$
- (2) The current into both  $V_+$  and  $V_-$  terminals is zero.

For ideal Op-Amp circuit:

- (1) Write the Kirchhoff node equation at the non inverting terminal  $V_+$
- (2) Write the Kirchhoff node equation at the inverting terminal  $V_-$
- (3) Set  $V_+ = V_-$  and solve for the desired closed-loop gain

# Non-Inverting Amplifier

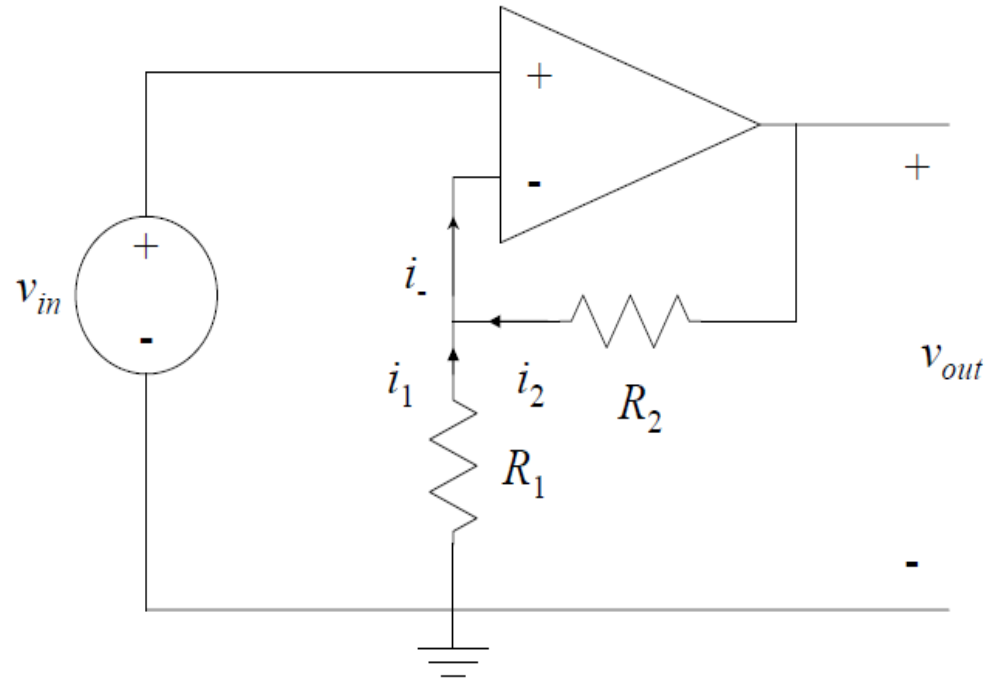
## KCL at the Inverting Input

$$i_- = 0$$

$$i_1 = \frac{-v_-}{R_1} = \frac{-v_{in}}{R_1}$$

Since  $v_- = v_+ = v_{in}$

$$i_2 = \frac{v_{out} - v_-}{R_2} = \frac{v_{out} - v_{in}}{R_2}$$



## Solve for $V_{out}$

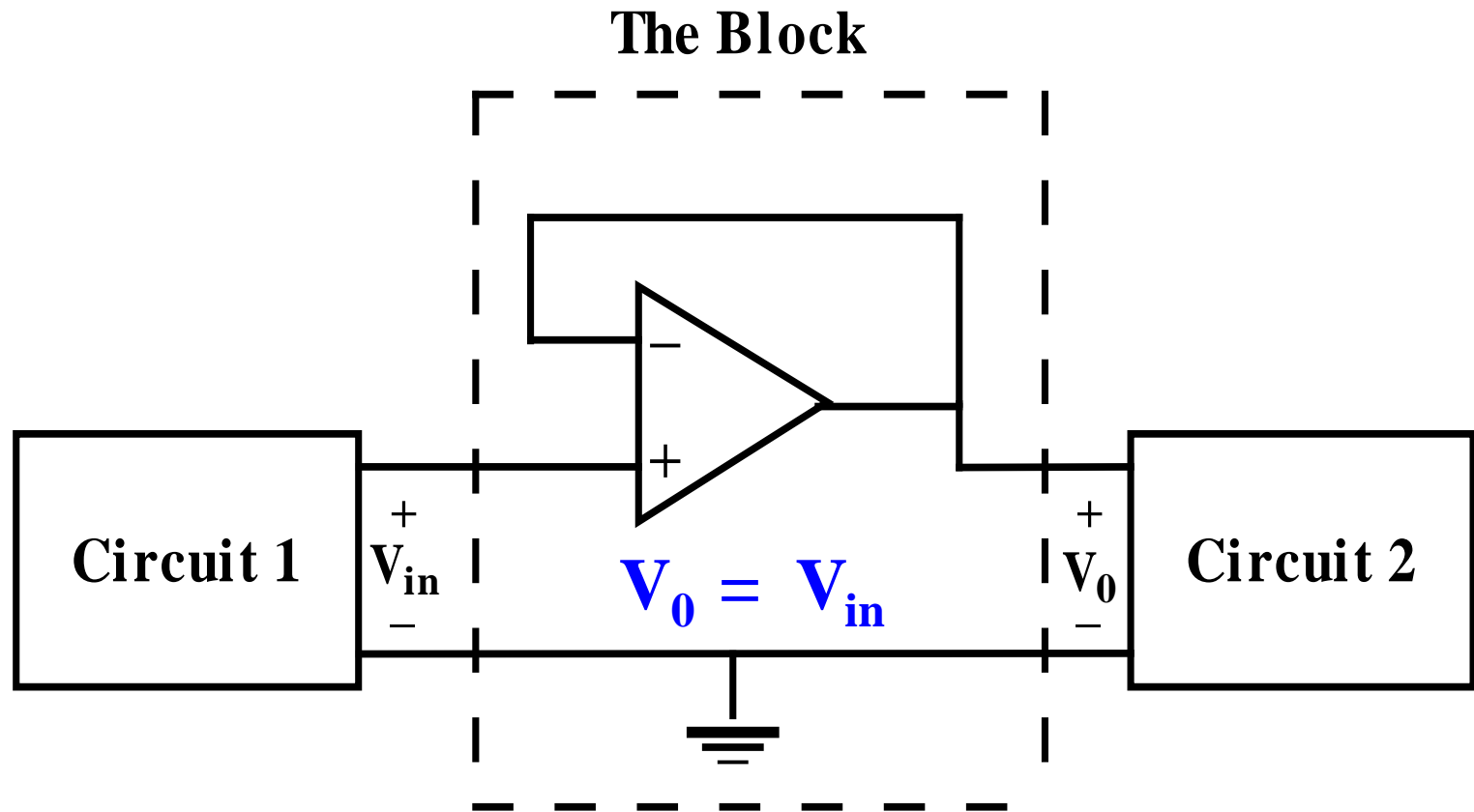
$$\frac{-v_{in}}{R_1} + \frac{v_{out} - v_{in}}{R_2} = 0$$



$$v_{out} = v_{in} \left( 1 + \frac{R_2}{R_1} \right)$$

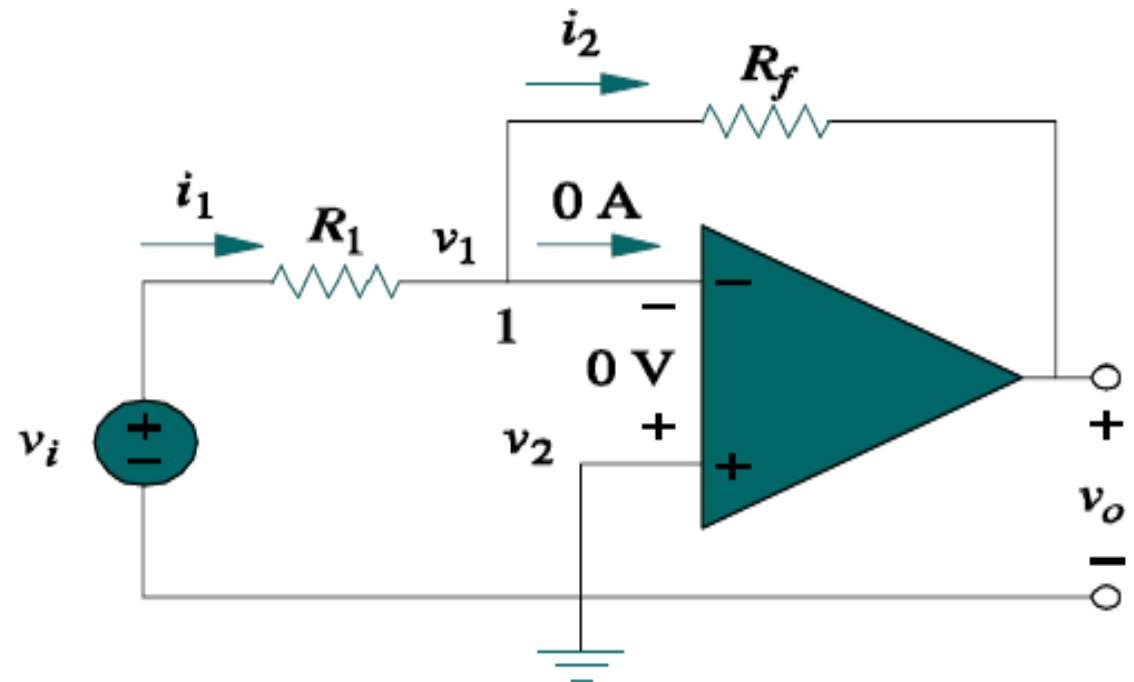


# *Isolation or Voltage Follower*



**Circuit isolation with an op-amp.**

# Inverting Amplifier



Since the noninverting terminal is grounded

$$v_1 = v_2 = 0$$

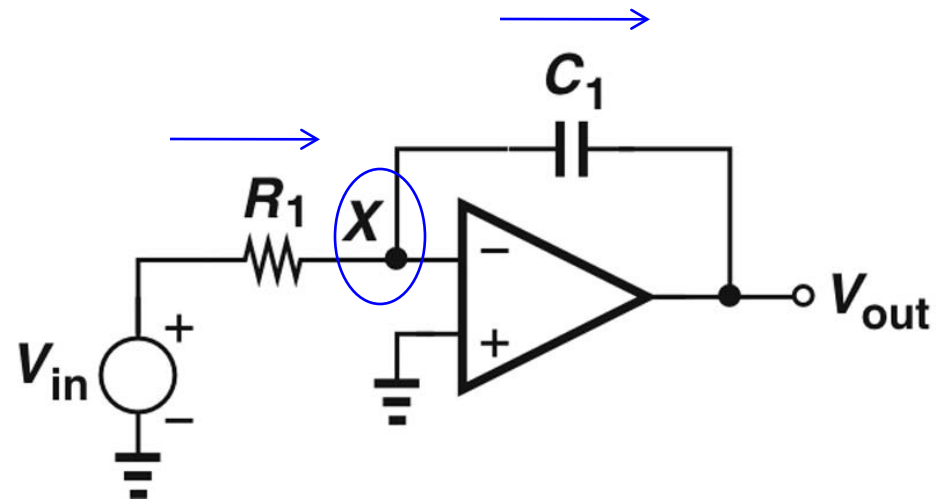
$$\text{KCL at } v_1: i_1 = i_2 \Rightarrow \frac{v_i - 0}{R_1} = \frac{0 - v_o}{R_f}$$



$$v_o = -\frac{R_f}{R_1} v_i$$

# Op-Amp Integrator

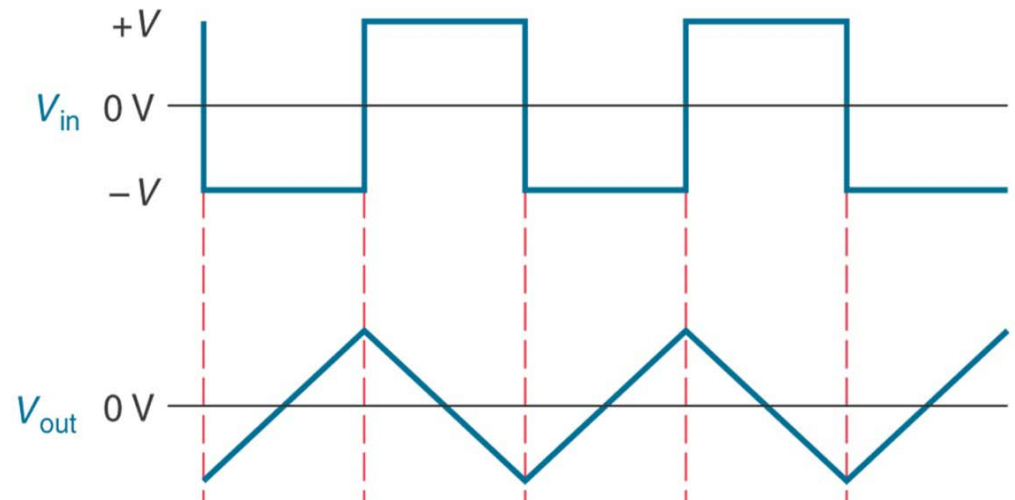
- The op-amp provides a constant-current source for the capacitor, causing it to charge at a linear rate.
- It is used as Low Pass Filter.



At point X

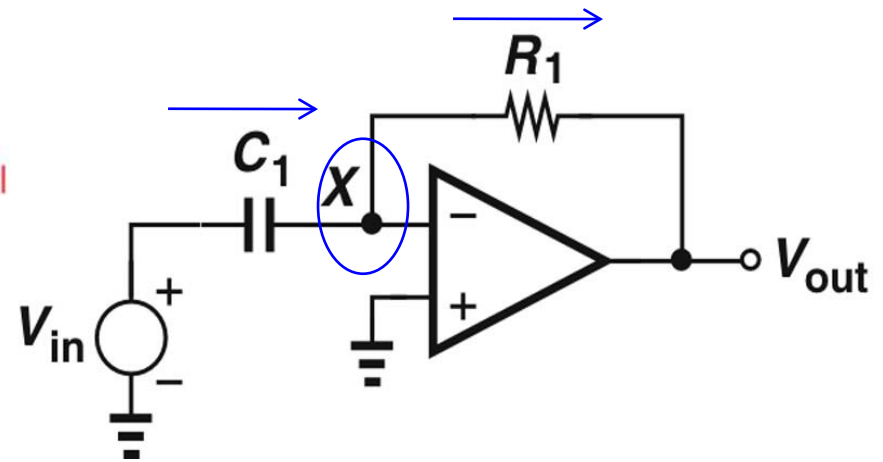
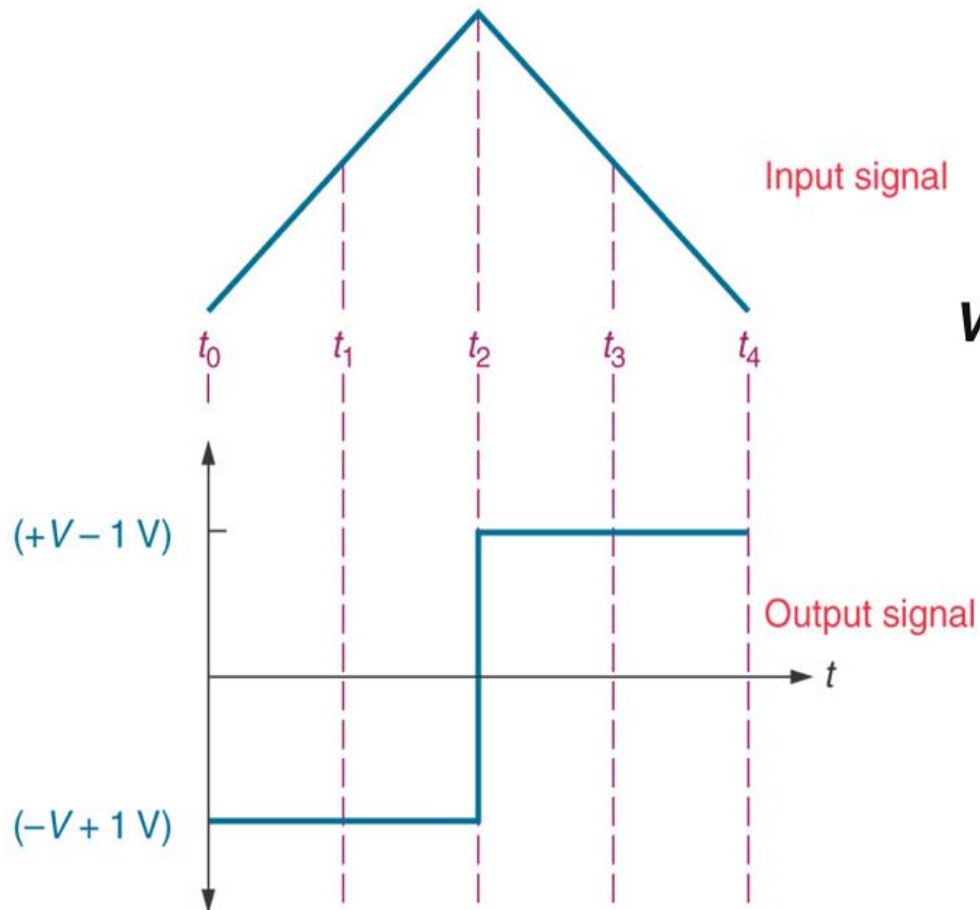
$$\frac{V_{in}}{R_1} = -C_1 \frac{dV_{out}}{dt}$$

$$V_{out} = -\frac{1}{R_1 C_1} \int V_{in} dt$$



# Op-Amp Differentiator

- The output signal is proportional to the rate of change of input signal.
- It is used as High Pass Filter.



At point X

$$C_1 \frac{dV_{in}}{dt} = - \frac{V_{out}}{R_1}$$

# Op-Amp with Multiple Inputs

## Noninverting Summer

At the noninverting input:

$$i_1 + i_2 + i_3 = 0$$

$$i_1 = \frac{v_1 - v_+}{R_1}$$

$$i_2 = \frac{v_2 - v_+}{R_2} \quad i_3 = \frac{v_3 - v_+}{R_3}$$

At the inverting input:

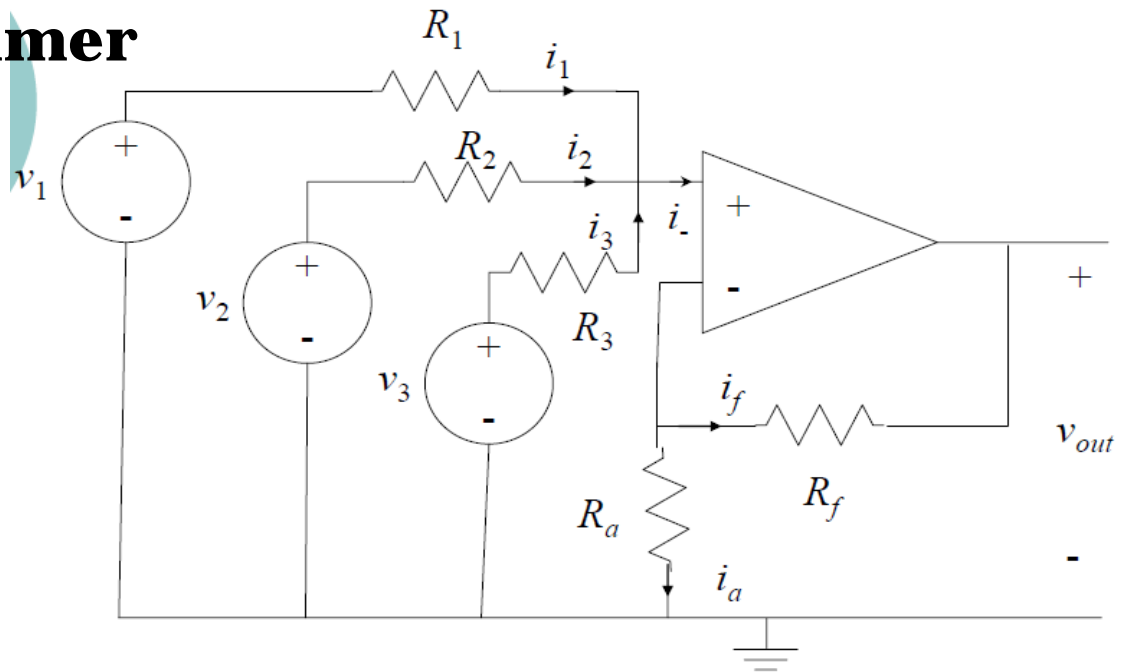
$$i_f + i_a = 0$$

$$i_f = \frac{v_- - v_{out}}{R_f}$$

$$i_a = \frac{v_-}{R_a}$$

$$v_- = \frac{R_a}{R_a + R_f} v_{out}$$

$$v_- = v_+$$



$$\frac{v_1}{R_1} + \frac{v_2}{R_2} + \frac{v_3}{R_3} = \left( \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right) v_+ \quad \frac{1}{R_T} = \left( \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right)$$

$$\frac{v_1}{R_1} + \frac{v_2}{R_2} + \frac{v_3}{R_3} = \frac{1}{R_T} \frac{R_a}{R_a + R_f} v_{out}$$

$$v_{out} = \left( 1 + \frac{R_f}{R_a} \right) \left( \frac{R_T}{R_1} v_1 + \frac{R_T}{R_2} v_2 + \frac{R_T}{R_3} v_3 \right)$$

# Inverting Summer

KCL at the Inverting Input

$$i_1 = \frac{v_1 - v_-}{R_1} = \frac{v_1}{R_1}$$

$$i_2 = \frac{v_2 - v_-}{R_2} = \frac{v_2}{R_2}$$

$$i_3 = \frac{v_3 - v_-}{R_3} = \frac{v_3}{R_3}$$

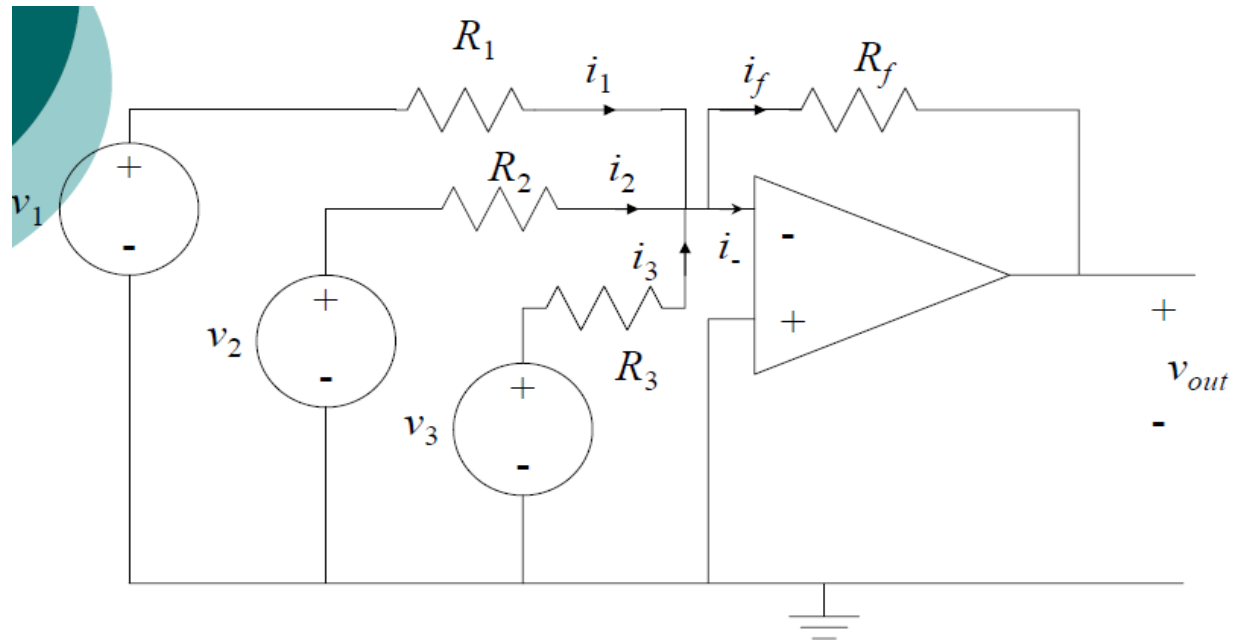
$$i_- = 0$$

$$i_f = \frac{v_{out} - v_-}{R_f} = \frac{v_{out}}{R_f}$$

$$\frac{v_1}{R_1} + \frac{v_2}{R_2} + \frac{v_3}{R_3} + \frac{v_{out}}{R_f} = 0$$

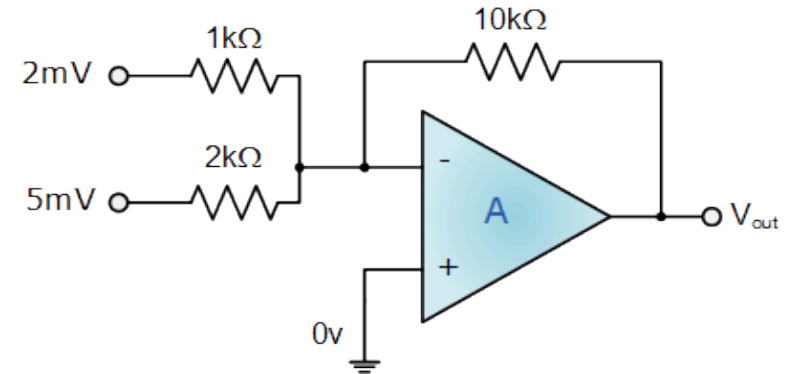


$$v_{out} = -\frac{R_f}{R_1}v_1 - \frac{R_f}{R_2}v_2 - \frac{R_f}{R_3}v_3$$



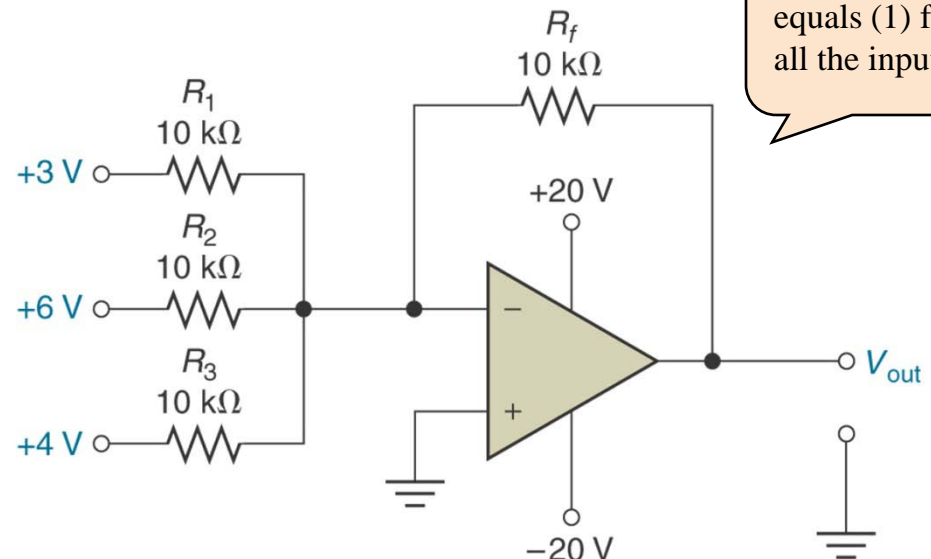
**Example 2** Calculate  $V_{out}$  for the following summing circuit.

$$\begin{aligned}
 V_{out} &= -R_f \left( \frac{V_1}{R_1} + \frac{V_2}{R_2} \right) \\
 &= -10 \times 10^3 \left( \frac{2 \times 10^{-3}}{1 \times 10^3} + \frac{5 \times 10^{-3}}{2 \times 10^3} \right) \\
 &= -10 \times 10^3 (2 \times 10^{-6} + 2.5 \times 10^{-6}) = 45 \times 10^{-3} \text{ V} = 45 \text{ mV}
 \end{aligned}$$



**Example 3** Determine  $V_{out}$  for the following summing circuit.

$$\begin{aligned}
 V_{out} &= -R_f \left( \frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} \right) \\
 &= -13 \text{ V}
 \end{aligned}$$



Voltage gain equals (1) for all the inputs.

## Example 4

Design op-amp summing circuit to satisfy the following equation:  
 $V_{\text{out}} = 0.2 V_1 + 0.25 V_2 - V_3$ . (Assume  $R_f = 10\text{k}\Omega$ )

### Design steps:

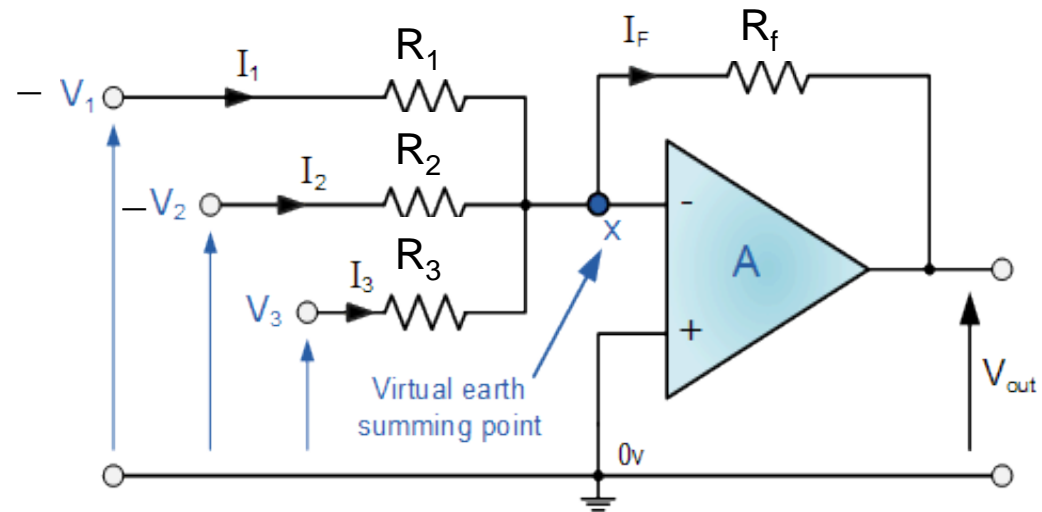
- ❖ Draw the summing circuit that has three input voltages and three resistances and reverse the sign of the three inputs as shown.
- ❖ Calculate the values of the three resistances by matching the summer equation with the given one as:

$$V_{\text{out}} = -\frac{R_f}{R_1}V_1 - \frac{R_f}{R_2}V_2 - \frac{R_f}{R_3}V_3$$

$$\frac{R_f}{R_1} = 0.2 \Rightarrow R_1 = \frac{10\text{k}\Omega}{0.2} = 50\text{k}$$

$$\frac{R_f}{R_2} = 0.25 \Rightarrow R_2 = \frac{10\text{k}\Omega}{0.25} = 40\text{k}$$

$$\frac{R_f}{R_3} = 1 \Rightarrow R_3 = \frac{10\text{k}\Omega}{1} = 10\text{k}$$



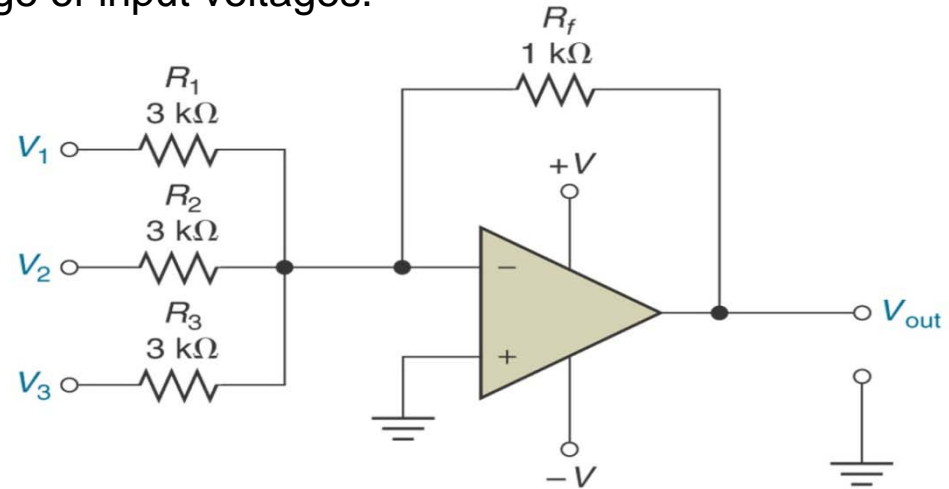


## Averaging Amplifier

**Averaging amplifier** – is a summing amplifier with proper input and feedback resistors, that provides an output proportional to the average of input voltages.

### Example 5

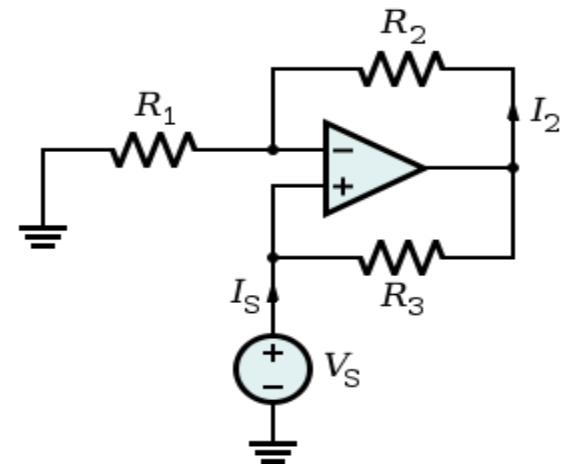
$$-V_{out} = \frac{1}{3}V_1 + \frac{1}{3}V_2 + \frac{1}{3}V_3$$
$$\therefore -V_{out} = \frac{V_1 + V_2 + V_3}{3}$$



## Negative Impedance Converter NIC

- Creates a negative resistor for any signal generator.
- The ratio between input voltage and input current (input resistance) is given by:

$$R_{in} = -R_3 \left( \frac{R_1}{R_2} \right)$$



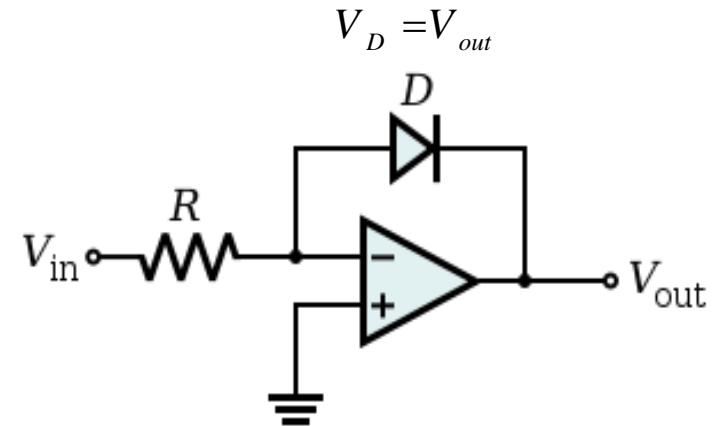
## Logarithmic op-amp

$$\frac{V_{in}}{R} = I_R = I_D$$

$$I_D = I_S \left( e^{(V_D/V_T)} - 1 \right) \approx I_S e^{(V_D/V_T)}$$

$$V_{out} = -V_T \ln \left( \frac{V_{in}}{I_S R} \right)$$

Where:  $I_S$  is the saturation current and  $V_T$  is the thermal voltage.

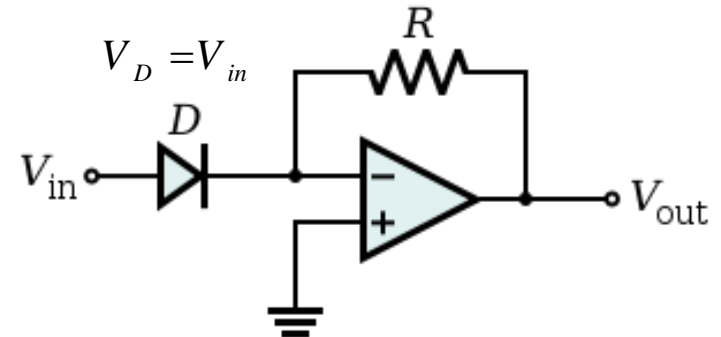


## Op-amp Exponential Amplifier

Considering ideal op-amp, the negative pin is virtually grounded, so the current through the diode is given by:

$$I_D = I_S \left( e^{(V_D/V_T)} - 1 \right) \approx I_S e^{(V_D/V_T)}$$

$$V_{out} = -RI_D = -RI_S e^{(V_{in}/V_T)}$$



# Voltage Subtractor

$$I_1 = \frac{V_1 - V_a}{R_1}, \quad I_2 = \frac{V_2 - V_b}{R_2}, \quad I_f = \frac{V_a - (-V_{out})}{R_3}$$

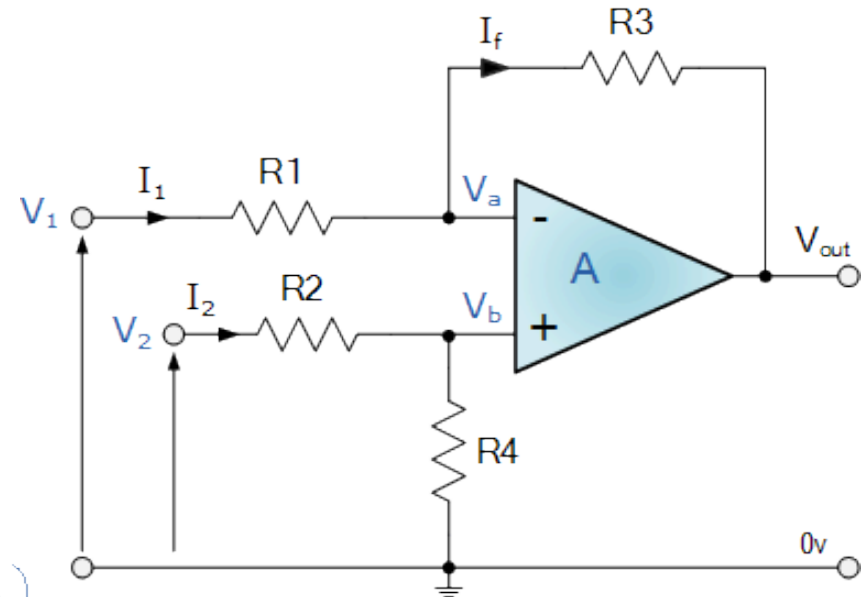
Summing point  $V_a = V_b$

If  $V_b = 0$ , then:  $V_{out(a)} = -V_1 \left( \frac{R_3}{R_3 + R_1} \right) = -V_1 \left( \frac{R_3}{R_1} \right)$

If  $V_a = 0$ , then:  $V_{out(b)} = V_2 \left( \frac{R_4}{R_2 + R_4} \right) \left( 1 + \frac{R_3}{R_1} \right)$

$$V_{out} = V_{out(a)} + V_{out(b)}$$

$$\therefore V_{out} = -V_1 \left( \frac{R_3}{R_1} \right) + V_2 \left( \frac{R_4}{R_2 + R_4} \right) \left( 1 + \frac{R_3}{R_1} \right)$$



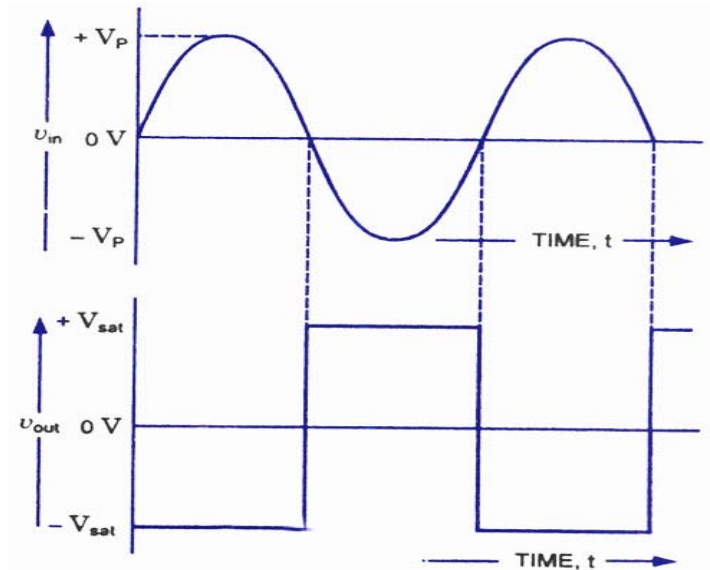
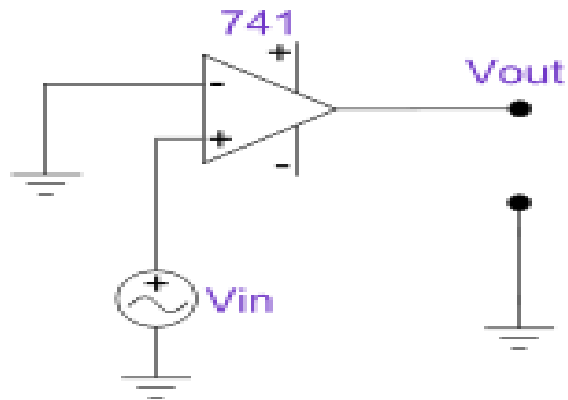
If  $R_1 = R_2$  and  $R_3 = R_4$

$$V_{out} = \frac{R_3}{R_1} (V_2 - V_1)$$

If  $R_1 = R_2 = R_3 = R_4$

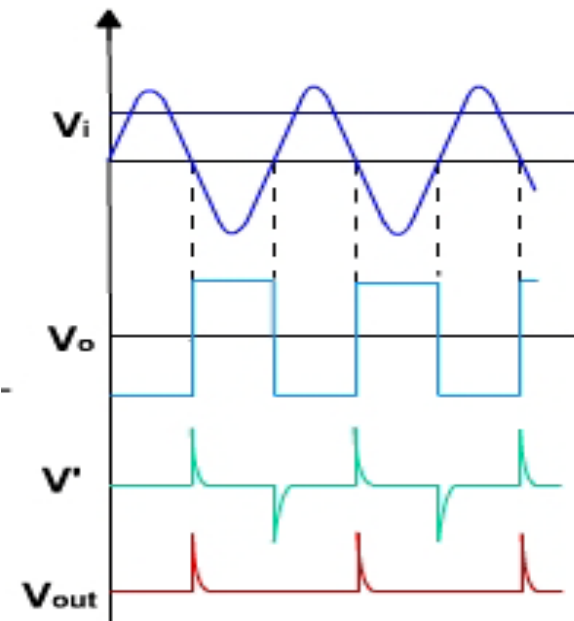
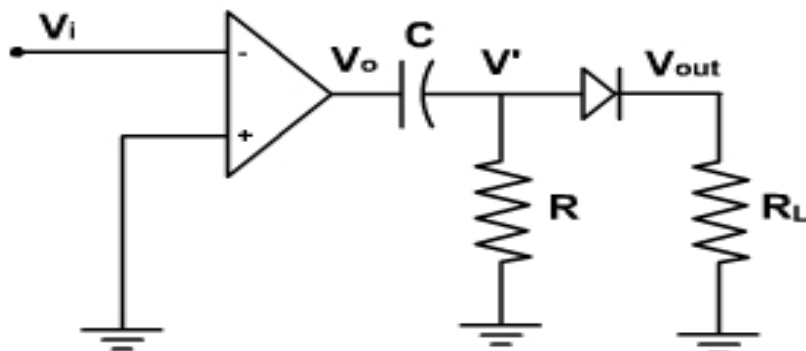
$$V_{out} = V_2 - V_1$$

# Zero Crossing Detector

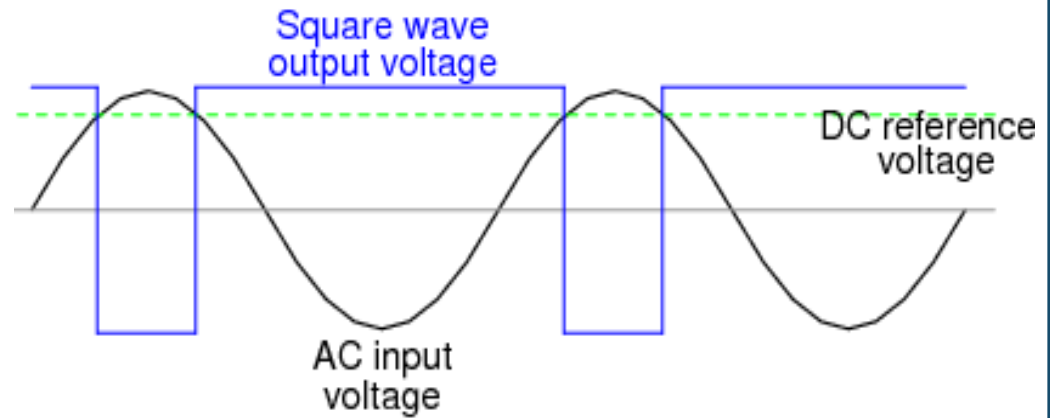
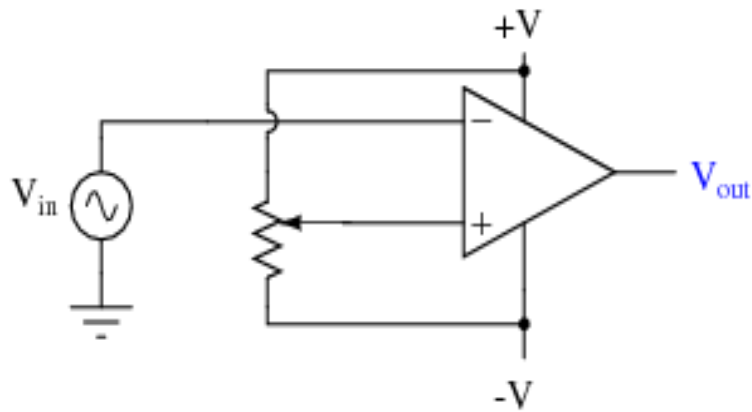


*Input and Output Waveforms*

**Zero crossing detector  
supplies trigger pulses**

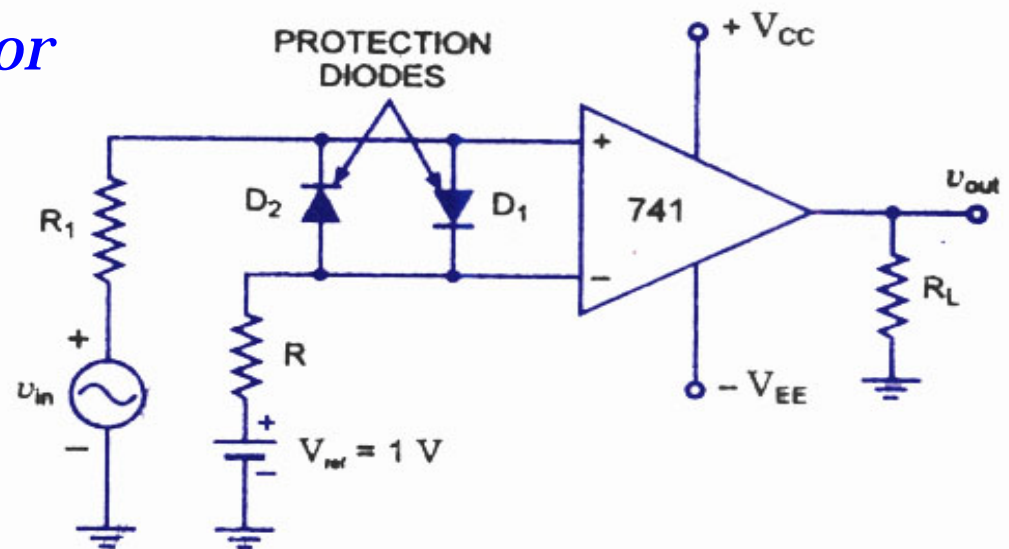


## *Inverting Comparator*



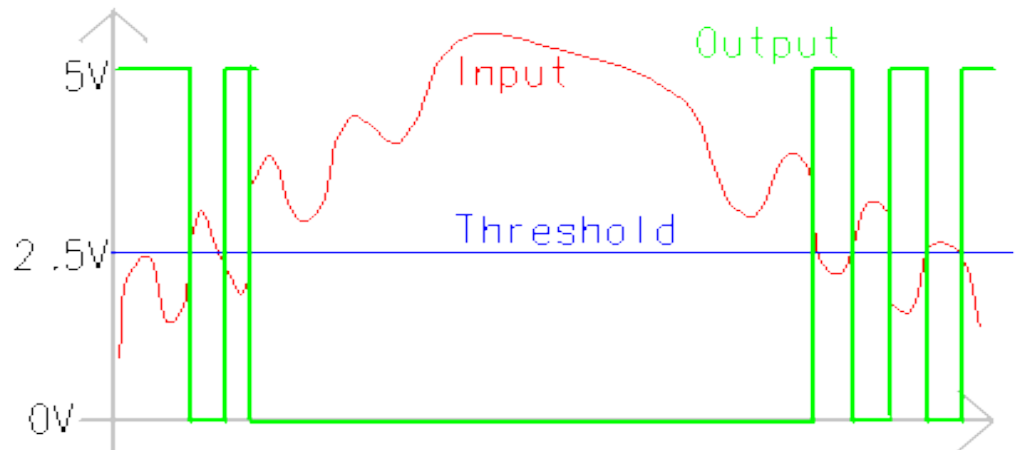
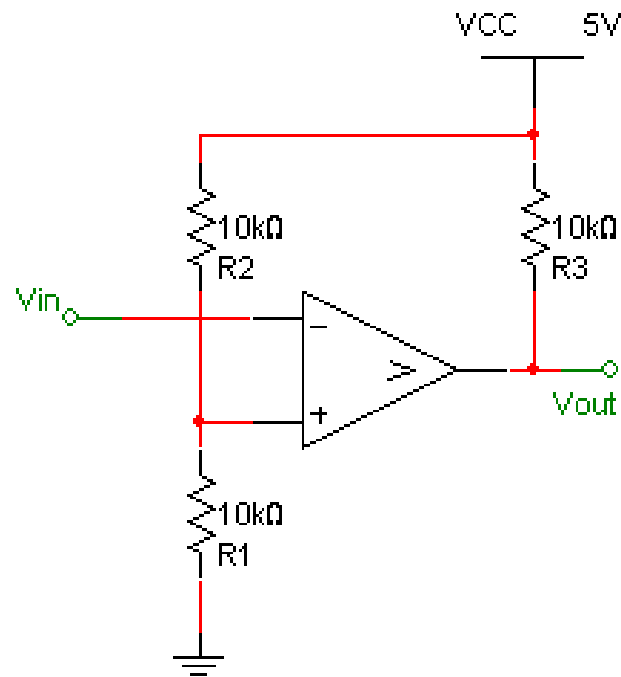
*A "clean" AC input waveform produces predictable transition points on the output voltage square wave*

## *Noninverting Comparator*



## Example 6

Inverting comparator circuit using op-amp and threshold voltage of 2.5 volt.

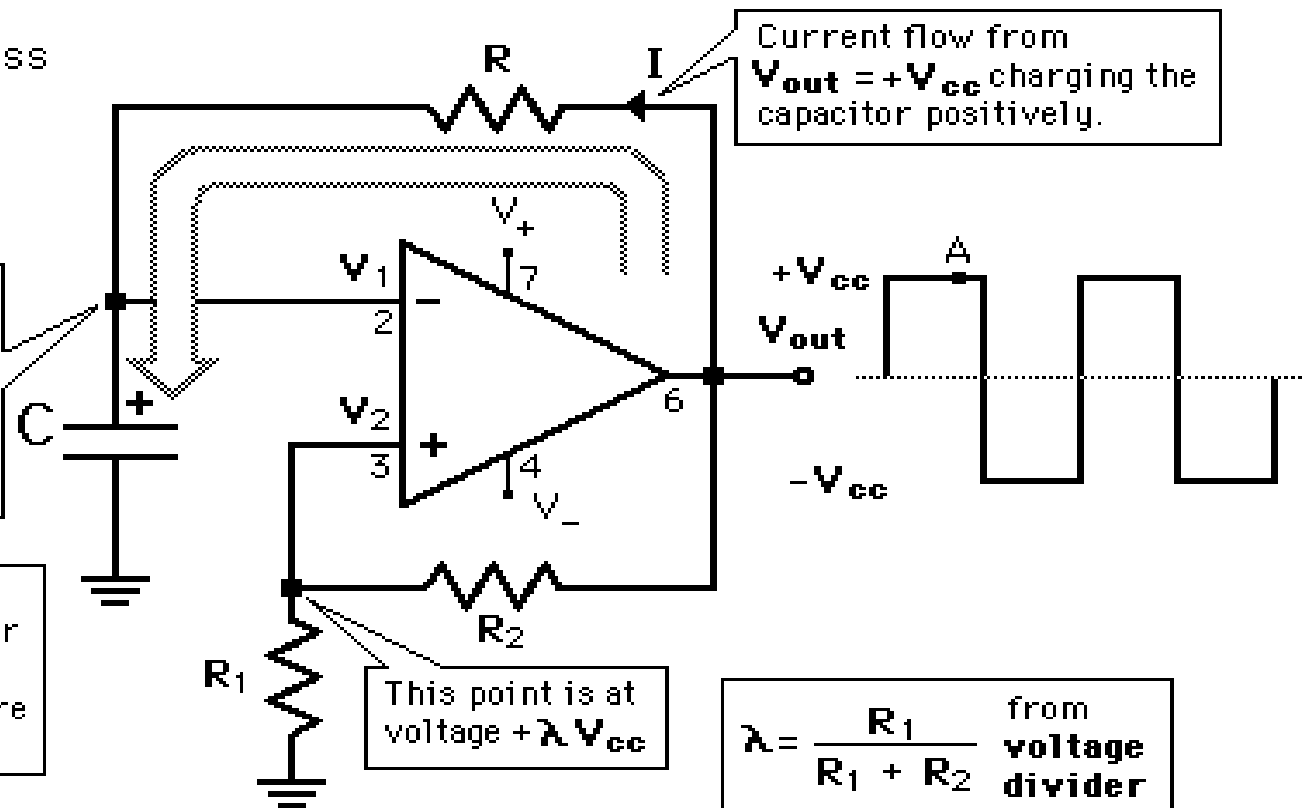


# Square Wave Generator

Follow the progress from a time when the output is at point A.

This point charging toward the voltage  $+\lambda V_{cc}$  at which the **comparator** action will flip the output to  $-V_{cc}$

The values of the resistors and capacitor determine the rate of discharge and therefore the **period**.



# Schmitt Trigger

Switching occurs when:

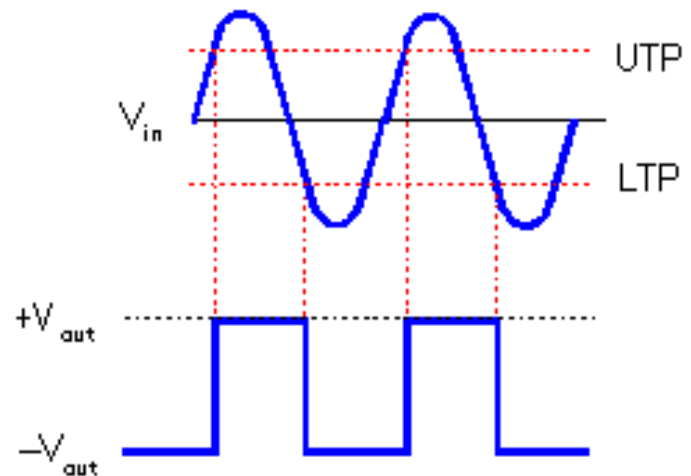
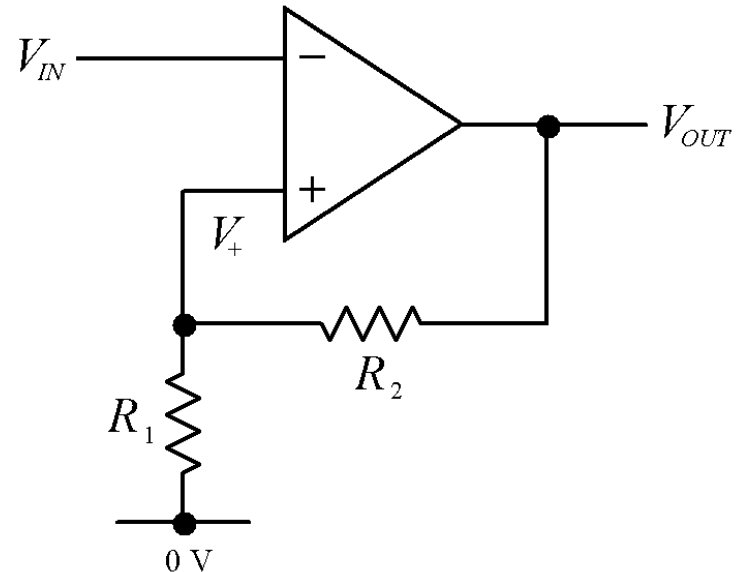
$$V_{IN} = V_- = V_+ = V_{OUT} \frac{R_1}{R_1 + R_2}$$

But,

$$V_{OUT} = \pm V_{SAT}$$

$\therefore$  Threshold input voltage  
for upper trigger point (UTP)  
and lower trigger point (LTP)

$$V_{IN} = \pm V_{SAT} \frac{R_1}{R_1 + R_2}$$





# Problems and Solutions

## Question 1

- (a) Derive an expression for  $(V_{out} / V_{in})$  for the inverting op-amp amplifier in terms of  $R_1$  and  $R_f$  .  
 (b) Inverting op-amp amplifier with 1kHz sine wave input of 2 volts peak-to-peak,  $R_1 = R_f = 10k\Omega$ .  
 1. Calculate  $V_{out}$ . 2. Draw the input and output waveforms ( $V_{in}$  and  $V_{out}$ ).

### Solution:

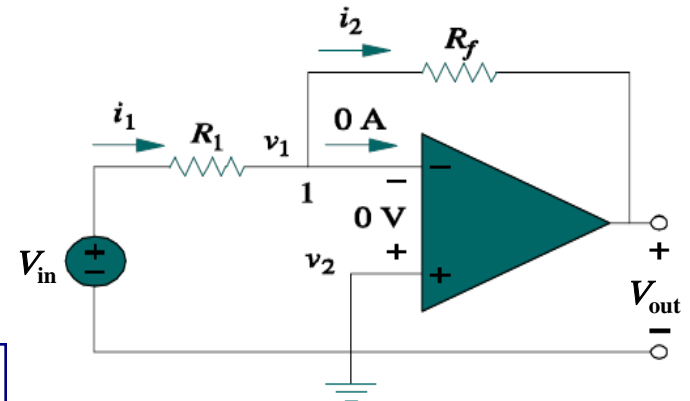
- (a) Since the non-inverting terminal is grounded:

$$v_1 = v_2 = 0$$

Also for the op-amp, we have:  $i_- = i_+ = 0$

Using KCL at the node 1 we get:

$$i_1 = i_2 \Rightarrow \frac{V_{in} - 0}{R_1} = \frac{0 - V_{out}}{R_f} \Rightarrow \therefore \frac{V_{out}}{V_{in}} = -\frac{R_f}{R_1}$$

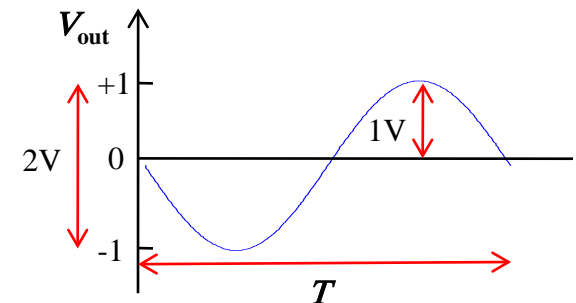
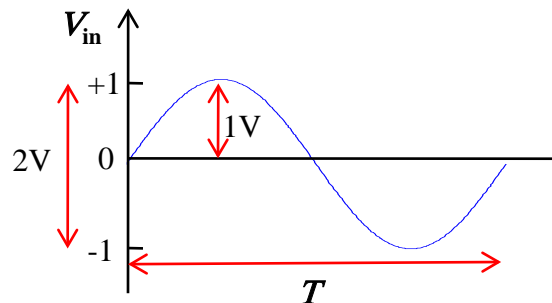


- (b)

$$V_{out} = -\frac{R_f}{R_1} V_{in}$$

$$V_{out} = -\frac{10 \times 10^3}{10 \times 10^3} \times 2$$

$$V_{out} = -2 \text{ volt}$$

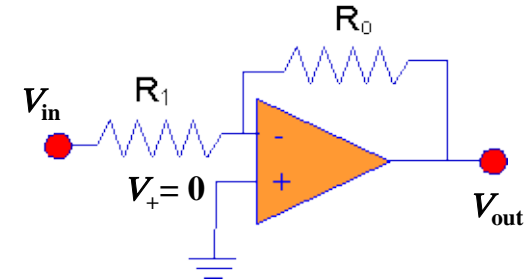


$$T = \frac{1}{f} = \frac{1}{1 \times 10^3} = 1 \text{ m sec}$$

**Question 2** For the following op-amp circuit with gain of  $A = -10$ , find the output voltage  $V_{out}$  if the input voltage  $V_{in} = 0.24$  volt .

**Solution:**

$$V_{out} = -\frac{R_0}{R_1}V_{in} = -10 \times 0.24 = -2.4 \text{ volt}$$



**Question 3** Inverting amplifier with  $R_f = 4700\Omega$  , find the value of  $R_1$  that produce gain of  $A = -5$ .

**Solution:**

The gain of inverting amplifier is:  $A = -\frac{R_f}{R_1} \Rightarrow R_1 = -\frac{R_f}{A} = -\frac{4700}{-5} = 940\Omega$

**Question 4** An op-amp has a differential gain  $G_d = 250,000$ . If the output voltage  $V_{out} = 3.75$  volt, find the difference between input voltages  $V_d$ .

**Solution:**

$$V_{out} = G_d V_{in}$$

$$V_{in} = \frac{V_{out}}{G_d} = \frac{3.75}{250,000} = 15 \times 10^{-6} \text{ volt} = 15\mu V$$

**Question 5** Calculate the voltage gain for each stage (  $A_1$  and  $A_2$  ) of the given amplifier circuit and then find the overall voltage gain  $A$ .

**Solution:**

The gain of any single stage non-inverting amplifier is:

$$A = \frac{V_{out}}{V_{in}} = \left( 1 + \frac{R_f}{R_1} \right)$$

The gain of stage 1 is:

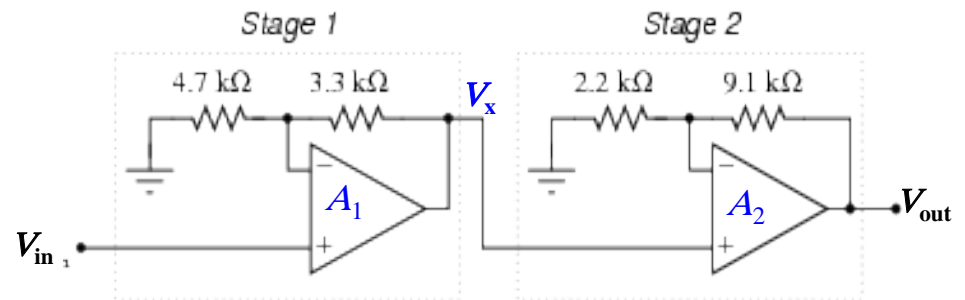
$$A_1 = \frac{V_x}{V_{in_1}} = \left( 1 + \frac{3300}{4700} \right) = 1.702$$

The gain of stage 2 is:

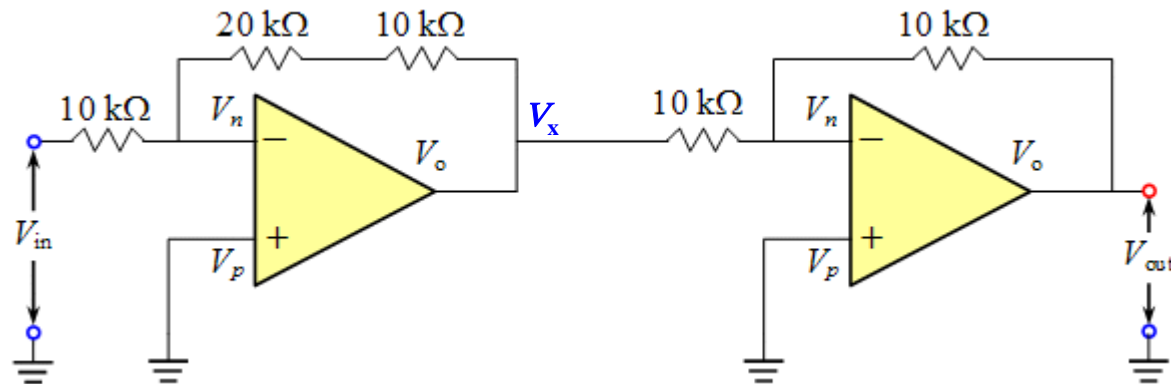
$$A_2 = \frac{V_{out}}{V_x} = \left( 1 + \frac{9100}{2200} \right) = 5.136$$

Thus, the overall gain is:

$$A = \frac{V_{out}}{V_{in}} = \frac{V_x}{V_{in}} \times \frac{V_{out}}{V_x} = A_1 \times A_2 = 1.702 \times 5.136 = 8.74$$



**Question 6** For the given circuit, calculate the output voltage  $V_{out}$  if the input voltage  $V_{in} = 1.5$  volt .



**Solution:**

The gain of any single stage inverting amplifier is:

$$A = -\frac{R_f}{R_1}$$

When  $V_{in} = 1.5\text{ V}$ , The output voltage of first stage is:

$$V_x = \left( -\frac{20 \times 10^3 + 10 \times 10^3}{10 \times 10^3} \right) \times V_{in} = (-3) \times 1.5 = -4.5\text{ Volt}$$

Therefore, the output voltage  $V_{out}$  at second stage is:

$$V_{out} = \left( -\frac{10 \times 10^3}{10 \times 10^3} \right) \times V_x = (-1) \times (-4.5) = 4.5\text{ Volt}$$

**Question 7** For the given circuit, determine  $V_1$  and  $V_2$ , and the output voltage  $V_{out}$ .

**Solution:**

The gain of any single stage inverting amplifier is:

$$A = -\frac{R_f}{R_1}$$

$$\therefore V_1 = \left( -\frac{2 \times 10^3}{2 \times 10^3} \right) \times V_{in} = (-1) \times 2 = -2 \text{ Volt}$$

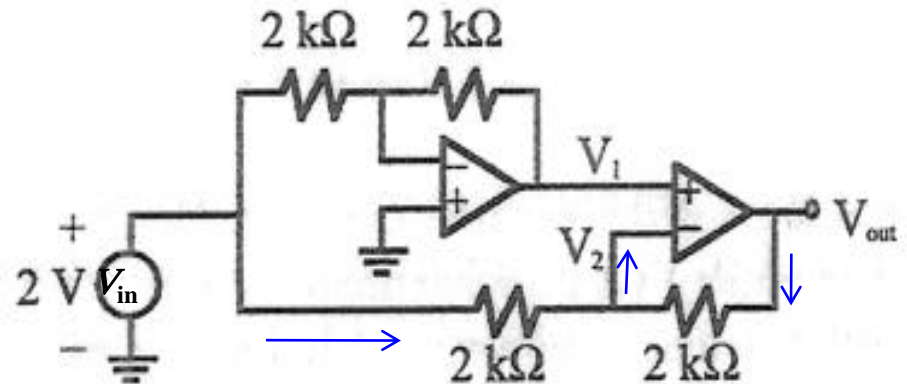
For ideal op-amp we have:  $V_1 = V_2 = -2 \text{ Volt}$

Also for the op-amp, we have:  $i_+ = i_- = 0$

Using KCL at node  $V_2$ , we get:

$$\frac{V_{in} - V_2}{2 \text{ k}\Omega} + \frac{V_{out} - V_2}{2 \text{ k}\Omega} = i_- = 0$$

$$\therefore V_{out} = V_2 + V_2 - V_{in} = -2 - 2 - (2) = -6 \text{ Volt}$$



**Question 8** For the given non-inverting op-amp, find the output voltage  $V_{out}$ .

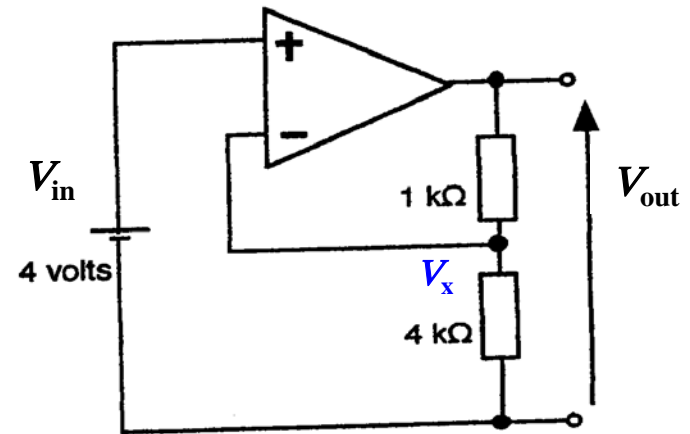
**Solution:**  $i_+ = i_- = 0$

$$v_x = v_- = v_+ = V_{in} = 4 \text{ Volt}$$

Using the voltage divider equation at node " $V_x$ ":

$$V_x = \left( \frac{4 \text{ k}\Omega}{4 \text{ k}\Omega + 1 \text{ k}\Omega} \right) V_{out}$$

$$\therefore V_{out} = \frac{5}{4} \times V_x = \frac{5}{4} \times 4 = 5 \text{ Volt}$$



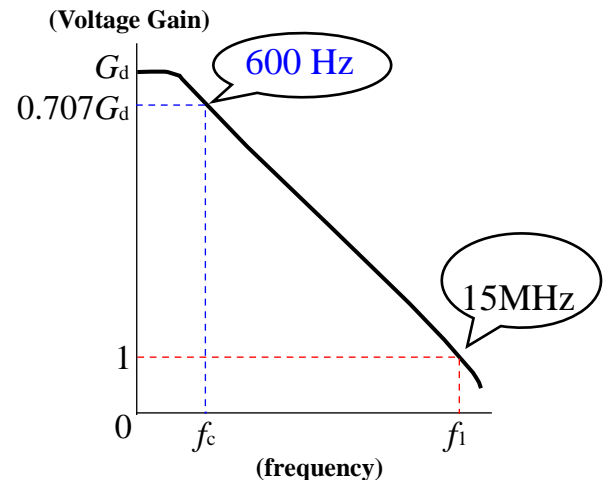
**Question 9** Determine the cutoff frequency  $f_c$  of an op-amp having a unit gain frequency  $f_1 = 15 \text{ MHz}$  and voltage differential gain  $G_d = 25 \text{ V/mV}$ . Draw the frequency response.

**Solution:**

$$G_d = 25 \text{ V/mV} = \frac{25 \text{ V}}{10^{-3} \text{ V}} = 25 \times 10^3$$

$$f_1 = G_d f_c$$

$$\therefore f_c = \frac{f_1}{G_d} = \frac{15 \times 10^6}{25 \times 10^3} = 600 \text{ Hz}$$



**Question 10** Design op-amp subtractor circuit to satisfy the following equation:  $V_{out} = 2(V_2 - V_1)$   
Assume the feedback resistance  $R_f = 10\text{k}\Omega$ .

**Solution:**

The circuit diagram of op-amp subtractor is shown as:

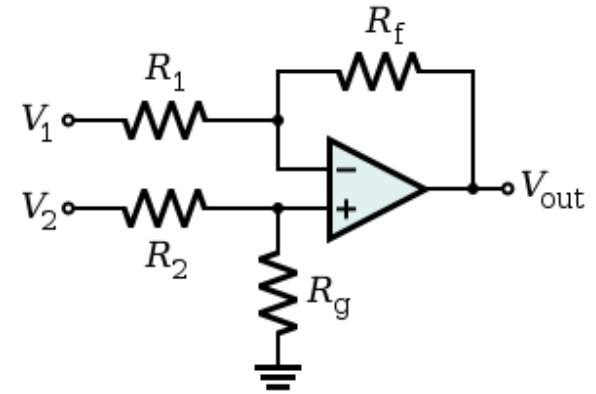
For good design  $R_2 = R_1$  and  $R_f = R_g$ .

Then, the output voltage  $V_{out}$  is given as:

$$V_{out} = \frac{R_f}{R_1}(V_2 - V_1)$$

And we have from the given question  $V_{out} = 2(V_2 - V_1)$

Then by similarity of both equations, we get  $\frac{R_f}{R_1} = 2 \Rightarrow \therefore R_1 = \frac{R_f}{2} = \frac{10\text{k}\Omega}{2} = 5\text{k}\Omega$



**Question 11** Calculate the voltage gain  $A$  for the voltage follower circuit.

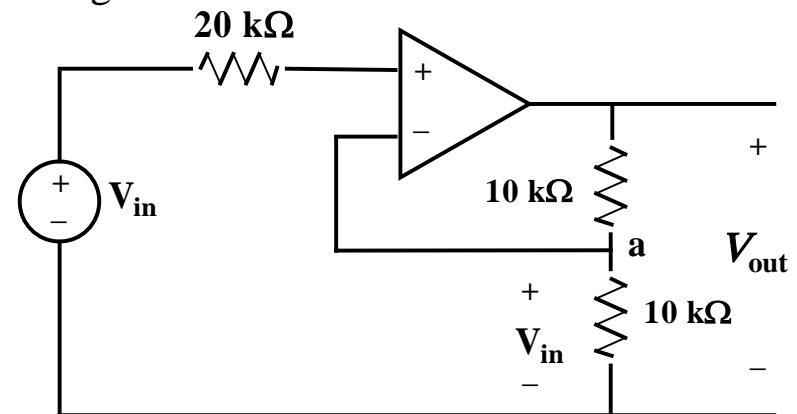
**Solution:**

$$i_+ = i_- = 0$$

$$v_a = v_- = v_+ = V_{in}$$

Using the voltage divider equation at node "a":

$$V_{in} = \left( \frac{10\text{k}\Omega}{10\text{k}\Omega + 10\text{k}\Omega} \right) V_{out} \Rightarrow \therefore A = \frac{V_{out}}{V_{in}} = 2$$



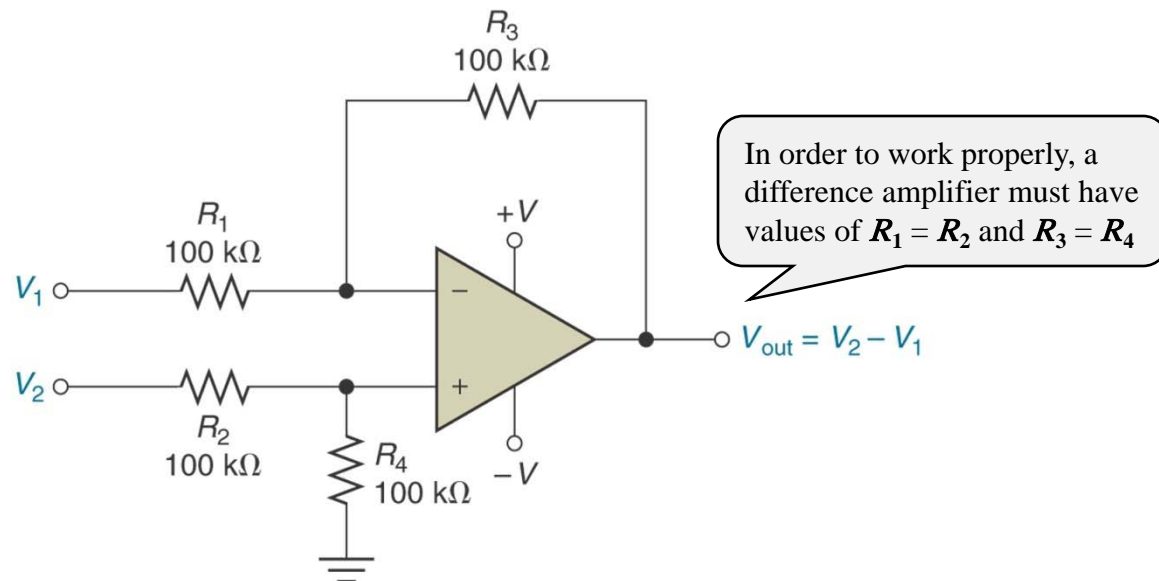
**Question 12** For the given difference amplifier (subtractor), write the equation of output voltage  $V_{out}$ .

**Solution:**

$$V_{out} = \frac{R_3}{R_1} (V_2 - V_1)$$

$$V_{out} = \frac{100\text{k}\Omega}{100\text{k}\Omega} (V_2 - V_1)$$

$$\therefore V_{out} = V_2 - V_1$$



**Question 13** Find  $V_{out}$  for the given op-amp circuit.

**Solution:**  $i_+ = i_- = 0$

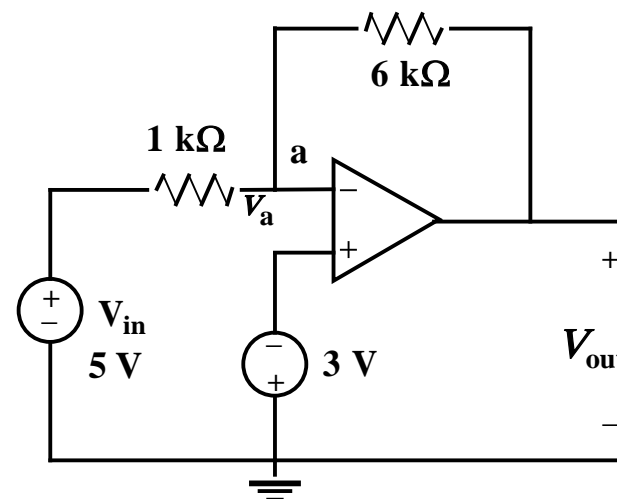
Since the non-inverting terminal is connected to +3 volts, we get

$$v_a = v_- = v_+ = +3 \text{ Volt}$$

Using KCL at the non-inverting node "a":

$$\frac{V_{in} - v_a}{1\text{k}\Omega} = \frac{v_a - V_{out}}{6\text{k}\Omega} + i_-$$

$$\therefore V_{out} = -51 \text{ Volt}$$





**Question 14** For the given non-inverting op-amp, find the output voltage  $V_{out}$ .

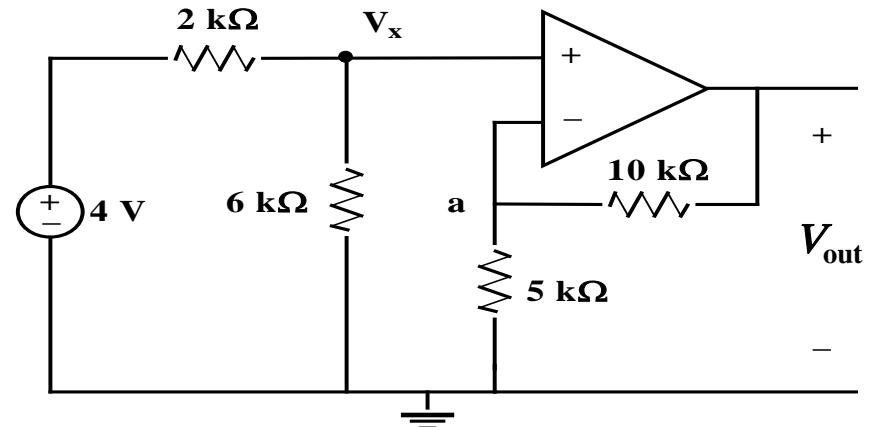
**Solution:**  $i_+ = i_- = 0$

$$v_a = v_- = v_+ = V_x$$

$$V_x = \left( \frac{6\text{k}\Omega}{6\text{k}\Omega + 2\text{k}\Omega} \right) \times 4 = 3\text{Volt}$$

Using the voltage divider equation at node "a":

$$V_a = \left( \frac{5\text{k}\Omega}{5\text{k}\Omega + 10\text{k}\Omega} \right) \times V_{out} \Rightarrow V_{out} = 3 \times V_a = 9\text{Volt}$$



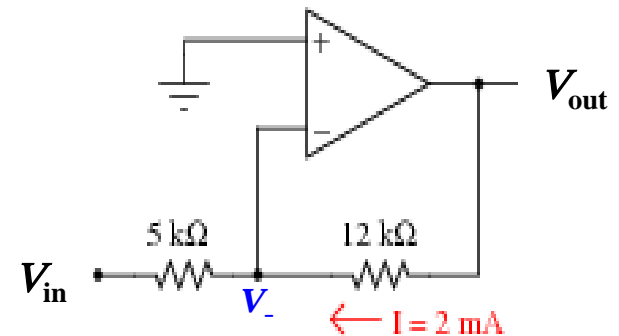
**Question 15** Determine both of input voltage  $V_{in}$  and output voltage  $V_{out}$  for given circuit.

**Solution:**  $i_+ = i_- = 0$

$$v_- = v_+ = 0 \Rightarrow V_{out} = 2\text{mA} \times 12\text{k}\Omega = 24\text{Volt}$$

For the inverting op-amp we have: 
$$V_{out} = -\frac{R_f}{R_1} V_{in}$$

$$\therefore V_{in} = -\frac{R_1}{R_f} V_{out} = -\frac{5\text{k}\Omega}{12\text{k}\Omega} \times 24 = -10\text{Volt}$$



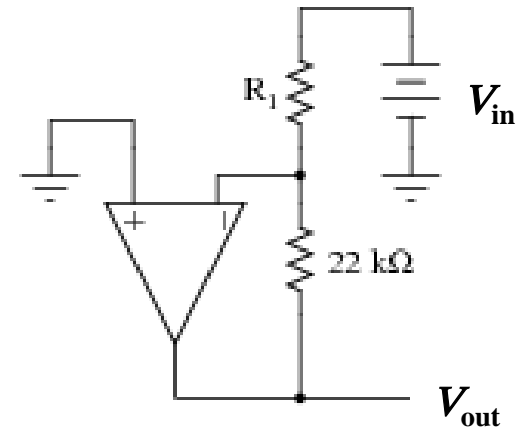
**Question 16** Calculate  $R_1$  to produce a voltage gain of  $A = 15$  in the given op-amp circuit.

**Solution:**

The voltage gain of inverting op-amp is:

$$A = \frac{R_f}{R_1}$$

$$\Rightarrow R_1 = \frac{R_f}{A} = \frac{22\text{k}\Omega}{15} = 1.46\text{k}\Omega$$



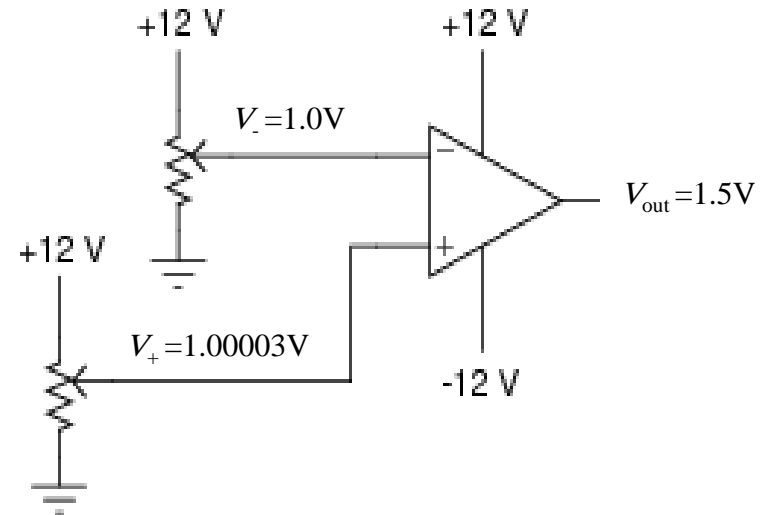
**Question 17** For the given op-amp circuit with two different input voltages. Determine the differential voltage gain  $G_d$  of this op-amp.

**Solution:**

$$V_{out} = G_d V_d$$

$$V_d = V_+ - V_- = 1.00003 - 1 = 30 \times 10^{-6} \text{ Volt}$$

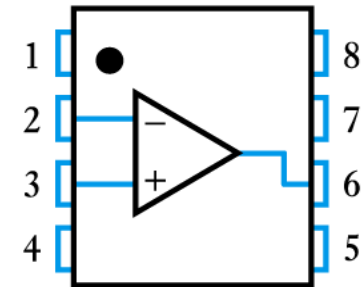
$$\Rightarrow G_d = \frac{V_{out}}{V_d} = \frac{1.5}{30 \times 10^{-6}} = 50000$$



**Question 18** Choose the correct alternative for the following multiple choice questions.

(1) What signal corresponds to pin 3 of this operational amplifier?

- A- The non-inverting output.      B- The positive supply voltage.  
☒ C- The non-inverting input.      D- The inverting input

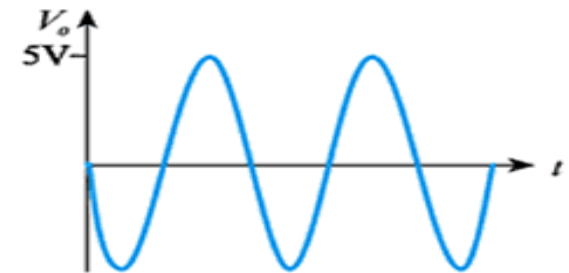
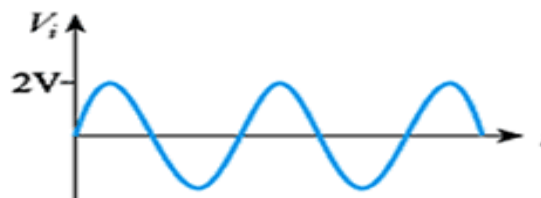


(2) What characteristics would characterize an ideal operational amplifier?

- A- An infinite voltage gain, an infinite input resistance and an infinite output resistance.  
B- An infinite voltage gain, zero input resistance and an infinite output resistance.  
C- An infinite voltage gain, zero input resistance and zero output resistance.  
☒ D- An infinite voltage gain, an infinite input resistance and zero output resistance

(3) The graphs show input and output waveforms of an op-amp. What is the gain of this circuit?

- A) - 0.4    ☒ B) -2.5    C) 2.5    D) 0.4

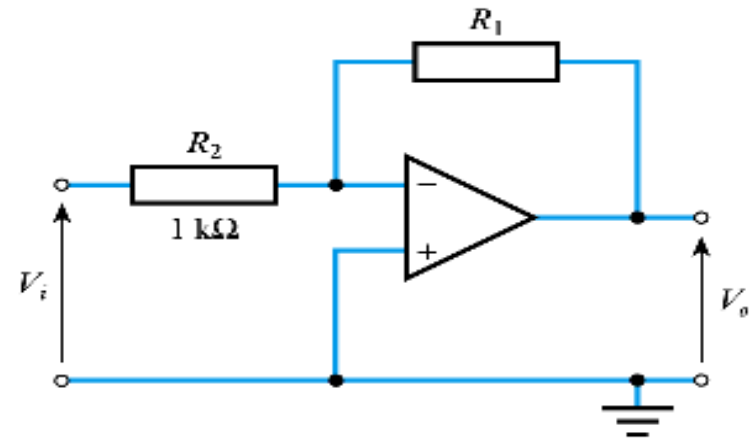


(4) A differential amplifier amplifies the ----- between two input signals.

- A- Addition    ☒ B- subtraction    C- multiplication

(5) In the given circuit, what value of  $R_1$  is required to give a voltage gain of -50 ?

- A) 49 k $\Omega$     ☒ B) 50 k $\Omega$     C) -50 k $\Omega$     D) -49 k $\Omega$



(6) Frequency response of the differentiator is same as that of .....

- ☒ a) high pass filter    b) low pass filter    c) band pass filter

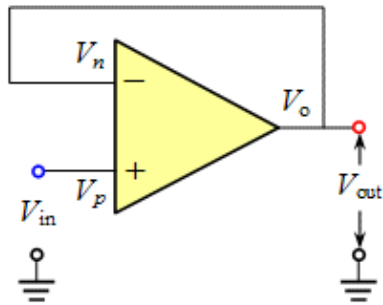
(7) What is the voltage gain of the unity follower?

- a) 0    ☒ b) 1    c) -1    d) infinity

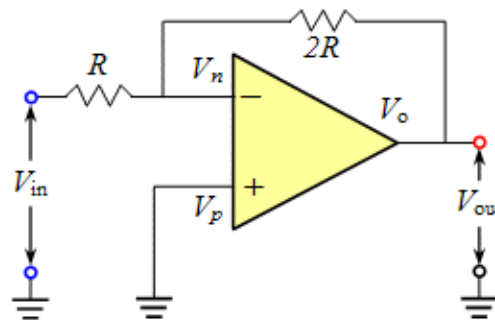
(8) What is the scale multiplier (factor) of a basic integrator?

- a) R/C    b) C/R    c) -RC    ☒ d) -1/RC

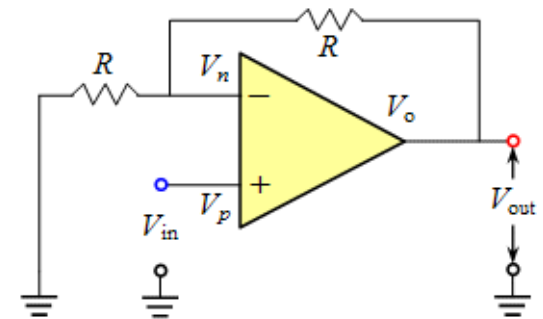
(9) Choose the circuit below that would take a DC input voltage  $V_{in} = 1\text{ V}$  and produce an output voltage  $V_{out} = 2\text{ V}$ .



(a)



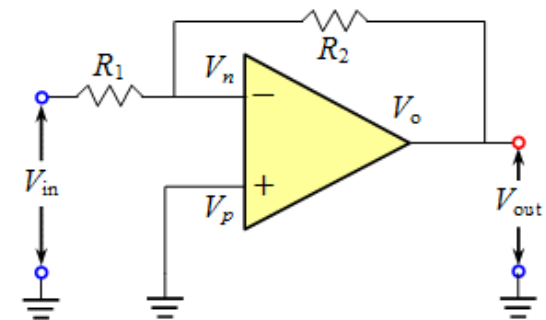
(b)



(c)

(10) If  $R_1 = 10\text{ k}\Omega$ , and  $R_2 = 10\text{ k}\Omega$ , this circuit would be.....

- A) buffer    B) inverting summer    (C) inverter  
D) inverting amplifier    E) noninverting amplifier  
F) low-pass filter    G) high-pass filter



(11) If  $R_1 = 10\text{ k}\Omega$ , and  $R_2 = 20\text{ k}\Omega$ , this circuit would be.....

- A) buffer    B) inverting summer    C) inverter  
D) inverting amplifier    (E) noninverting amplifier

